

Assignment_Two Q2

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```
name<- Sys.info()
name[7]
  user
"erico"
```

```
library(rlang)
library(dplyr)
library(kableExtra)
library(ggdag)      # For plotting DAGs
library(dagitty)    # For working with DAG logic
library(modelsummary) # For making regression tables
library(AER) # this package has lots of applied metrics packages
library(foreign)
# Helpful for reading in data from Stata or other code languages
library(lubridate) # For figures
library(stargazer) # For tables
library(data.table) # data manipulation and wrangling
library(lme4)
library(psych)
library(readxl) # Read in data
library(expss) # value labelling from spss style
library(readstata13)
library(marginaleffects) # To calculate marginal effects
library(knitr) # Alternative table package
set.seed(03262020) # random number generators; same numbers across machines
```

```
#https://stat.ethz.ch/pipermail/r-help/2017-August/448710.html
```

```
load("C:/Users/erico/Desktop/ACADEMICS/MY UofT COURSES/YEAR TWO/SEMESTER ONE/HAD5744H Ap
```

Loading objects:

addvars

```
file.exists("C:/Users/erico/Desktop/ACADEMICS/MY UofT COURSES/YEAR TWO/SEMESTER ONE/HAD5  
[1] TRUE
```

```
ls()
```

```
[1] "addvars" "name"
```

```
mydata<-addvars
```

```
#library(readr)
```

```
library(R.utils)
```

```
saveObject(addvars, "C:/Users/erico/Desktop/ACADEMICS/MY UofT COURSES/YEAR TWO/SEMESTER  
mydata1 <- loadObject("C:/Users/erico/Desktop/ACADEMICS/MY UofT COURSES/YEAR TWO/SEMESTER
```

```
#name of stored object is addvars
```

```
mydata2 <- read.dta("C:/Users/erico/Desktop/ACADEMICS/MY UofT COURSES/YEAR TWO/SEMESTER
```

```
mydata2<- select (mydata2, RCT_ID_TV2, post_ie_charges_180_IP,  
Ireadmit2_180_100,  
Iaa_100, Ihispanic_100, Iwhite_100, Irace_other_100)
```

```
mydata1<- select (mydata1, RCT_ID_TV2, link2care_duration, Icontrol, Itreatment,  
Imale)
```

```
mydata<- merge(mydata1, mydata2, by = c("RCT_ID_TV2"), all =T)
```

```
mydata <- mydata %>% mutate(treated=ifelse(link2care_duration>89,1,0))
```

```
mydata <- mydata %>% mutate(random=ifelse(Itreatment==1,1,0))
```

```
mydata <- mydata %>%mutate(rand_treated=ifelse(random==1&treated==1,1,0))
```

```
mydata <- mydata %>% mutate(rand_untreated=ifelse(random==1&treated==0,1,0))
```

```
mydata <- mydata %>% mutate(male=ifelse(Imale==1,1,0))
```

```
mydata <- mydata %>% mutate(african_american=ifelse(Iaa_100==100,1,0))
```

```
mydata <- mydata %>% mutate(hispanic=ifelse(Ihispanic_100==100,1,0))
```

```
mydata <- mydata %>%mutate(white=ifelse(Iwhite_100 ==100,1,0))
```

```
mydata <- mydata %>% mutate(other=ifelse(Irace_other_100 ==100,1,0))
```

```
mydata <- mydata %>% mutate(readmit=ifelse(Ireadmit2_180_100==100,1,0))

#correct name
#mydata <- select and merge

#merge the Dataset 2b RCT and also the RCT additional variables to create the;
#Ireadmit2_180_100 and post_ie_charges_180_IP
```

#Question A

Voluntary participation in the program introduces selection bias (or endogeneity) into the RCT. In the DAG, gender affects both program participation and the rate of 180-day readmission. It also affects the rate of 180-day readmission through program participation.

It is possible that there are unobserved characteristics of individuals that affect both individual program take up and the rate of hospital readmission and it may account for any association between program participation and the 180-day hospital readmission rates. For example, unhealthy individuals who have high likelihood of re-admissions might self-select themselves into the program and hence, its features might have little causal impact on their actions or behaviors and outcomes.

In addition, super-utilizers of health care or super-spenders who do not participate in the program might be fundamentally different on unobserved characteristics from those who actually participated. This process of program participation must be accounted for, if not, the observed association between program participation and 180-day readmission rates likely reflect the effect of unmeasured individual or family characteristics that motivated program participation.

It is worth mentioning here that since participation is voluntary, we may not be able to observe the potential outcome of individuals who do not participate in the program. Hence there will be sample selection.

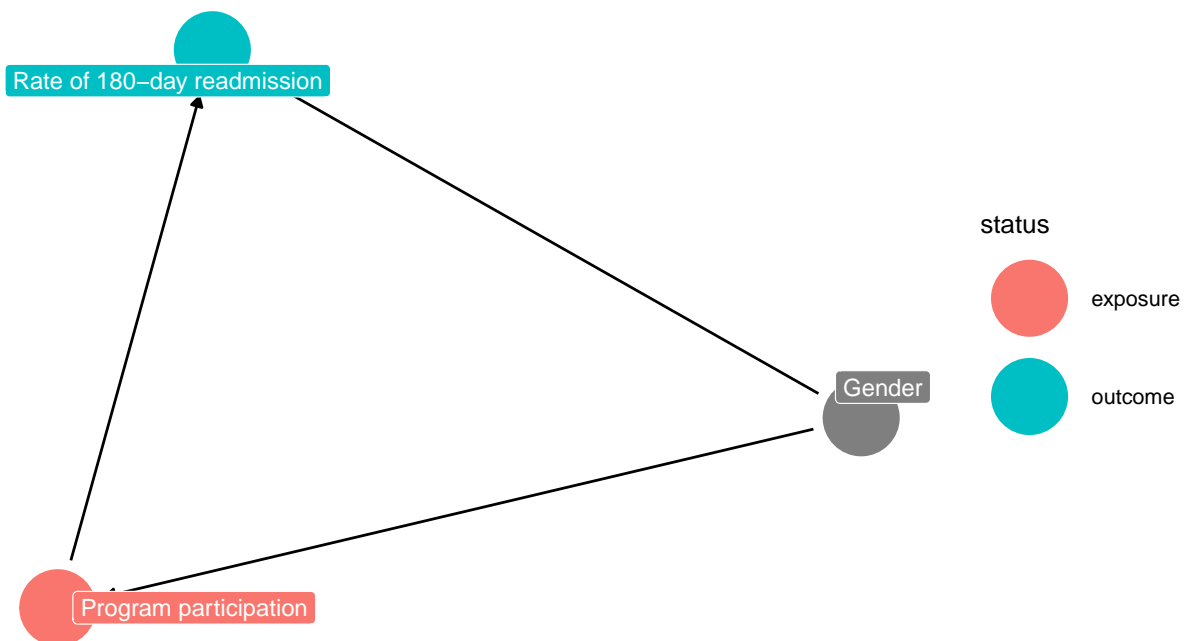
In conclusion, voluntary participation biases the estimates and makes them inconsistent. The ‘selection effects’ must be separated from the ‘program effects’.

```

the_dag <- dagify( # Create super basic DAG
  readmit ~ male,
  rand_treated ~ male,
  readmit ~ rand_treated,
  exposure = "rand_treated",
  outcome = "readmit",
  labels = c(readmit = "Rate of 180-day readmission",
             rand_treated = "Program participation",
             male="Gender"))

set.seed(26445111) #prevents DAG shape from changing
ggdag_status(the_dag, use_labels= "label",
             text = FALSE) + theme_dag()

```



#Question B

Using the potential outcome framework, let Z (i.e., the instrumental variable) represent whether an individual i was initially randomized to take up the program ($Z=1$) or not ($Z=0$). Let D denote the treatment- whether an individual i actually participated or took up the program ($D=1$) or not ($D=0$). D is a potentially endogenous variable in the model. Let Y denote the outcome- the rate of 180-day hospital readmission of individual i . Let X denote control variables or covariates.

Let $Y_{\{i\}}(D_{\{i\}}=1)$ denote the potential outcome that would be observed for individual i if he/she had actually participated in the program. However, we would not be able to observe $Y_{\{i\}}(D_{\{i\}}=1)$ for individual i if he/she did not actually participate in the program. Thus, $Y_{\{i\}}(D_{\{i\}}=1)$ would denote unobserved, counterfactual outcome if he/she had not participated (control group). The treatment effect for individual i is the difference between his/her potential outcomes under treatment and control: $Y_{\{i\}}(D_{\{i\}}=1) - Y_{\{i\}}(D_{\{i\}}=0)$. Meanwhile, only one of these potential outcomes is observed (Holland, 1986; Felton and Stewart, 2022).

Let $D_{\{i\}}(Z_{\{i\}}=1)$ denote the potential treatment (i.e., actual program take up or not) that would be observed if individual i had been randomly assigned to the program rather than to the control group. $Y_{\{i\}}(D_{\{i\}}=1, Z_{\{i\}}=1)$ represents the potential outcome that would be observed for individual i had he/she had been randomized into the program and had also actually taken up the program.

The identification of the randomization as instrumental variable is analyzed based on six assumptions: Relevance, Exclusion restriction, Exogeneity, unconfoundedness, monotonicity, stable unit-treatment-value assumption (SUTVA) and positivity.

Relevance depicts that being randomized into the program has a causal effect on whether individual i participated in the program or not and such impact is expected in this RCT. Thus: $E[D_{\{i\}}(Z_{\{i\}}=1) - D_{\{i\}}(Z_{\{i\}}=0)]$ is not equal to zero.

Unconfounded (or exogenous) instrument means that the instrument (i.e., randomization) can share no unmeasured common causes with neither the outcome (i.e., rate of 180-day readmission) nor the treatment (i.e., program participation). This assumption is also satisfied in the model as the IV is randomized.

The exclusion restriction requires that the instrumental variable has no effect on the outcome except through the treatment. Here, the randomization instrumental variable affects the rate of 180-day hospital readmission (i.e., outcome) only through the program participation (i.e., treatment).

Monotonicity: Let's identify four plausible "compliance types". Assume people are randomized to the control and treatment arms or groups. Hence, randomization is unconfounded since participants are assigned randomly.

Neuer is a *never taker* if, regardless of the group he is randomly *assigned* to, he is never going to *participate* in the program itself. Whitaker is a *always taker* if, regardless of the group he is randomly *assigned* to, he is always going to *participate* in the program. Collins is a *complier* if he will *participate* in the program if he is assigned to the treatment arm but

he will not participate if he was randomized into the control group. Daphne is a *defier* if she would participate in the program even though she was initially randomized not to join the treatment group but would not participate even if she was initially randomized to join the treatment group. The monotonicity assumption, which is untestable, expects that there are no *defiers* in the sample (Felton and Stewart, 2022). The SUTVA assumption expects no *hidden* versions of the instrument or treatment and strikes out interference across units.

Positivity requires that, in every stratum of measured confounders (i.e., those necessary for unconfoundedness of the instrument to hold) at least some units receive the instrument (Aronow and Miller, 2019).

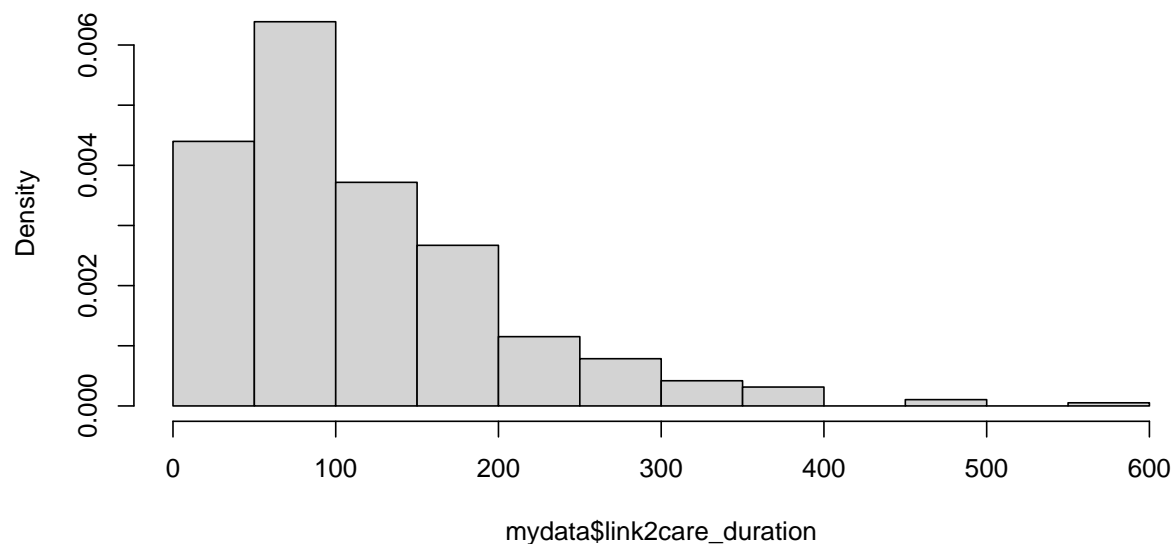
To the best of my knowledge, the randomization instrumental variable meets the testable assumptions.

##Question C

The link2care_duration is left-skewed. There are lesser individuals who were randomized in the control group (n=389), a dummy variable, relative to those who were randomized into the treatment group (n=393). Those who were randomized and treated (n=194), a dummy variable, were less relative to their counterparts (n=577). Those who were randomized but not treated (n=188), a dummy variable, were lesser relative to their counterparts (n=583).

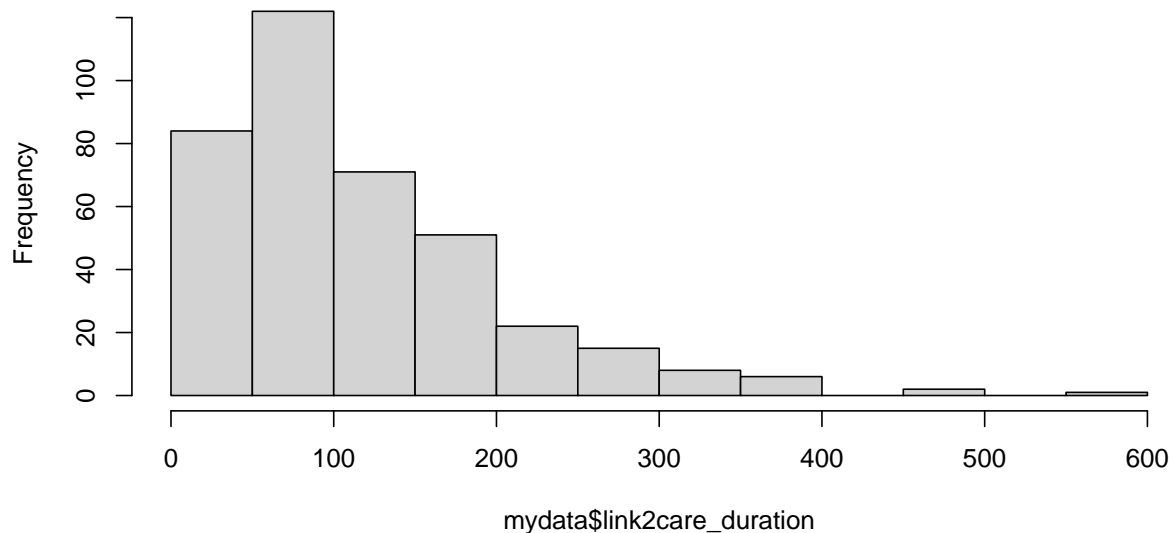
```
#mydata <- mydata %>% mutate(coverage = ifelse(q0411<4, 1, 0))  
#summary(mydata$treated)  
#table(mydata$treated)  
  
#table(mydata$link2care_duration)  
hist(mydata$link2care_duration, freq=F) #Density
```

Histogram of mydata\$link2care_duration



```
hist(mydata$link2care_duration, freq=T) #Frequency
```


Histogram of mydata\$link2care_duration



```
#summary of control groups
summary(mydata$Icontrol)
  Min. 1st Qu.  Median    Mean 3rd Qu.    Max.
  0.0000  0.0000  0.0000  0.4974  1.0000  1.0000
table(mydata$Icontrol, exclude = NA)

  0    1
393 389
describe(mydata$Icontrol)
  vars   n mean  sd median trimmed mad min max range skew kurtosis   se
X1    1 782  0.5 0.5      0      0.5  0  0  1    1 0.01      -2 0.02
str(mydata$Icontrol)
int [1:782] 1 0 0 1 1 1 1 1 0 1 ...

#interact Itreatment with treated variable
summary(mydata$Itreatment)
  Min. 1st Qu.  Median    Mean 3rd Qu.    Max.
  0.0000  0.0000  1.0000  0.5026  1.0000  1.0000
#table(mydata$Itreatment)

#create randomization
#table(mydata$random)

#summary of randomized and treated
summary(mydata$rand_treated)
```

```

      Min. 1st Qu.  Median    Mean 3rd Qu.    Max.   NA's
0.0000 0.0000 0.0000 0.2516 1.0000 1.0000    11
table(mydata$rand_treated, exclude = NA)

  0   1
577 194
describe(mydata$rand_treated)
  vars   n mean   sd median trimmed mad min max range skew kurtosis   se
X1    1 771 0.25 0.43      0   0.19  0  0  1    1 1.14    -0.7 0.02
str(mydata$rand_treated)
num [1:782] 0 0 1 0 0 0 0 0 1 0 ...

#summary of randomized but not treated
summary(mydata$rand_untreated)
      Min. 1st Qu.  Median    Mean 3rd Qu.    Max.   NA's
0.0000 0.0000 0.0000 0.2438 0.0000 1.0000    11
table(mydata$rand_untreated, exclude = NA)

  0   1
583 188
describe(mydata$rand_untreated)
  vars   n mean   sd median trimmed mad min max range skew kurtosis   se
X1    1 771 0.24 0.43      0   0.18  0  0  1    1 1.19    -0.58 0.02
str(mydata$rand_untreated)
num [1:782] 0 1 0 0 0 0 0 0 0 0 ...

#confirmation with cross tabulation
#xtabs(~random+treated, data=mydata)

#desc_table

desc_table = data.frame(
  Measure = c("Control", "Randomized and Treated",
              "Randomized but not Treated"),
  M_1     = c(782, 771, 771),
  M_2     = c(389, 194, 188))

kable(
  desc_table,
  col.names = c("Measure", "*Observation*", "*Number of Values*"),
  digits = 2,
  caption = "Summary of Variables"

```

Table 1: Summary of Variables

Measure	*Observation*	*Number of Values*
Control	782	389
Randomized and Treated	771	194
Randomized but not Treated	771	188

)

##QUESTION D

The coefficient (in the Logistic regression) means that there is a positive association between randomization and ‘actual’ take up or participation of the program. The F-statistic is greater than 104.7 hence the instrument is strong. This regression highlights the ‘Relevance’ assumption. Thus, the instrumental variable is expected to have significant effect on the treatment variable.

First Stage-Logit	
(Intercept)	−19.566*** (2×10^{-8})
random	19.597*** (0.108)
Num.Obs.	771
AIC	533.5
BIC	542.8
Log.Lik.	−264.735
F	33 005.295
RMSE	0.35
Std.Errors	HC3
* p < 0.1, ** p < 0.05, *** p < 0.01	

```
table(mydata$treated)

  0   1
188 194

# First stage regression of IV: take up on randomization

m1 <- glm(rand_treated ~ random,data=mydata,
          family='binomial'(link='logit'))

msummary(list("First Stage-Logit"=m1),
          vcov=c("robust"),
          tab_header=c("First Stage"),
          stars=c('*' = .1, '**' = .05, '***' = .01))
```

##QUESTION E

There is not much difference between both the naive and the 2SLS models. Contrary to what was expected, the F statistics and *R-squared* for the naive model were higher than for the 2SLS model. Also, the estimates of the treatment variables is not significant for the 2SLS model but it is significant for the naive model (at 10 percent significance level). This shows that failure to account for potential endogeneity can lead to misleading results.

```
#first stage #logit #binary treatment
#random is the IV
#run endogenous variable on the IV and controls
#run that probit

m1r <- glm(rand_treated ~ random+african_american+hispanic+white+male,
            data=mydata,
            family='binomial'(link='probit'))

mydata$pred_x_X <- predict(m1r, mydata)

#Forbidden regresion #sticking predicted values into the 2nd stage
forbid <- lm(post_ie_charges_180_IP ~ pred_x_X+african_american+hispanic+white+
             male,data=mydata)

##The 2SLS #predicted values in place of instrument
m1_second <- lm(rand_treated ~ pred_x_X+african_american+hispanic+white+male,
                data=mydata)

mydata$pred_pred_x <- predict(m1_second, mydata)

#2 nd stage
# Regress outcome on pred_X
m3 <- lm(post_ie_charges_180_IP ~ pred_pred_x+african_american+hispanic+white+
         male,data=mydata)

#naive
m2 <- lm(post_ie_charges_180_IP ~ rand_treated+african_american+hispanic+white+
         male,data=mydata) #Linear model
msummary(list("Naive"=m2),
          vcov=c("robust"),
```

	Naive
(Intercept)	73 294.700 (70 357.841)
rand_treated	32 476.350* (18 900.733)
african_american	28 962.300 (71 138.197)
hispanic	41 090.264 (71 583.065)
white	25 445.903 (71 621.763)
male	5296.179 (13 962.350)
Num.Obs.	771
R2	0.006
R2 Adj.	−0.0003
AIC	20 974.2
BIC	21 006.7
Log.Lik.	−10 480.092
F	0.837
RMSE	193 671.31
Std.Errors	HC3
* p < 0.1, ** p < 0.05, *** p < 0.01	

```
stars=c('*' = .1, '**' = .05, '***' = .01))
```

```
#Combination
msummary(list("Naive"=m2,"Forbidden"=forbid,"2SLS"=m3),
          vcov=c("robust","robust", "robust"),
          stars=c('*' = .1, '**' = .05, '***' = .01))
```

	Naive	Forbidden	2SLS
(Intercept)	73 294.700 (70 357.841)	89 867.209 (74 146.775)	87 665.330 (74 913.654)
rand_treated	32 476.350* (18 900.733)		
african_american	28 962.300 (71 138.197)	21 619.251 (74 938.291)	21 893.208 (75 039.319)
hispanic	41 090.264 (71 583.065)	30 748.657 (75 373.984)	31 160.332 (75 466.633)
white	25 445.903 (71 621.763)	13 593.149 (75 437.049)	13 958.747 (75 545.228)
male	5296.179 (13 962.350)	7395.142 (13 870.551)	7372.826 (13 853.843)
pred_x_X		314.619 (2284.640)	
pred_pred_x			3735.089 (27 122.785)
Num.Obs.	771	782	782
R2	0.006	0.001	0.001
R2 Adj.	-0.0003	-0.005	-0.005
AIC	20 974.2	21 272.3	21 272.3
BIC	21 006.7	21 305.0	21 305.0
Log.Lik.	-10 480.092	-10 629.161	-10 629.161
F	0.837	0.256	0.256
RMSE	193 671.31	193 559.31	193 559.31
Std.Errors	HC3	HC3	HC3

* $p < 0.1$, ** $p < 0.05$, *** $p < 0.01$

#QUESTION F

An instrumental variable helps to recover the Local Average Treatment Effects (LATE). The LATE, also referred to as the complier average causal effect (CACE), denotes the treatment effect for the subset of the sample that participated in the program when they were initially randomized to do so (i.e., the compliers). This helps to fulfil the monotonicity assumption of eliminating *defiers*.

Meanwhile, the LATE is only policy or economically relevant if it has been proved in the literature that many individuals comply to such programs. There is not enough information to conclude on this so I would say that the LATE is not economically relevant.

#QUESTION G

The estimate for the treatment variable in the ‘Naive-OLS’ is significant (0.087) even though it is not significant in the 2SLS model. Their estimates show a positive association between program participation and the rate of 180-day hospital readmission. However, though insignificant, the estimates of the Bivariate regression shows a negative association between program participation and the rate of 180-day hospital readmission.

```

library(GJRM)
Loading required package: mgcv
Loading required package: nlme

Attaching package: 'nlme'
The following object is masked from 'package:lme4':

    lmList
The following object is masked from 'package:dplyr':

    collapse
This is mgcv 1.8-41. For overview type 'help("mgcv-package")'.

This is GJRM 0.2-6.
For overview type 'help("GJRM-package")'.
table(mydata$readmit)

  0    1
498 284

#male and race are the restricted variables
out2<-gjrm(list(rand_treated ~ random+african_american+hispanic+white,
               readmit ~ rand_treated+random+male), #rand_treated
           data = mydata,
           margins = c("probit", "probit"),
           Model = "B")
conv.check(out2)

Largest absolute gradient value: 1.115763e-07
Observed information matrix is positive definite
Eigenvalue range: [1.348283e-07,908.8774]

Trust region iterations: 10
Estimated overall probability range: 1.997374e-13 0.9880989
Estimated overall density range: 1.804796e-11 1.088973
summary(out2)

COPULA: Gaussian
MARGIN 1: Bernoulli
MARGIN 2: Bernoulli

EQUATION 1
Link function for mu.1: probit
Formula: rand_treated ~ random + african_american + hispanic + white

```

Parametric coefficients:

	Estimate	Std. Error	z value	Pr(> z)
(Intercept)	-6.2446	1925.7260	-0.003	0.997
random	6.7048	1925.7259	0.003	0.997
african_american	-0.3158	0.7537	-0.419	0.675
hispanic	-0.6574	0.7578	-0.868	0.386
white	-0.5430	0.7672	-0.708	0.479

EQUATION 2

Link function for mu.2: probit

Formula: readmit ~ rand_treated + random + male

Parametric coefficients:

	Estimate	Std. Error	z value	Pr(> z)
(Intercept)	-0.38223	0.07804	-4.898	9.68e-07 ***
rand_treated	-0.24996	1.02893	-0.243	0.808
random	0.16429	0.57838	0.284	0.776
male	0.06390	0.09063	0.705	0.481

Signif. codes: 0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1

n = 771 theta = 0.353(-0.812,0.911) tau = 0.229(-0.606,0.73)

total edf = 10

#AIC(out2); BIC(out2)

Testing the hypothesis of absence of endogeneity post estimation...

#gt.bpm(out2)

treatment effect, risk ratio and odds ratio with CIs and random effects

mb(mydata\$rand_treated, mydata\$Ireadmit2_180_100, Model = "B")

Worst-Case Manski's bounds for ATE (%):

Lower Bound: -40.2

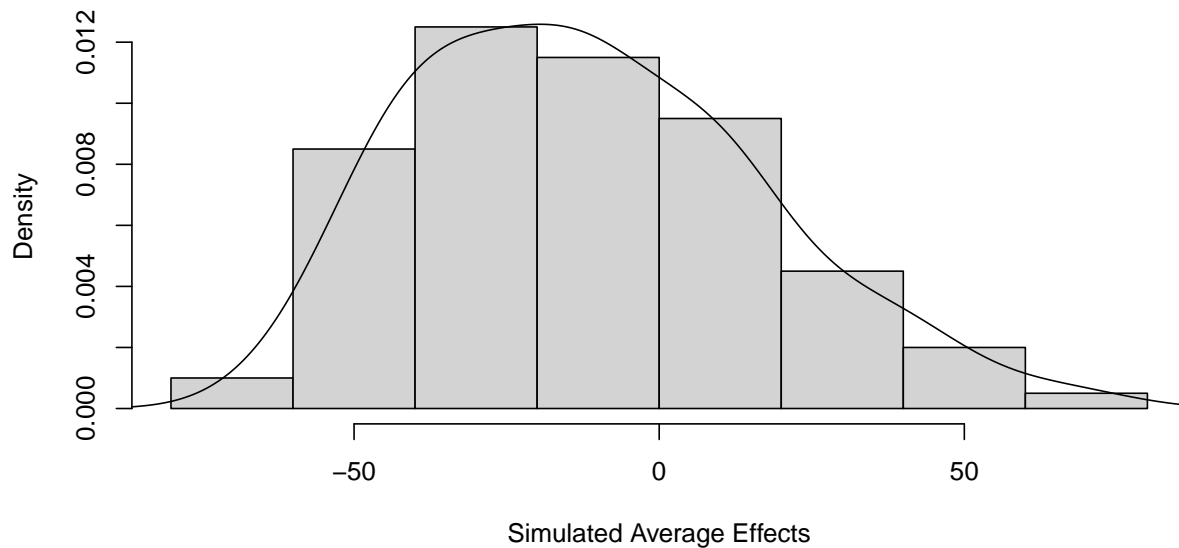
Upper Bound: 59.8

Imbens&Manski's CI for ATE (%): [-40.3,59.9]

ATE assuming random assignment (%): 8.64

AT(out2, nm.end = "rand_treated", hd.plot = TRUE)

Histogram and Kernel Density of Simulated Average Effects



Treatment effect (%) with 95% interval:

-9.18 (-53.97,46.25)

```
RR(out2, nm.end = "rand_treated")
```

Risk ratio with 95% interval:

0.767 (0.109,3.556)

```
OR(out2, nm.end = "rand_treated")
```

Odds ratio with 95% interval:

0.6664 (0.0354,13.3539)

```
#AT(out2, nm.end = "rand_treated", type = "univariate")
```

```
#re.imp <- imputeCounter(out2, m = 10, "rand_treated") #Random effects
```

```
#random effects
```

```
#re.imp$AT
```

```
#compare with below
```

```
# iii)
```

```
# ols #naive
```

```
m6_ols <- lm(readmit ~ rand_treated+african_american+hispanic+white+male,  
             data=mydata)
```

```

# binary IV regression
m5_first <- glm(rand_treated ~ random+african_american+hispanic+white+male,
                data=mydata, family='binomial'(link='probit'))

#predict X with Z:
mydata$pred_x_naive <- predict(m5_first, mydata)

#replace IV with binnary IV prediction #first stage
m5_first_naive <- lm(rand_treated ~ pred_x_naive+african_american+hispanic+white
                    +male,data=mydata)

#predict X with Z:
mydata$the_pred_x_naive <- predict(m5_first_naive, mydata)

# Regress outcome on pred_X
m6_second_naive <- lm(readmit ~ the_pred_x_naive+african_american+hispanic
                    +white+male,data=mydata)

msummary(list("Naive-OLS"=m6_ols,"Naive-2SLS"=m6_second_naive),
          vcov=c("robust","robust"),
          stars=c('*' = .1, '**' = .05, '***' = .01))

```

	Naive-OLS	Naive-2SLS
(Intercept)	0.206 (0.273)	0.249 (0.290)
rand_treated	0.087** (0.041)	
african_american	0.120 (0.275)	0.093 (0.290)
hispanic	0.120 (0.275)	0.092 (0.291)
white	0.181 (0.277)	0.146 (0.293)
male	0.023 (0.035)	0.027 (0.035)
the_pred_x_naive		0.002 (0.069)
Num.Obs.	771	782
R2	0.009	0.003
R2 Adj.	0.003	−0.004
AIC	1070.8	1086.3
BIC	1103.4	1118.9
Log.Lik.	−528.413	−536.154
F	1.343	0.369
RMSE	0.48	0.48
Std.Errors	HC3	HC3

* $p < 0.1$, ** $p < 0.05$, *** $p < 0.01$

#QUESTION H

The results suggest that there is a negative association (insignificant) between take up of the program and the rate of 180-day readmission (for the Bivariate regression model). Hence, it can be deduced that the program is not effective in reducing the rate of 180-day readmission.

In addition, the 2SLS also showed that there is an insignificant association between program participation and superutilization spending. Hence, it can be inferred that the program is not effective in reducing superutilization spending.


```
packages <- knitr::write_bib(file = 'packages.bib')
packages
```

\$AER @Manual{R-AER, title = {AER: Applied Econometrics with R}, author = {Christian Kleiber and Achim Zeileis}, year = {2022}, note = {R package version 1.2-10}, url = {https://CRAN.R-project.org/package=AER}, }

\$base @Manual{R-base, title = {R: A Language and Environment for Statistical Computing}, author = {{R Core Team}}, organization = {R Foundation for Statistical Computing}, address = {Vienna, Austria}, year = {2022}, url = {https://www.R-project.org/}, }

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