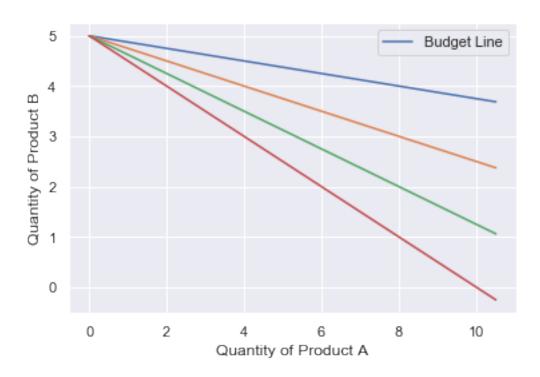
Assignment 3

December 8, 2018

```
In [11]: import pandas as pd
         import numpy as np
         import matplotlib.pyplot as plt
         import seaborn as sns
         sns.set()
In [14]: Income = 200
         Pas = [5, 10, 15, 20]
         Pb = 40
         Qa = np.arange(0,11,0.5)
         Qb = [((Income)/(Pb)) - ((Pa*Qa)/(Pb)) \text{ for Pa in Pas}]
         df = pd.DataFrame(list(zip(Qa,Qb[0],Qb[1],Qb[2],Qb[3])),
                            columns=['Quantity of Product A'] +
                                     ['Quantity of Product B at Price A = {}'.format(Pa) for Pa
         print(df)
                            Quantity of Product B at Price A = 5 \
    Quantity of Product A
0
                                                            5.0000
                                                            4.9375
1
                       0.5
2
                       1.0
                                                            4.8750
3
                                                            4.8125
                       1.5
4
                       2.0
                                                            4.7500
5
                       2.5
                                                            4.6875
6
                       3.0
                                                            4.6250
7
                       3.5
                                                            4.5625
8
                       4.0
                                                            4.5000
9
                       4.5
                                                            4.4375
10
                       5.0
                                                            4.3750
                       5.5
                                                            4.3125
11
12
                       6.0
                                                            4.2500
13
                       6.5
                                                            4.1875
                       7.0
                                                            4.1250
14
                       7.5
                                                            4.0625
15
                       8.0
16
                                                            4.0000
17
                       8.5
                                                            3.9375
18
                       9.0
                                                            3.8750
19
                       9.5
                                                            3.8125
```

```
20
                      10.0
                                                             3.7500
21
                      10.5
                                                             3.6875
    Quantity of Product B at Price A = 10 \
0
                                      5.000
1
                                      4.875
2
                                      4.750
3
                                      4.625
4
                                      4.500
5
                                      4.375
6
                                      4.250
7
                                      4.125
8
                                      4.000
9
                                      3.875
10
                                      3.750
11
                                      3.625
12
                                      3.500
13
                                      3.375
14
                                      3.250
15
                                      3.125
16
                                      3.000
17
                                      2.875
18
                                      2.750
19
                                      2.625
20
                                      2.500
21
                                      2.375
    Quantity of Product B at Price A = 15 \
0
                                     5.0000
                                     4.8125
1
2
                                     4.6250
3
                                     4.4375
4
                                     4.2500
5
                                     4.0625
6
                                     3.8750
7
                                     3.6875
8
                                     3.5000
9
                                     3.3125
10
                                     3.1250
11
                                     2.9375
12
                                     2.7500
13
                                     2.5625
14
                                     2.3750
                                     2.1875
15
16
                                     2.0000
17
                                     1.8125
18
                                     1.6250
                                     1.4375
19
```

```
20
                                     1.2500
21
                                     1.0625
    Quantity of Product B at Price A = 20
                                       5.00
0
1
                                       4.75
2
                                       4.50
                                       4.25
3
                                       4.00
4
                                       3.75
5
6
                                       3.50
7
                                       3.25
8
                                       3.00
9
                                       2.75
10
                                       2.50
11
                                       2.25
12
                                       2.00
13
                                       1.75
14
                                       1.50
                                       1.25
15
                                       1.00
16
                                       0.75
17
                                       0.50
18
19
                                       0.25
                                       0.00
20
21
                                      -0.25
```



```
In [15]: x = np.arange(1, 10.1, 0.1)
         indifference_curve = lambda x: 25/(2*x)
         for Pa in Pas:
             df['Indifference Curve at Pa = {}'.format(Pa)] = indifference_curve(df['Quantity
         print(df)
    Quantity of Product A Quantity of Product B at Price A = 5 \
0
                       0.0
                                                           5.0000
1
                       0.5
                                                           4.9375
2
                       1.0
                                                           4.8750
3
                       1.5
                                                           4.8125
4
                       2.0
                                                           4.7500
5
                       2.5
                                                           4.6875
6
                       3.0
                                                           4.6250
7
                       3.5
                                                           4.5625
8
                       4.0
                                                           4.5000
9
                       4.5
                                                           4.4375
                       5.0
                                                           4.3750
10
                       5.5
                                                           4.3125
11
                       6.0
12
                                                           4.2500
                       6.5
                                                           4.1875
13
14
                       7.0
                                                           4.1250
15
                       7.5
                                                           4.0625
16
                       8.0
                                                           4.0000
```

```
17
                       8.5
                                                             3.9375
18
                       9.0
                                                             3.8750
                       9.5
19
                                                             3.8125
20
                      10.0
                                                             3.7500
21
                      10.5
                                                             3.6875
    Quantity of Product B at Price A = 10 \
0
                                      5.000
1
                                      4.875
2
                                      4.750
3
                                      4.625
4
                                      4.500
5
                                      4.375
6
                                      4.250
7
                                      4.125
                                      4.000
8
9
                                      3.875
10
                                      3.750
11
                                      3.625
12
                                      3.500
13
                                      3.375
14
                                      3.250
15
                                      3.125
16
                                      3.000
17
                                      2.875
18
                                      2.750
19
                                      2.625
20
                                      2.500
21
                                      2.375
    Quantity of Product B at Price A = 15
0
                                     5.0000
                                     4.8125
1
2
                                     4.6250
3
                                     4.4375
4
                                     4.2500
5
                                     4.0625
6
                                     3.8750
7
                                     3.6875
8
                                     3.5000
9
                                     3.3125
10
                                     3.1250
11
                                     2.9375
12
                                     2.7500
13
                                     2.5625
14
                                     2.3750
15
                                     2.1875
                                     2.0000
16
```

```
17
                                      1.8125
18
                                      1.6250
19
                                      1.4375
20
                                      1.2500
21
                                      1.0625
                                              Indifference Curve at Pa = 5 \
    Quantity of Product B at Price A = 20
0
                                        5.00
                                                                    2.500000
1
                                        4.75
                                                                    2.531646
                                                                    2.564103
2
                                        4.50
3
                                        4.25
                                                                    2.597403
4
                                        4.00
                                                                    2.631579
5
                                        3.75
                                                                    2.666667
6
                                        3.50
                                                                    2.702703
7
                                        3.25
                                                                    2.739726
8
                                        3.00
                                                                    2.777778
9
                                        2.75
                                                                    2.816901
                                        2.50
10
                                                                    2.857143
11
                                        2.25
                                                                    2.898551
12
                                        2.00
                                                                    2.941176
                                                                    2.985075
13
                                        1.75
                                        1.50
                                                                    3.030303
14
15
                                        1.25
                                                                    3.076923
16
                                        1.00
                                                                    3.125000
17
                                        0.75
                                                                    3.174603
                                        0.50
                                                                    3.225806
18
19
                                        0.25
                                                                    3.278689
20
                                        0.00
                                                                    3.333333
21
                                       -0.25
                                                                    3.389831
    Indifference Curve at Pa = 10   Indifference Curve at Pa = 15
0
                           2.500000
                                                            2.500000
1
                           2.564103
                                                            2.597403
2
                           2.631579
                                                            2.702703
3
                           2.702703
                                                            2.816901
4
                           2.777778
                                                            2.941176
5
                           2.857143
                                                            3.076923
6
                           2.941176
                                                            3.225806
7
                           3.030303
                                                            3.389831
8
                           3.125000
                                                            3.571429
9
                           3.225806
                                                            3.773585
10
                           3.333333
                                                            4.000000
11
                           3.448276
                                                            4.255319
12
                                                            4.545455
                           3.571429
13
                           3.703704
                                                            4.878049
14
                           3.846154
                                                            5.263158
15
                           4.000000
                                                            5.714286
16
                           4.166667
                                                            6.250000
```

```
17
                         4.347826
                                                          6.896552
18
                         4.545455
                                                          7.692308
19
                         4.761905
                                                          8.695652
20
                         5.000000
                                                         10.000000
21
                          5.263158
                                                         11.764706
    Indifference Curve at Pa = 20
0
                         2.500000
                         2.631579
1
2
                         2.777778
3
                         2.941176
4
                         3.125000
5
                         3.333333
6
                         3.571429
7
                         3.846154
8
                         4.166667
9
                         4.545455
10
                         5.000000
11
                         5.55556
12
                         6.250000
13
                         7.142857
14
                         8.333333
15
                        10.000000
16
                         12.500000
17
                        16.666667
18
                        25.000000
19
                        50.000000
20
                               inf
21
                        -50.000000
In [39]: fig, ax = plt.subplots(ncols=1, nrows=2, figsize=(10,15))
         for Pa in Pas:
             ax[0].plot(df['Quantity of Product A'], df['Quantity of Product B at Price A = {}
         for i in np.arange(1,2,0.25):
             ax[0].plot(x+i-1, i*indifference_curve(x))
             ax[0].scatter([5+i-1],indifference\_curve(5+i-1)+3*(i-1), marker='x')
         ax[0].set_xlabel('Quantity of Product A')
         ax[0].set_ylabel('Quantity of Product B')
         ax[0].set_ylim(0, 20)
         ax[0].legend(['Indifference Curve', 'Budget Line', 'Equilibrium point (Qa = 5, Qb = 2
         for Pa in Pas:
             ax[1].plot(df['Quantity of Product A'], df['Quantity of Product B at Price A = {}
         ax[1].plot(x, indifference_curve(x))
         ax[1].scatter([5],indifference_curve(5), marker='x')
         ax[1].set_xlabel('Quantity of Product A')
         ax[1].set_ylabel('Quantity of Product B')
```

```
ax[1].legend(['Indifference Curve', 'Budget Line', 'Equilibrium point (Qa = 5, Qb = 2
ax[1].set_ylim(2,3)
ax[1].set_xlim(4,6)
plt.show()
```

