

Aptitude Assignment 2

What quantity of water should be added to the milk water mixture so that the milk water ratio changes from 2:3 to 4:11. The quantity of milk in the mixture is 40 litres?

Solution:

Given, the ratio of milk and water = 2: 3

And we have total 40 litres of milk

Let x be the litres added to the mixture.

Step 1:

Quantity of Milk in mixture of 40 litres = $\frac{2}{5} \times 40 = 32$ litres

So, the quantity of water in mixture of 40 liters = $40 - 32 = 8$ litres.

Now, let x litres of water be added to the mixture ,

And the ration of milk and water after adding water is 4:11

$$\Rightarrow 4/11 = 32/8+x$$

$$\Rightarrow .4(8+x) = 11*32$$

$$32+4x=352$$

$$4x=352-32$$

$$4x=320$$

$$X=80$$

80 liters of water should be added.

Qus2

Linear equation $2x+3y=0$ meets the x & y-axis at the point?

$$2x+3y=0$$

x	y
-3	2
3	-2

0	0
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Que3

a & b are positive integers such that $a^2 - b^2 = 19$. Find a & b?

$$a^2 - b^2 = 19$$

$$a > 0$$

$$b > 0$$

factors are 1 & 19 only as 19 is a prime number

$$(a+b)(a-b) = 19$$

$$a+b > 0$$

$$a-b > 0$$

hence factors are 10 & 9 as this value gives us the positive addition and positive subtraction.

$$A = 10 \text{ \& } b = 9$$

Que3

Find $a^3 + b^3 + c^3 + 3abc$, where $a+b+c=5$ & , $a^2 + b^2 + c^2 = 10$?

$$(a+b+c)^2 = a^2 + b^2 + c^2 + 2(ab+bc+ac) \Rightarrow ab+bc+ca$$

$$25 - 10 = 15$$

$$a^3 + b^3 + c^3 = (a+b+c)[a^2 + b^2 + c^2 + ab+bc+ca]$$

$$= 5[10+15]$$

$$5 \times 25 = 125$$

$$\mathbf{a^3 + b^3 + c^3 = 125}$$

5. Sum of two, two-digit numbers is a perfect square. The digits of the first two-digit number are two consecutive positive integers; also, when the digits of the first number are reversed, the second number is formed. Find these numbers & the square root of their sum.

Solution

The greatest possible sum of two digits is $9+9=18$. As such, we only need to consider perfect squares less than or equal to 18, of which there are four:

$$1^2=1$$

$$2^2=4$$

$$3^2=9$$

$$4^2=16$$

We can now list the ways of writing each square as a sum of two single digit numbers.

$$1=1+0$$

$$4=4+0=3+1=2+2$$

$$9=9+0=8+1=7+2=6+3=5+4$$

$$16=9+7=8+8$$

It is now a simple matter to see what two digit numbers can be formed from those combinations.

1: 10

4: 40,31,13,22

9: 90,81,18,72,27,63,36,54,45

16: 97,79,88