

**Problem Statement 1:**

Is gender independent of education level? A random sample of 395 people were surveyed and each person was asked to report the highest education level they obtained. The data that resulted from the survey is summarized in the following table:

High School Bachelors Masters Ph.d. Total

Female 60 54 46 41 201

Male 40 44 53 57 194

Total 100 98 99 98 395

Question: Are gender and education level dependent at 5% level of significance? In other words, given the data collected above, is there a relationship between the gender of an individual and the level of education that they have obtained?

Problem 1	High School	Bachelors	Masters	Ph.d.	Total
Female	50.886	49.868	50.377	49.868	201
Male	49.114	48.132	48.623	48.132	192
Total	100	98	99	98	395

$$\chi^2 = \frac{(60 - 50.886)^2}{50.886} + \dots + \frac{(57 - 48.132)^2}{48.132}$$

$$= 8.006$$

df = 3  
tabular  $\chi^2 = 7.815$   
Since,  $8.006 > 7.815$   
⇒ We Reject the  $H_0$   
∴ Education level depends on gender at 5% level of significance.

**Problem Statement 2:**

Using the following data, perform a oneway analysis of variance using  $\alpha = .05$ . Write up the results in APA format.

[Group1: 51, 45, 33, 45, 67]

[Group2: 23, 43, 23, 43, 45]

[Group3: 56, 76, 74, 87, 56]

## Problem 2

Group 1

$$\bar{x} = 48.2, 35.4, 69.8$$

51	48.2	2.8	7.84
45	48.2	-3.2	10.24
33	48.2	-15.2	231.04
45	48.2	-3.2	10.24
67	48.2	18.8	353.44
mean		deviation	Std. dev.

Group 2

	mean	dev.	std dev
23	35.4	-12.4	153.76
43	35.4	7.6	57.76
23	35.4	-12.4	153.76
43	35.4	7.6	57.76
45	35.4	9.6	92.16

Group 3

	mean	dev	std dev
56	69.8	-13.8	190.44
76	69.8	6.2	38.44
74	69.8	4.2	17.64
87	69.8	17.2	295.84
56	69.8	-13.8	190.44

$$MSS = 612.8, 515.2, 732.8$$

$$Var = 153.2, 128.8, 183.2$$

$$MS_{\text{error}} = \frac{153.2 + 128.8 + 183.2}{3} = 155.07$$

$$df_{\text{error}} = 15 - 3 = 12$$

$$SS_{\text{error}} = (155.07) \times 12 = 1860.8$$

$$\text{Grand mean} = \frac{48.2 + 35.4 + 69.8}{3} = 51.13$$

$$\text{dev} = -2.93, -15.73, 18.67$$

$$sq. \text{ dev} = 8.58, 247.13, 348.57$$

$$SS_{\text{mean}} = 604.58$$

$$\begin{aligned}
 \text{Var means} &= 302.29 \\
 \text{MS between} &= (302.29) \times 5 \\
 &= 1511.45 \\
 \text{df group} &= 2, \text{ SS group} = 1511.45 \times 2 \\
 &= 3022.9 \\
 F &= \frac{1511.45}{155.07} = 9.75 \\
 F_{\text{critical}}(2, 12) &= 3.89 \\
 \Rightarrow 9.77 > 3.89 \\
 \text{Thys, Reject } H_0
 \end{aligned}$$

### Problem Statement 3:

Calculate F Test for given 10, 20, 30, 40, 50 and 5, 10, 15, 20, 25.

For 10, 20, 30, 40, 50:

Set 1	Set 2
$N = 10, 20, 30, 40, 50$ $n = 5$ $\bar{x} = 30$ $SD = 15.8114$ $\text{Var} = 250$	$N = 5, 10, 15, 20, 25$ $n = 5$ $\bar{x} = 15$ $SD = 7.9057$ $\text{Var} = 62.5$

$$\begin{aligned}
 \text{F-Test} &= 250 / 62.5 \\
 &= \boxed{4}
 \end{aligned}$$