# Methods for Causal Inference Lecture 1

### Ava Khamseh School of Informatics



2021-2022

### Logistics

These lectures are being recorded.

- Lectures: Mondays and Thursdays at 10:00-11:00am
- Tutorials: Every other week Wednesdays 12:00-1:00pm
  40GS\_LG.07 Teaching Studio, first session: 26/01/2022
- Slides and recordings will appear on Learn
- Office Hours: Wednesdays 15:00-17:00
- Email me any questions, happy to discuss!

#### References

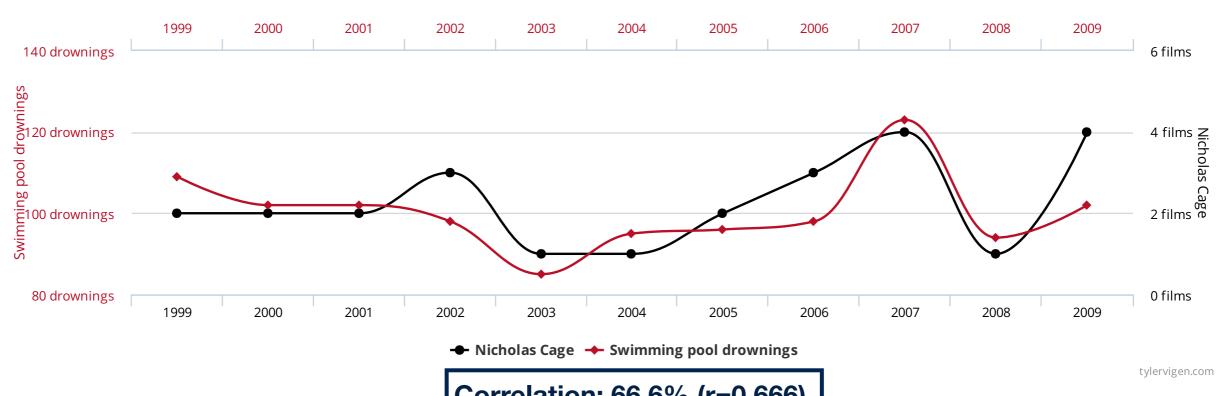
- Causal Inference in Statistics: A Primer (Pearl, Glymour, Jewell, 2016)
- More advanced: Causality (Pearl, 2009)
- Elements of Causal Inference: Foundations and Learning Algorithms (Peters, Janzing and Schölkopfk)
- Many other papers from the literature ... (will be referenced)

### Spurious correlation (random coincidence)

#### Number of people who drowned by falling into a pool

correlates with

#### Films Nicolas Cage appeared in



Correlation: 66.6% (r=0.666)

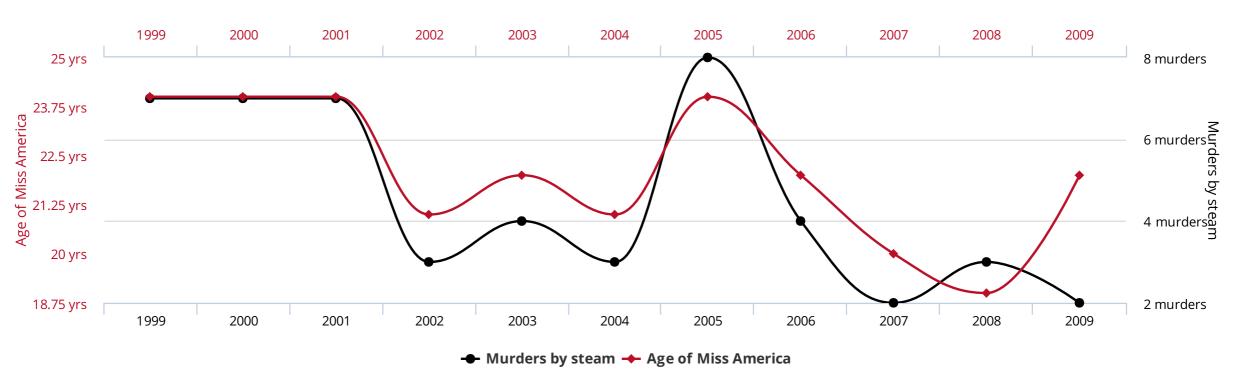
tylervigen.com/spurious-correlations

### Spurious correlation (random coincidence)

#### **Age of Miss America**

correlates with

#### Murders by steam, hot vapours and hot objects



Correlation: 87.01% (r=0.8701)

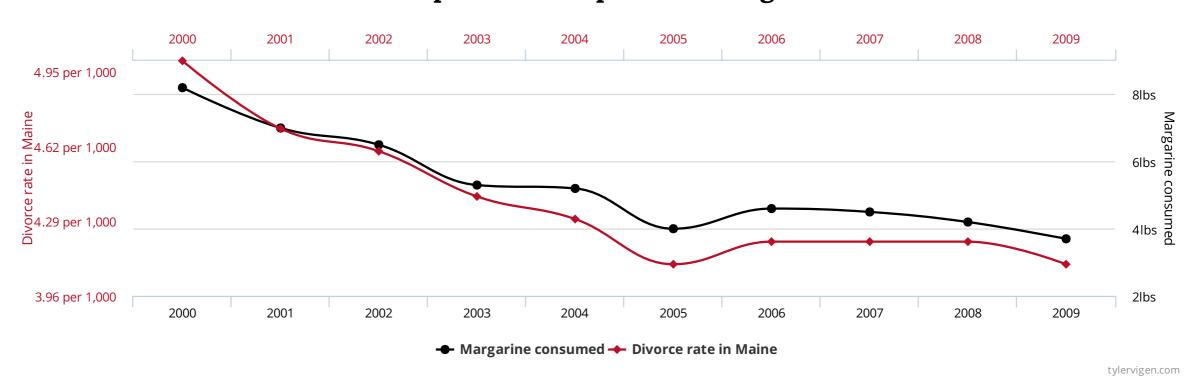
tylervigen.com

### Spurious correlation (random coincidence)

#### Divorce rate in Maine

correlates with

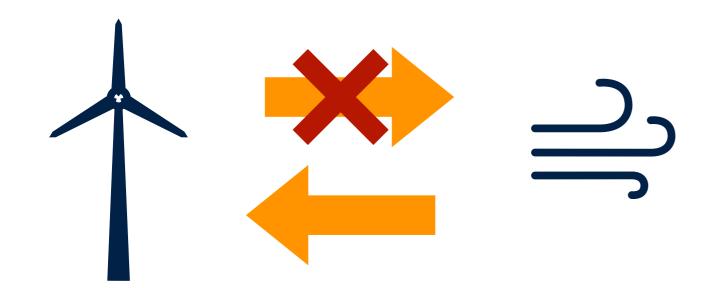
#### Per capita consumption of margarine



Correlation: 99.26% (r=0.9926)

#### **Reverse causation:**

The faster the wind-turbine rotates, the more wind is observed. Therefore, rotation of turbines is the cause for winds!



#### Circular/bidirectional cause and consequence:

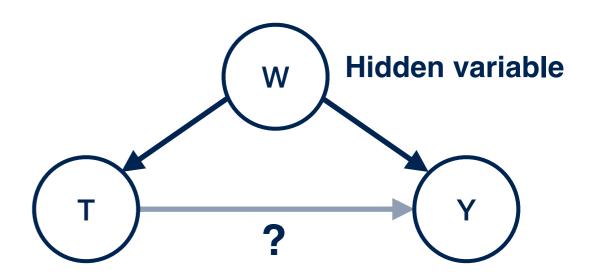
Hours spent on Netflix and weight gain

Hours spent on Netflix -> Less activity -> increase in weight Weight gain -> exercising becomes harder -> more time online as hobby



#### **Confounding factor:**

- Fever is not a cause of sneezing, they are both symptoms of flu (No arrow)
- Treatment outcome relationship confounded by age



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- To understand how and why interventions affect outcomes
- Predict what would have happened under a different intervention:
  "What if I were to act differently?"

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- Controversial examples:
- Biomedical: "Vaccines lead to autism"
- Political/Economical: "increases minimum wage, increases unemployment (people become lazy)"

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- Political: How social media posts from famous individuals (e.g. celebrities, ex-political figures, etc.) influence elections

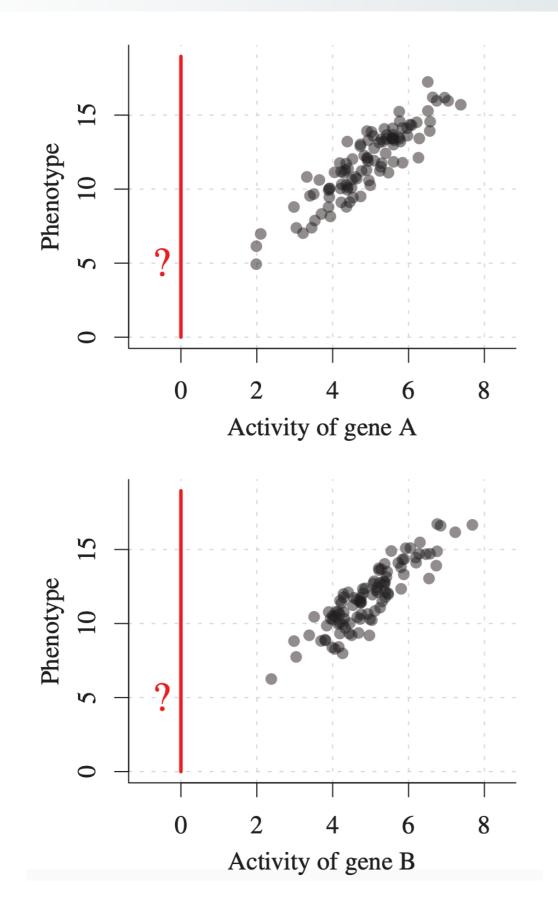
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- Environmental: Is the constant energy consumption in region X due to the regions's energy efficiency standards or due to its mild climate, demographics
- Education: People with feature X are more likely to obtain an internship in tech

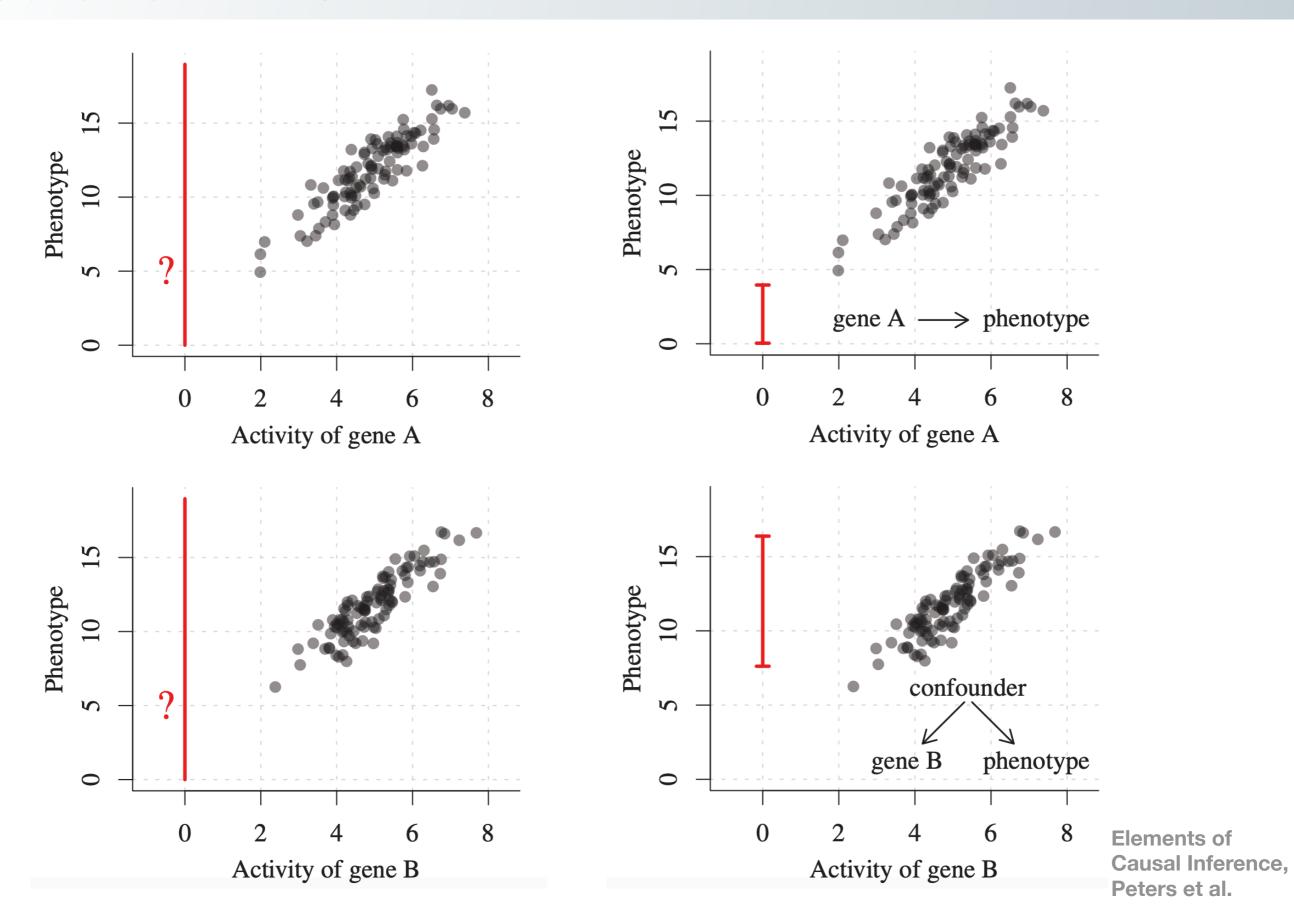
#### Personalised Medicine

- Patient diagnosed with a particular disease
- Certain baseline covariates are known, e.g. age, weight, BMI, blood sugar, ...
- Question: Should treatment A or treatment B be given
  - What is the causal effect of A vs B
  - Design a policy: Features —> {A,B}
  - i.e. best treatment for a given individual
- Source: Electronic Health Records

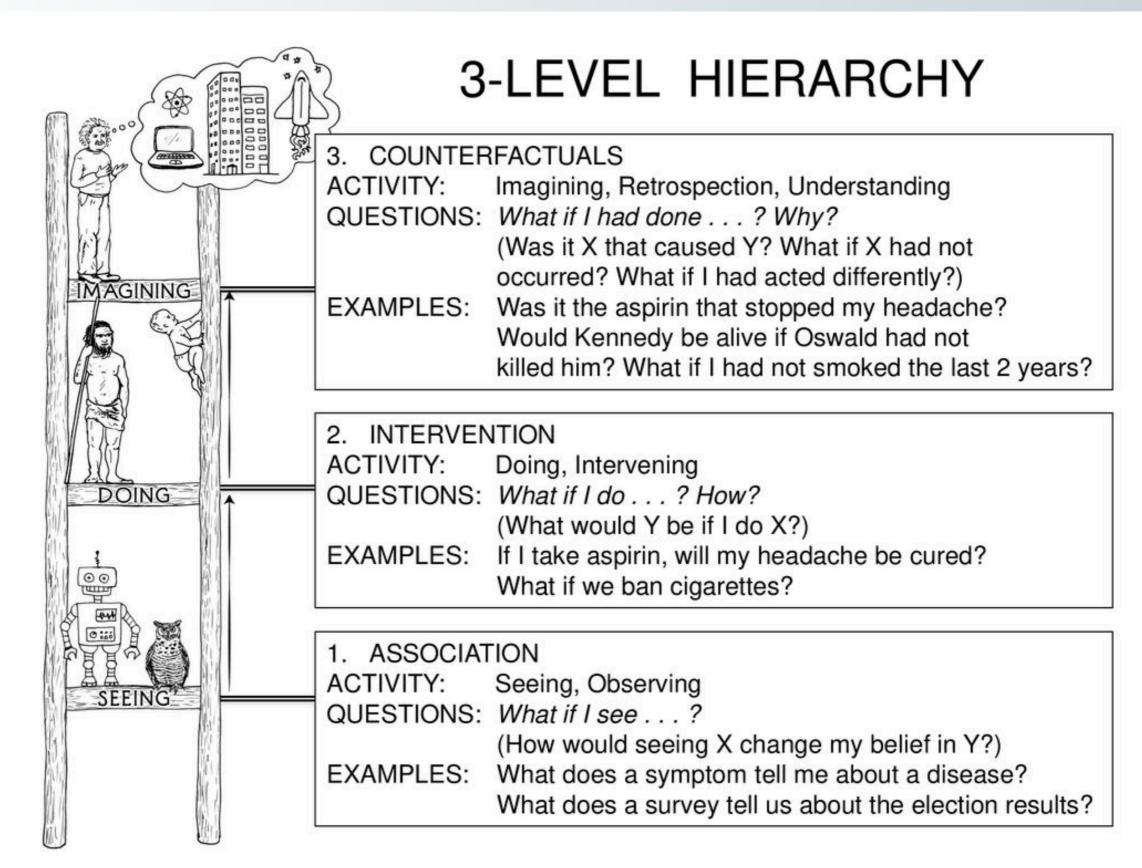
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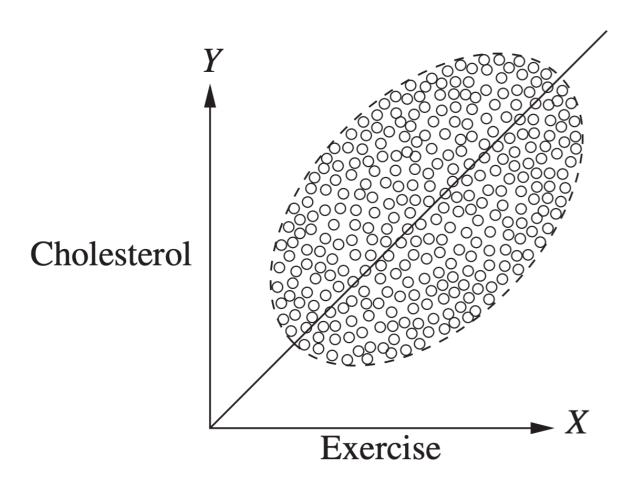


### Pearl's ladder of causation



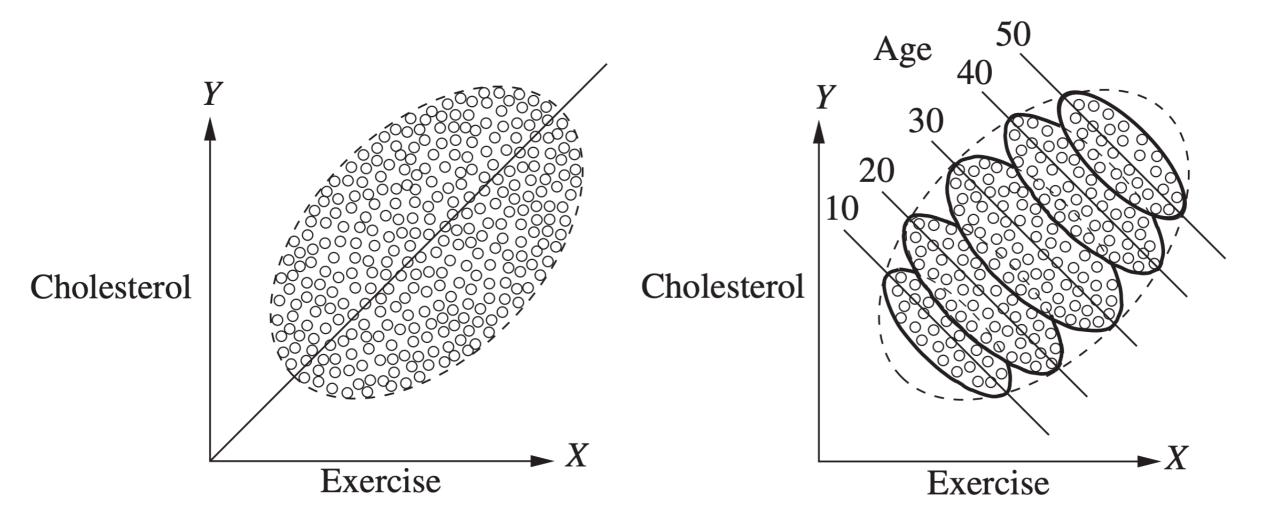
# Simpson's Paradox

 Why concluding causality from purely associational measures, i.e. correlation, can be **very wrong** (not just neutral): "It would have better not to make any statements!"



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## Example with numbers

We will come back to this example after having built the causal calculus how the causal effect can be detected accurately (without us suffering ...)

## Language of causality and the roles of variables

"What intervention", "how much", "when", "how often", "Control", "effect of", "why did", "what if", ...

Causality language

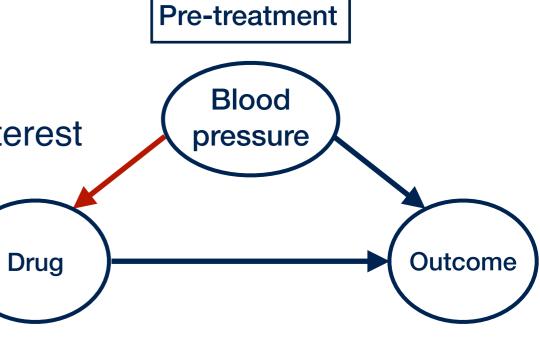
Consider all variables affecting the system of interest and the role each plays.

Patient: Info on DNA variants and biomarkers, traits/disease, confounders

Clinician: What drug, what dose, when, how often, ...

Consider all variables affecting the system of interest and the role each play (as far as possible)

Blood pressure is a **confounder** here:



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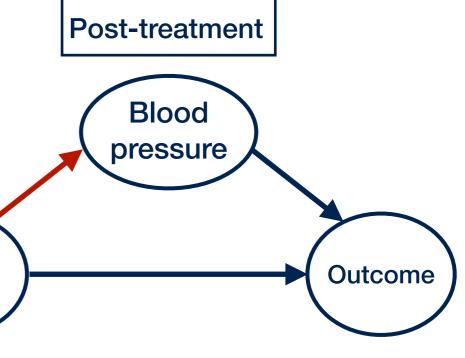
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**Drug** 

Clinician: What drug, what dose, when, how often, ...

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Blood pressure is a **mediator** here:



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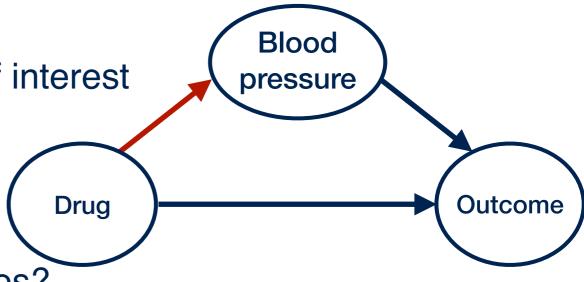
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Clinician: What drug, what dose, when, how often, ...

Consider all variables affecting the system of interest and the role each play (as far as possible)

Blood pressure is a **mediator** here:

What happens when there are lots of variables?

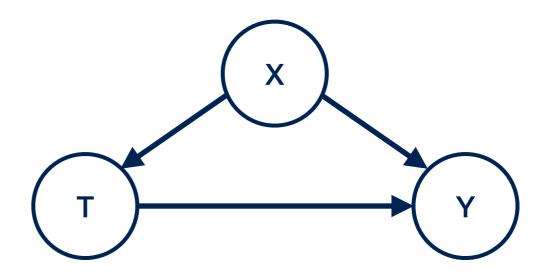


#### Conventions

Variable to be manipulated: treatment (T), e.g. drug

 Variable we observe as response: outcome (Y), e.g. success/ failure of drug

- Other observable variables that can affect treatment and outcome causally and we wish to correct for: confounders (X), e.g. age, sex, socio-economic status, ...
- Unobservable confounder (U)



### **Causal Estimation of Effects**

 Have a prior causal knowledge (may be incomplete) and know the treatment/outcome pair, c.e., weight gain, hours online

• Interested in estimating the **effect size**:

$$\mathbb{E}[y_{t=1}(x) - y_{t=0}(x)] = \int (y_1(x) - y_0(x))p(x)dx$$

Note: The features/confounders x for both treatment and control groups are drawn from the **same** distribution p(x)

• Goal: Find an unbiased estimator, e.g. signal/noise ratio

### Randomised experiments: Already in causal framework

- In a randomised experiment, p(x) is designed to be the same for both treatment groups (t=0 or t=1), typically uniform
- Paired 'clones' in treatment and outcome groups
- Simply take the difference of the averages:

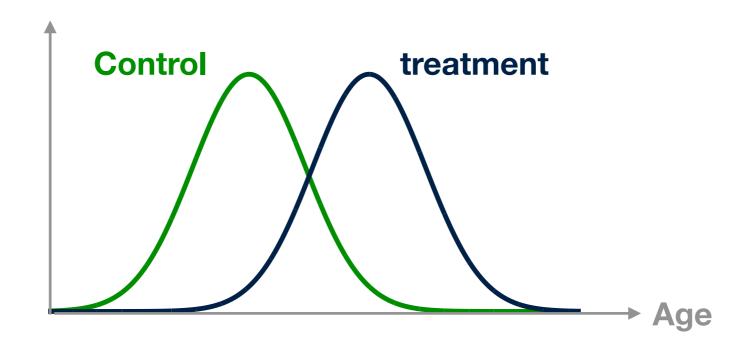
$$\Delta \hat{\mu} = \hat{\mathbb{E}} [y_{t=1}(x) - y_{t=0}(x)] = \frac{1}{N} \sum_{i=1}^{N} (y_1^{(i)}(x) - y_0^{(i)}(x))$$

Statistical test: e.g. T-test and p-values ...

$$\frac{\Delta \hat{\mu}}{\sqrt{\frac{(\hat{\sigma}_{\Delta \mu})^2}{N}}} > t^*$$

### Observational data: What goes wrong?

$$p(x|t=1) \neq p(x|t=0)$$



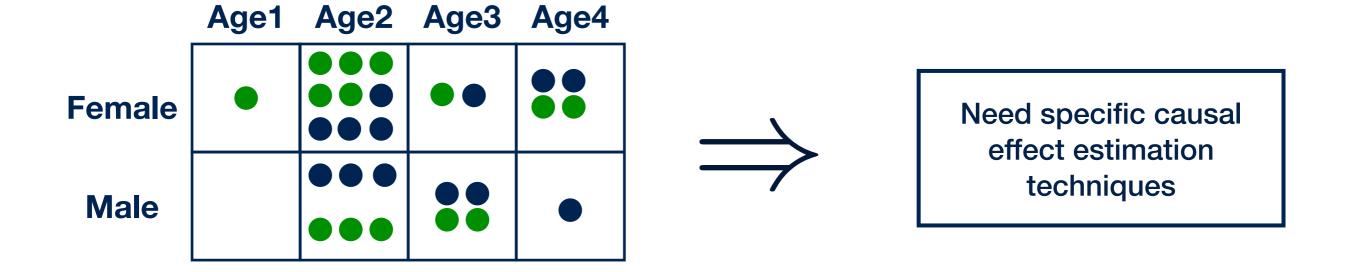
$$\left( \int y_1(x)p(x|t=1)dx - \int y_0(x)p(x|t=0)dx \right) \neq \int (y_1(x) - y_0(x))p(x)dx$$

#### Observational data: Stratification

- Measure outcome (success/failure), within each of the young/old groups separately
- Take weighted average by the probability of being young/old

$$\mathbb{E}(\text{Healed}|t=1) = \mathbb{E}(\text{Healed}|t=1,\text{young})p(\text{young}) + \mathbb{E}(\text{Healed}|t=1,\text{old})p(\text{old})$$

- Disadvantages:
  - All possible confounders need to be observed
  - Assumes overlap between the two distributions (if there is no overlap, sample is not representative, e.g. performing the experiment only for old people )
  - Bad estimates as confounder dimensionality increases



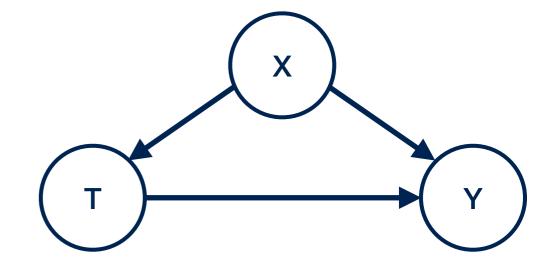
## Two main Frameworks for causal estimation/discovery

#### Potential outcomes (Rubin):

- Requires a given treatment-outcome pair (known directionality)
- Mainly applies to causal estimation (learning effects)
- More familiar to biologists

#### Structural causal models (Pearl):

- Causal graph
- Structural equations
- Algorithmic: Causal Discovery



 $x = f_x(\epsilon_x), \ t = f_t(x, \epsilon_t), \ y = f_y(x, t, \epsilon_y)$ 

Extend the language of probability theory:

do-calculus

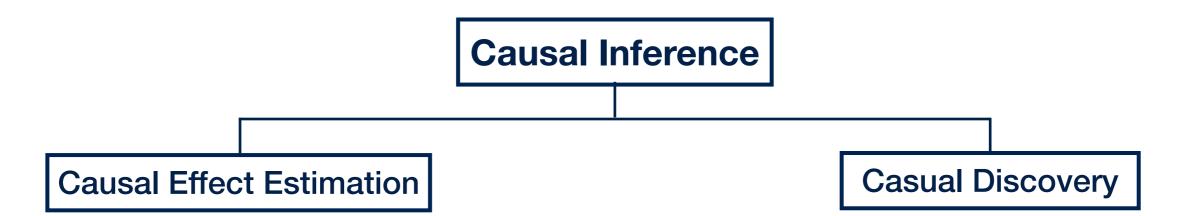
Assumption: Independent noise terms:  $\epsilon_x \perp\!\!\!\perp \epsilon_t \perp\!\!\!\perp \epsilon_y$ 

• Lecture 1: Introduction & motivation, why do we care about causality? Why deriving causality from observational data is non-trivial.

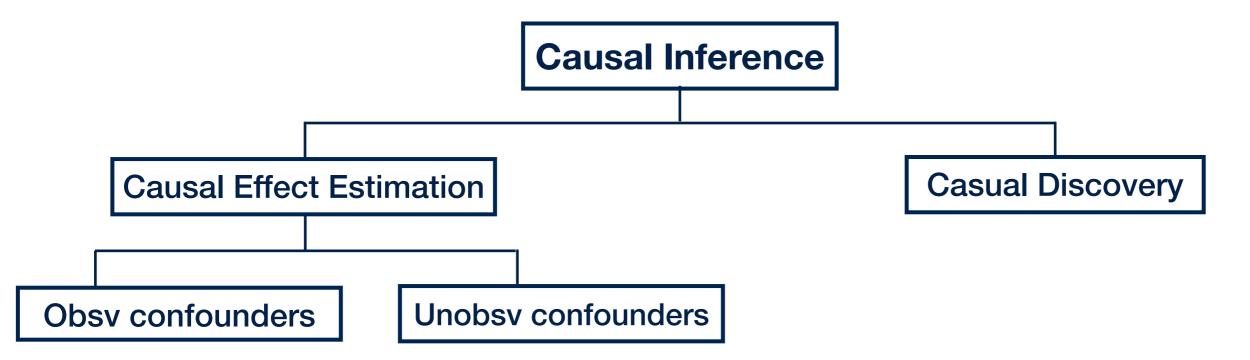
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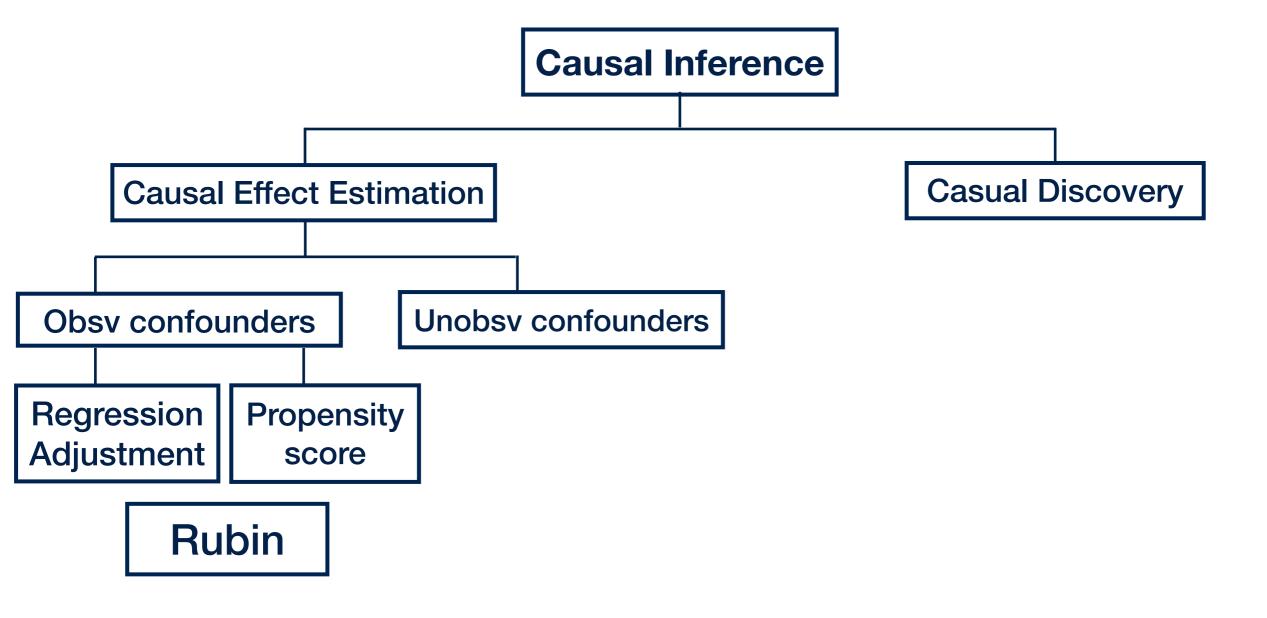
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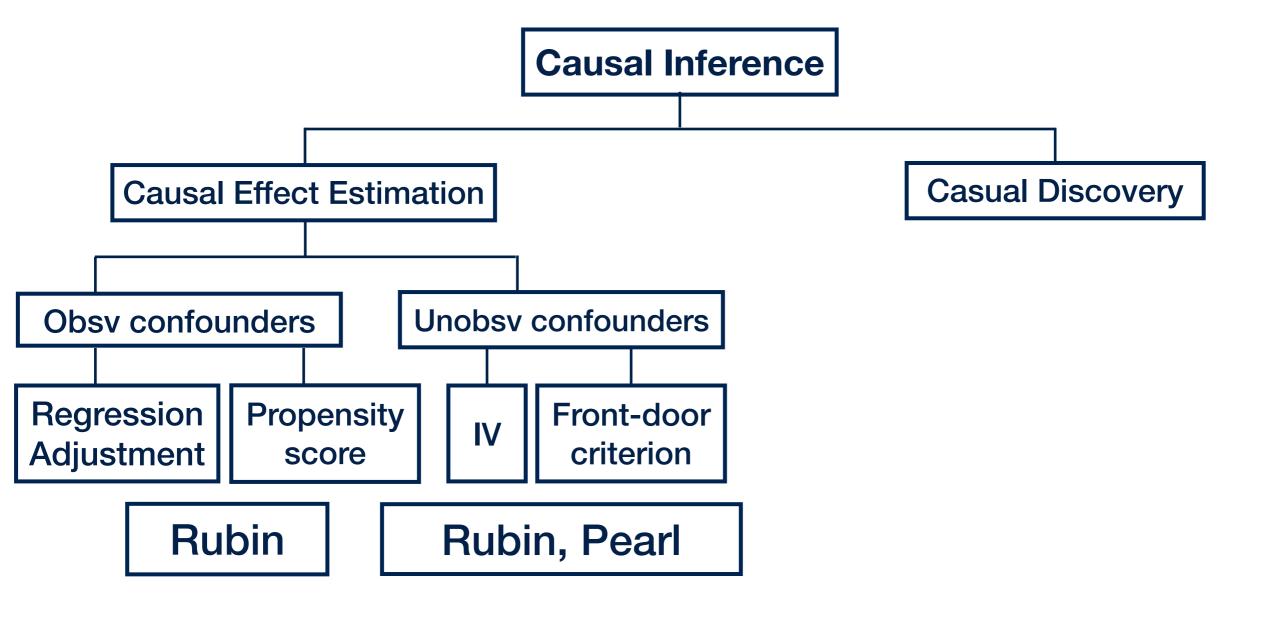
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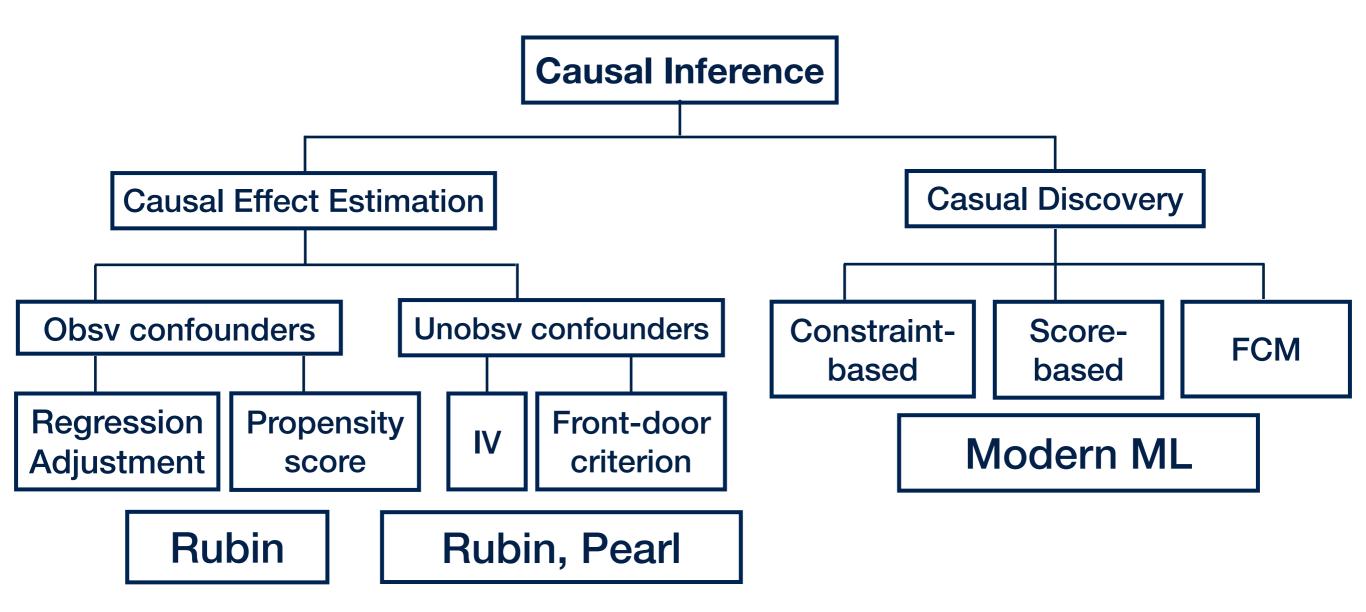
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## Causal Estimation of Effects vs Causal Discovery

- How much would some variables (features or labels)
  change if we manipulate the value of another variable?
  - Have a prior causal knowledge (may be incomplete)
  - Wish to estimate degrees of causal dependencies
- By modifying the value of which variables could we change the value of another variable?
  - Wish to discover the causal graph
  - Apply causal inference