

Formal Verification  
Coursework 1: NuSMV  
Autumn 2021

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This is the first assessed practical exercise for the Formal Verification course. You will be using the NuSMV model checker to verify CTL and LTL properties.

**Date issued:** Monday 4th October 2021

**Submission date:** Monday 25th October 2021, 4pm

**Mark total:** 50. **Weight:** 20%

**Submission Instructions:** See Section 3.

**Coursework Regulations:** See Section 4.

## 1 Getting Started and Practice Question

Create a new directory for your work on a DICE machine and change to that directory. For instructions on using NuSMV see the *NuSMV Startup Guide*<sup>1</sup>.

Download the coursework files from Learn

The following question is *not* assessed:

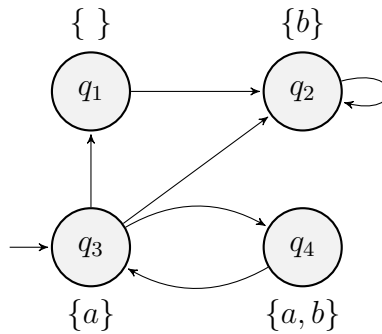


Figure 1: Model for Q1

1. Create a NuSMV model for the system shown in Fig 1. For each of the LTL formulas  $\phi$  below,
  - (a)  $\mathbf{G} a$
  - (b)  $a \mathbf{U} b$
  - (c)  $a \mathbf{U} \mathbf{X} (a \wedge \neg b)$
  - (d)  $\mathbf{X} \neg b \wedge \mathbf{G} (\neg a \vee \neg b)$
  - (e)  $\mathbf{X} (a \wedge b) \wedge \mathbf{F} (\neg a \wedge \neg b)$

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<sup>1</sup><http://www.inf.ed.ac.uk/teaching/courses/fv/nusmv/nusmv-startup.html>

use NuSMV to (i) determine whether the formula  $\phi$  is valid, and (ii) persuade NuSMV to exhibit some path which satisfies  $\phi$ .

*Hints:*

- It's simplest to create a NuSMV model of the state machine that uses 1 state variable with 4 values, one for each of the states of the state machine. Then use DEFINE assignments to specify in which states the atomic propositions 'a' and 'b' are true. An alternative approach that can yield a more compact model, but that can be slightly less straightforward, is to introduce 2 state variables, one for 'a', one for 'b'.
- For (ii), consider what NuSMV does if you direct it to try proving  $\neg\phi$ .

Check that the answers you get with NuSMV correspond to your own understanding of the model and the formulas.

Insert your answers into template file `question1.smv`. At the top of this file you insert your model and a brief explanation of the approach you use for finding satisfying paths. Then, for each part of the question, you give the NuSMV code for the LTL formula, state whether the formula is valid, and give an example satisfying path. You do not need to include this file in your submission.

Compare your solution to `question1-solution.smv`

(0 points, not assessed)

## 2 Questions

These questions are assessed.

2. Consider the transition system  $TS$ , shown in Figure 2, over the set of atomic propositions  $AP = \{a, b, c\}$ . Model this transition system in NuSMV. Insert your answers into template file `question2.smv`.

(3 points)

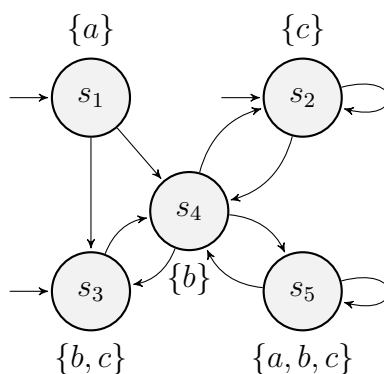


Figure 2: Model for Q2

For each of the LTL formulae  $\phi_i$  below, use NuSMV to determine whether  $TS \models \phi_i$  holds. If  $TS \not\models \phi_i$ , provide a path  $\pi \in Paths(TS)$  such that  $\pi \not\models \phi_i$ , i.e., a counterexample.

- (a)  $\phi_1 = \mathbf{F G} c$
- (b)  $\phi_2 = \mathbf{G F} c$
- (c)  $\phi_3 = \mathbf{X} \neg c \implies \mathbf{X X} c$
- (d)  $\phi_4 = a \mathbf{U G} (b \vee c)$
- (e)  $\phi_5 = (\mathbf{X X} b) \mathbf{U} (b \vee c)$

(5 points)

3. Let  $\Phi$  and  $\Psi$  be arbitrary CTL formula. Which of the following pairs of CTL formulae are equivalent? For those which are, argue briefly why they are equivalent. For those which are not, create a NuSMV module with a model and the two formulas, each as a property to check, such that one property is true of the model and the other false. Use the **CTLSPEC** keyword in NuSMV to introduce CTL properties, just as the **LTLSPEC** keyword introduces LTL properties. Insert your answers into template file `question3.smv`.

- (a)  $\mathbf{EF} \Phi$  and  $\mathbf{EG} \Phi$
- (b)  $\mathbf{EX EG} \Phi$  and  $\mathbf{EG EX} \Phi$
- (c)  $\mathbf{AF} a \vee \mathbf{AF} b$  and  $\mathbf{AF} (a \vee b)$
- (d)  $\top$  and  $\mathbf{AG} \Phi \implies \mathbf{EG} \Phi$
- (e)  $\mathbf{AG} \Phi$  and  $\Phi \vee \mathbf{AX AG} \Phi$
- (f)  $\mathbf{EF EG} \Phi$  and  $\mathbf{EG EF} \Phi$
- (g)  $\mathbf{E}(\Phi \mathbf{U} \Psi)$  and  $\mathbf{E}(\Phi \mathbf{U} (\neg \Phi \wedge \Psi))$
- (h)  $\mathbf{AG}(\Phi \implies \Psi)$  and  $(\mathbf{EX} \Phi \implies \mathbf{EX} \Psi)$
- (i)  $\mathbf{AF AG} \Phi$  and  $\mathbf{AG AF} \Phi$
- (j)  $\mathbf{A}(\Phi \mathbf{W} \Psi)$  and  $\neg \mathbf{E}(\neg \Phi \mathbf{W} \neg \Psi)$

(10 points)

4. In the following questions you will verify properties of a model of a FIFO digital circuit.

A block diagram of the FIFO (First In First Out) circuit is shown in Figure 3.

Abstractly, a FIFO is a variable-length queue of data words. It has two interfaces, one *input interface* for adding words to one end of the queue and one *output interface* for reading and removing words from the other end of the queue.

The hardware circuit is a *synchronous* circuit. Its behaviour is governed by a Boolean **clock** signal input which usually alternates between *true* and *false* at a uniform frequency. Each time the **clock** changes from *false* to *true*, the internal state of the circuit is updated, based on the current internal state and inputs to the circuit at that time. When modelling a synchronous circuit in NuSMV, we do not explicitly include the **clock** signal. Rather, we design a transition system that takes one step per clock cycle and that uses the transition relation to specify how the internal state is updated based on the current state and inputs. In general synchronous circuits might have outputs that depend both on the current state and the inputs. Here we use a restriction of this scheme where the outputs depend only

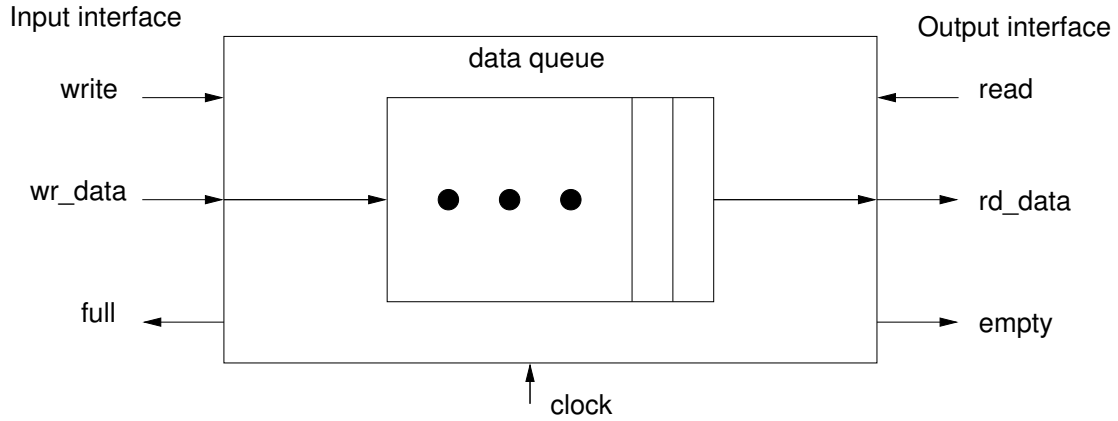


Figure 3: FIFO Block Diagram

on the current state. For simplicity, the following description of FIFO behaviour is in terms of the transition system model rather than the hardware circuit.

To add or write a word of data to the FIFO, the data is presented on the *write data* `wr_data` input and the Boolean signal `write` is asserted (set to *true*). Providing the FIFO is not currently full, the write data word is then added to the queue on the transition to the next step. The FIFO has a maximum number of words it can hold in the queue at any one time. The Boolean `full` output of the FIFO indicates whether or not it currently holds the maximum number.

The *read data* `rd_data` output of the FIFO shows the current end word in the FIFO's internal queue, providing that the queue is not empty. The queue being empty is signalled by the Boolean `empty` output being set to *true*. If the Boolean `read` signal is set to *true* and the queue is not empty, on the transition to the next step the current end word in the queue is removed and the word behind it (if any) then appears on the FIFO `rd_data` output.

The provided file `fifo.smv` presents the NuSMV FIFO model. Have a look at the model. For simplicity and to ensure rapid NuSMV execution times, we set the `DEPTH` constant for the maximum number of words to 5 and the `WIDTH` constant for the word size to 1. In practice we would often use larger values for both parameters.

Internally, the FIFO uses a *circular buffer* to implement the queue. This consists of an array `buffer` of words of size `DEPTH` and two pointers into this array, the *read pointer* `rd_p` and the *write pointer* `wr_p`. If the queue is not empty, the read pointer points to word which is the current output word of the queue and, if the queue is not full, the write pointer points to the position to write the next input word. When a new word is written into the queue, the write pointer is incremented, wrapping it around as necessary. When a word in the queue is removed, the read pointer is incremented, wrapping it around as necessary. See Figure 4 for two examples of the internal configuration of the FIFO when the queue holds the words `w0`, `w1` and `w2`, added in that order.

With the provided FIFO realisation, the FIFO could be either empty or full when the two pointers are equal. The design uses the Boolean `empty` internal state variable to distinguish between these two cases.

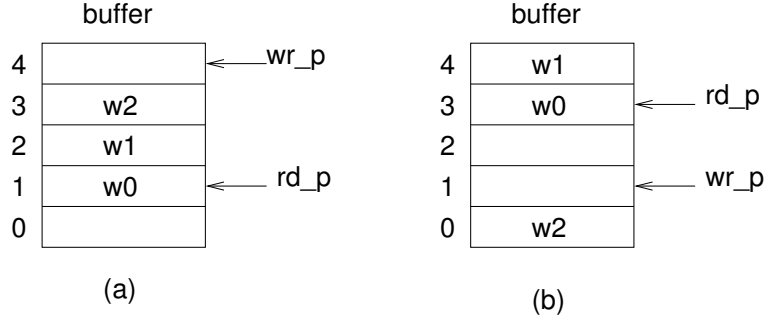


Figure 4: Examples of internal FIFO configurations

- (a) In the provided template file `fifo-properties.smv`, add formulas for the LTL properties requested below (i,ii, iii, iv, v, vi). Verify your properties with NuSMV by running the command

```
NuSMV -pre cpp fifo.smv
```

The `fifo.smv` file brings in the `fifo-properties.smv` file using a preprocessor `#include` directive at its end. The `-pre cpp` option to NuSMV here is necessary to ensure it runs the C preprocessor on `bridge.smv` in order to interpret this directive. If you don't want to see counter-examples for false formulas, also add the `-dcx` option.

All the properties should be found true of the FIFO model in `fifo.smv`.

- i. the property

*It is never the case that the FIFO indicates simultaneously it is both empty and full.*

This is an example of a *safety* property. Safety properties in general are about undesired behaviour not happening.

- ii. the property

*If write is asserted forever and read is never asserted, then the FIFO eventually becomes full.*

This is an example of a *liveness* property. Liveness properties in general are about desired behaviour actually happening.

- iii. the property

*At any time, if a 1 is presented to the FIFO data input and write is asserted, then eventually a 1 will appear on the FIFO data output*

with further reasonable assumptions added after the *if* concerning FIFO signals such as `read`, `empty` or `full`, to ensure the property checks true.

- iv. the same property as in (iii), except that it is phrased to hold for any data value, not just the value 1. Use the 'frozen variable' `data1` to do this. Consult the NuSMV user guide for documentation on *frozen variables* (also sometimes known in temporal logic as *rigid variables*).
- v. the same property as in (iii), except that, in addition, it requires the `empty` output of the FIFO to be set to false at all times *inbetween* the time the write of the data is set up and the time the data can first be read out, but not actually at either of these times. You may take advantage of the

fact that the earliest we expect the data to appear is the step after it is written.

- vi. a similar property to that for (iv), except that it assumes that two possibly-distinct data values are input on consecutive steps, and checks for the same two values appearing on the output on consecutive steps. Use the provided frozen variables `data1` and `data2` to refer to the two data values.

(12 points)

- (b) Write CTL formulas for the following properties and verify the properties with NuSMV. All the properties should be found true,

- i. the property

*there exists a run for which, at some time onwards, the FIFO is always full,*

- ii. the property

*from every reachable state in which the FIFO is full, there exists a path along which the FIFO eventually becomes empty.*

(4 points)

Both of the above properties should be found true of the FIFO model in `fifo.smv`.

- 5. The FIFO has a bug. In this part you discover and fix it.

- (a) In the indicated place in `fifo-properties.smv`, write an LTL property that checks that

*always, if the FIFO indicates it is empty, then the read and write pointers are equal.*

NuSMV should find it false and show a counter-example.

(2 points)

- (b) Give a summary of the behaviour found in the shortest counter-example in the indicated place in the `fifo-properties.smv` file.

(2 points)

- (c) Make a copy of `fifo.smv` called `fifo-fixed.smv`. Make changes to the code in the `main` module in the `fifo-fixed.smv` file to fix this bug. Your changes should address the general problem identified by this bug. Full marks will not be given if you just make some minimal change such that the particular property you wrote to identify the problem now checks true.

Do *not* alter `fifo.smv`.

At the top of `fifo-fixed.smv`, add comments briefly describing your diagnosis of the problem and why your changes fix it.

(4 points)

- 6. As remarked in lecture, in LTL model checking of a formula  $\phi$ , one constructs a Büchi automaton for  $\neg\phi$  which accepts just those paths  $\pi$  as input that satisfy  $\neg\phi$ . The formula is then true just when the language accepted by this automaton intersected with that accepted by the model automaton is empty.

Let  $\phi$  be the LTL property  $\mathbf{G}(\text{full} \wedge \text{read} \Rightarrow \mathbf{X} \neg\text{full})$ .

- (a) Write  $\neg\phi$  in a normalised form, where the negations are pushed inwards so they just surround atomic formulas and the only binary logical connectives used are  $\wedge$  and  $\vee$ . This should simplify the writing of a Büchi automaton for  $\neg\phi$ .  
(3 points)
- (b) Write a NuSMV module that emulates a Büchi automaton for  $\neg\phi$ . *Hint:* you should not need an automaton with more than 3 or 4 states.  
(3 points)
- (c) Write an LTL property that captures the acceptance condition of the Büchi automaton, that, if true, indicates that there are no accepting runs of the automaton.  
(2 points)

Insert your solution into the file `fifo-ltlmc.smv` in the indicated positions at the start. This file include a copy of the module from `fifo.smv`, but with the `main` module renamed to `system` and a new `main` module that composes the system with the negated formula automaton.

## 3 Submission

### 3.1 Packaging your submission

Make sure all of your NuSMV files are in one folder, called `fv-cw1`. Make a compressed version of your project folder (including a pdf of your solutions, and all the NuSMV files you used) using zip compression:

- On Linux systems use the command `zip -r fv-cw1.zip fv-cw1`
- On Windows systems use **Send to** > **Compressed (zipped) folder**.
- On Mac systems use **File** > **Compress "fv-cw1"**.

You should now have a file called `fv-cw1.zip`.

### 3.2 How to submit

Ensure that you are LEARN-authenticated by visiting <http://learn.ed.ac.uk>. Go to the Formal Verification LEARN page. Click on the Assessment link in the left-hand margin bar and then the link that says **Coursework 1: NuSMV - Submission**. Use the Browse Local Files option to find and upload your ZIP file.

In order to streamline the processing of your submissions, and help avoid lost submissions, please use exactly these filenames. When finished, make sure that you click Submit.

This submission mechanism should allow you to make multiple submissions. Later submissions will over- write earlier ones. Submissions which arrive after the coursework deadline will be subject to the School's late submission penalties as detailed at

<http://web.inf.ed.ac.uk/infweb/student-services/ito/admin/coursework-projects/late-coursework-extension-requests>.

Extension Rule 1 will be applied for submissions “Extensions are permitted (7 days) and Extra Time Adjustments (ETA) for extensions are permitted”. The complete statement of this rule is available at the URL above.

## 4 Coursework Regulations

### 4.1 Good scholarly practice

Please remember the good scholarly practice requirements of the University regarding work for credit. You can find guidance at the School page:

`https://web.inf.ed.ac.uk/infweb/admin/policies/academic-misconduct`

This also has links to the relevant University pages. You are required to take reasonable measures to protect your assessed work from unauthorised access. For example, if you put any such work in a source code repository then you must set access permissions appropriately, limiting access to at most yourself and members of the formal verification course team.

You may collaborate with other students *only* on the first unassessed question. All work that you submit for assessment must be your own.

### 4.2 Late submission policy

It may be that due to illness or other circumstances beyond your control that you need to submit work late. Submissions which arrive after the coursework deadline will be subject to the School’s late submission penalties as detailed at

`http://web.inf.ed.ac.uk/infweb/student-services/ito/admin/coursework-projects/late-coursework-extension-requests`.

Extension Rule 1 will be applied for submissions for Coursework 1 and Coursework 2. This states that “Extensions are permitted (7 days) and Extra Time Adjustments (ETA) for extensions are permitted.” The complete statement of this rule is available at the URL above.