



中国科学技术大学  
University of Science and Technology of China



KDD2024  
BARCELONA, SPAIN

# Kill both Spatial and Temporal shifts

 with one *STONE* 

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# Spatio-temporal OOD prediction problem



## Challenges

- ❖ Temporal shift.
- ❖ Spatial shift.

## Objective

- ❖ Default prediction:

$$\min_{\mathcal{F}} \mathbb{E}_{(\mathbf{x}, \mathbf{y}) \sim P(\mathbf{x}, \mathbf{y} | e)} [\mathcal{L}(\mathcal{F}(\mathbf{x}, \mathcal{G}), \mathbf{y})]$$

- ❖ OOD prediction:

$$\min_{\mathcal{F}} \max_{e^* \in E} \mathbb{E}_{(\mathbf{x}, \mathbf{y}) \sim P(\mathbf{x}, \mathbf{y} | e^*)} [\mathcal{L}(\mathcal{F}(\mathbf{x}, \mathcal{G}), \mathbf{y})]$$

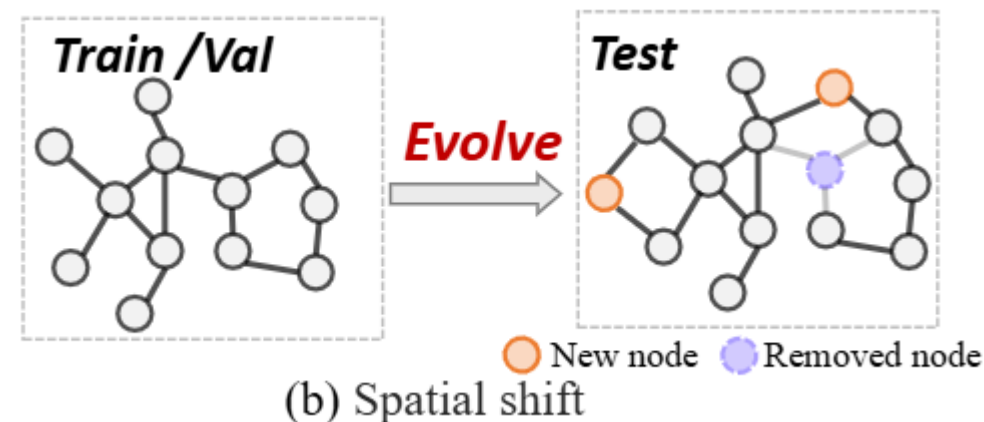
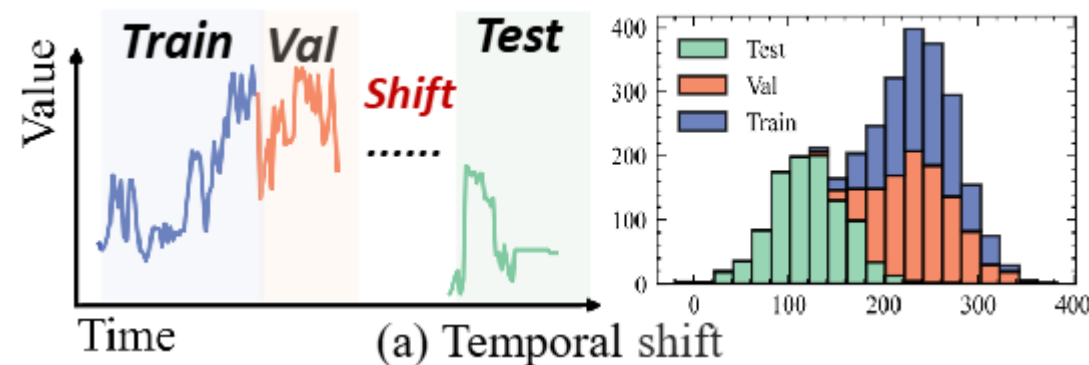


Figure 1. Visualization of temporal (a) and spatial (b) shifts.

# Spatio-temporal environments shifts



## ◇ Portray and perceive

- ❖ Semantic graph: A suitable **metric** is utilized to portray the temporal or spatial similarity between nodes at the current time.

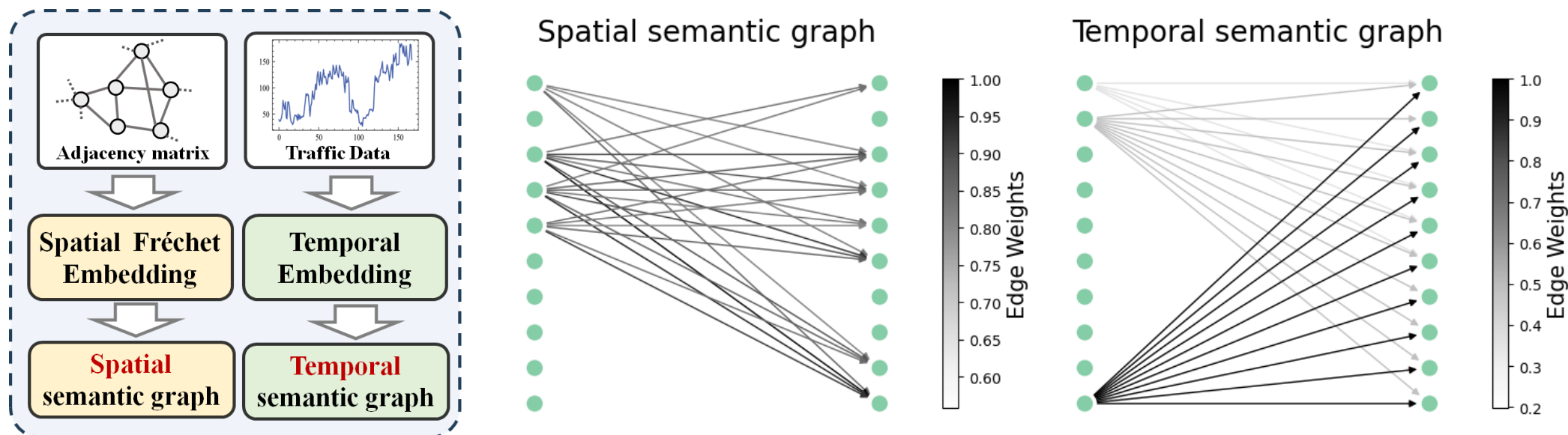


Figure 2. Spatial and Temporal semantic graphs.

# Spatio-temporal environments shifts



## ◇ The case of traffic prediction

- ❖ Node #1 ~ #5 in SD.
- ❖ Similarity of DTW distances based on 12 time steps.

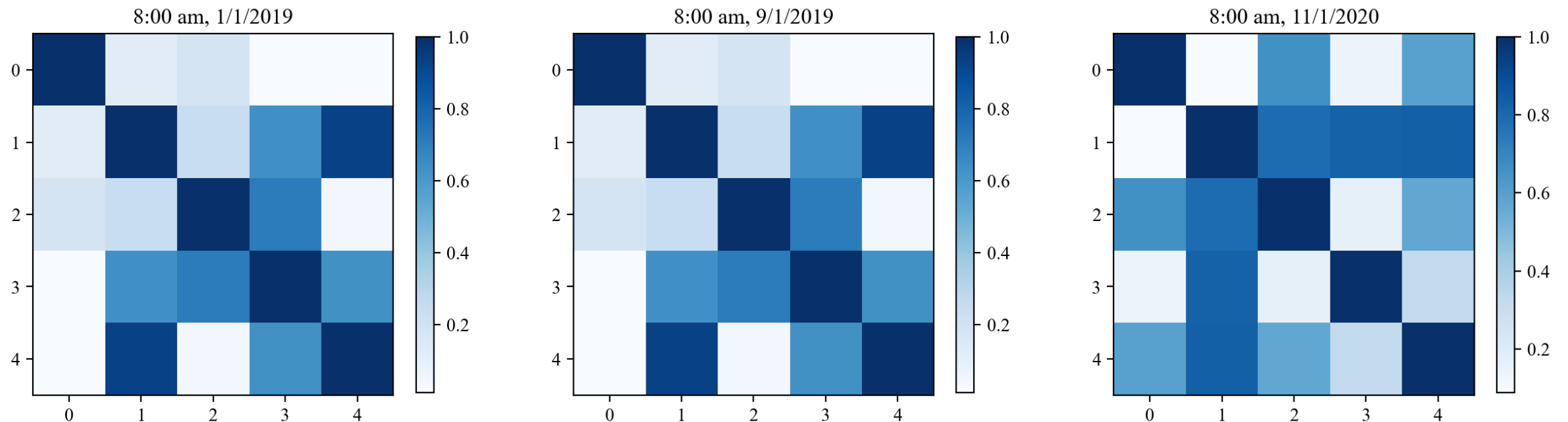


Figure 3. Case study of #1 to #5 sensors in SD datasets.

## ◇ Bourgain's Theorem (1985)

❖ If  $(X, d)$  is an  $N$ -point metric space and  $f$  is an **Fréchet** embedding, then

$$\frac{1}{\mathcal{O}(\log N)} d(x, y) \leq \mathbb{E}_f \|f(x) - f(y)\| \leq d(x, y), \forall x, y \in X.$$

## ◇ Spatial Fréchet Embedding

- ❖ Dimension is not affected by the addition of new nodes.
- ❖ Solid Theory.
- ❖ Based on **Hamming** distance. Low complexity.

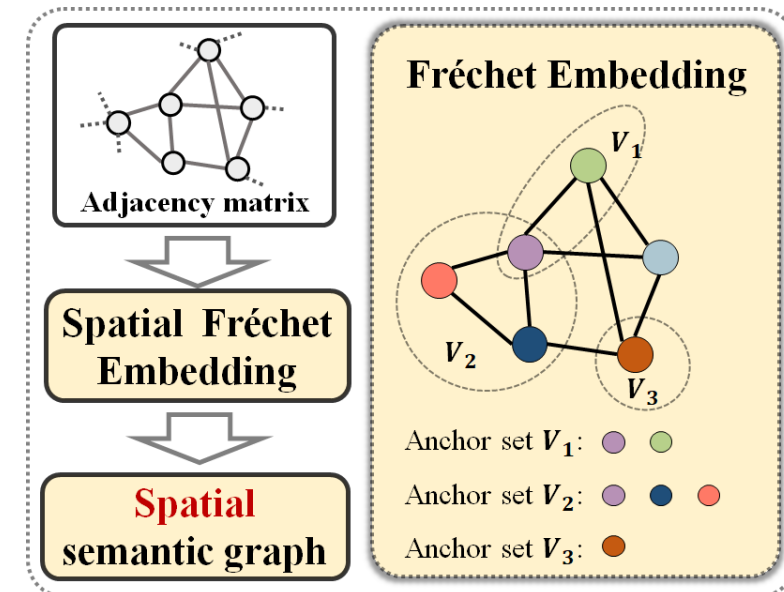


Figure 4. Fréchet Embedding

## ◇ Optimized objects for multiple environments

❖ Mask operators  $\mathbb{M}$  for disturbing spatio-temporal environment in training phase.

$$\begin{aligned} & \min_{\Theta} \text{Var}\{\mathcal{L}_{\Theta}(\mathcal{F}(\mathbf{x}, \mathcal{G}), \mathbf{y} | \mathbb{M}^*, \Theta)\} + \beta \mathbb{E}[\mathcal{L}_{\Theta}(\mathcal{F}(\mathbf{x}, \mathcal{G}), \mathbf{y} | \mathbb{M}^*)], \\ \text{s. t. } & \mathbb{M}^* = (\mathbb{M}_1^*, \mathbb{M}_2^*, \dots, \mathbb{M}_{K_M}^*) = \underset{\mathbb{M}_m \in \{0,1\}^{N \times N}}{\text{argmax}} \text{Var}\{\mathcal{L}_{\Theta}(\mathcal{F}(\mathbf{x}, \mathcal{G}), \mathbf{y} | \mathbb{M}^m, \Theta)\}. \end{aligned}$$

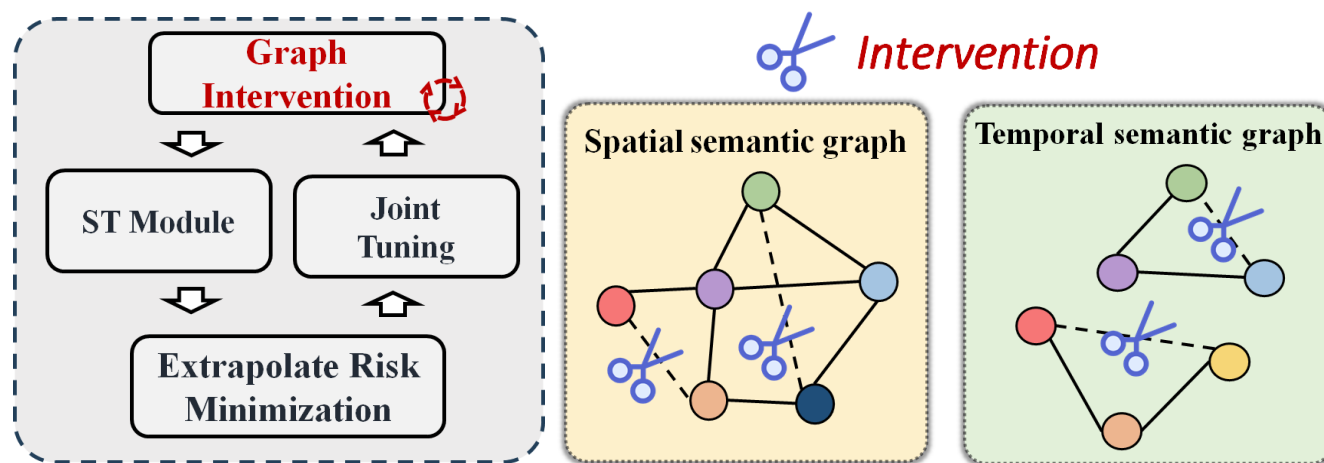


Figure 5. Mask operators and optimization.





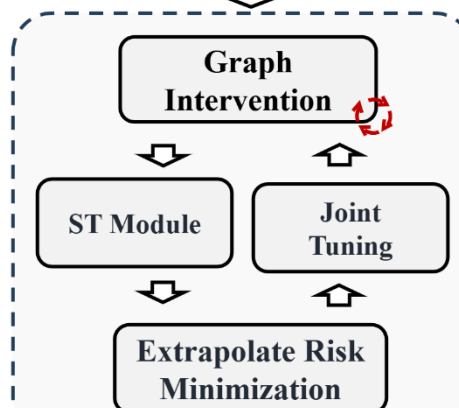
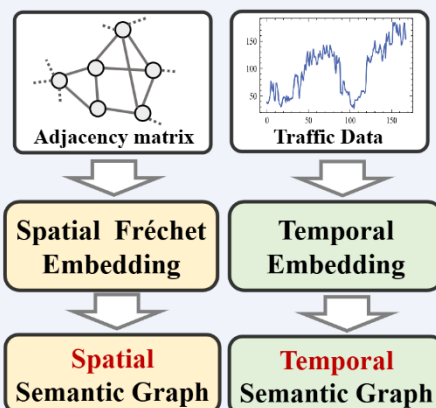
# STONE



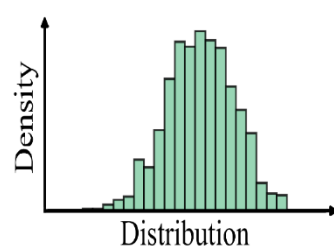
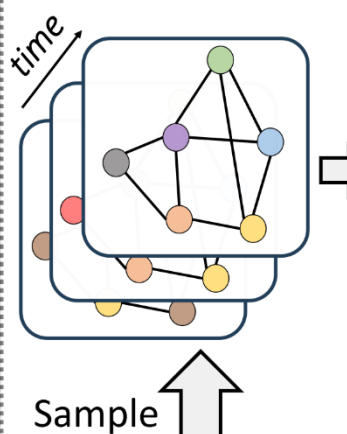
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## ❖ Spatio-Temporal OOD Graph Learning Networks with Fréchet EMBEDDING

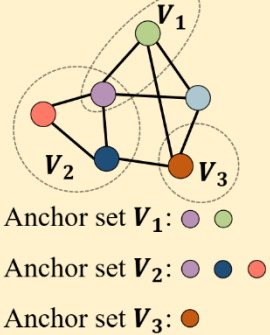
### Overview of STONE



### Training Data



### Fréchet Embedding

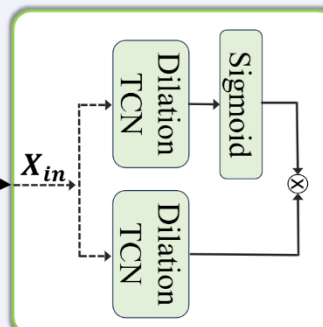
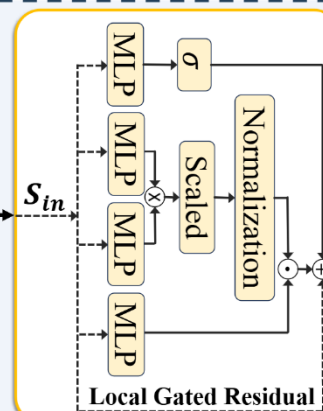


### Temporal Embedding

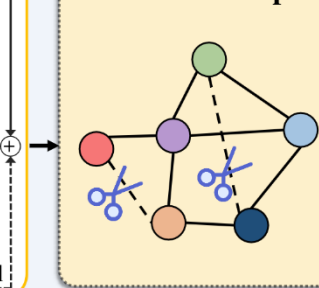
Day Type



Holiday

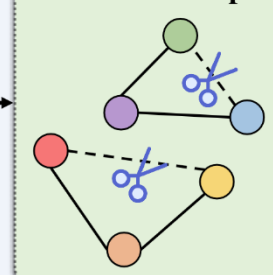


### Spatial Semantic Graph



Intervention

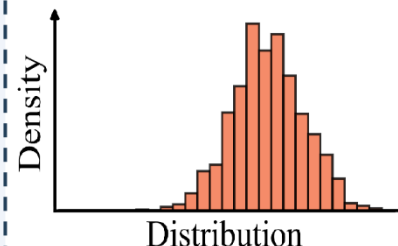
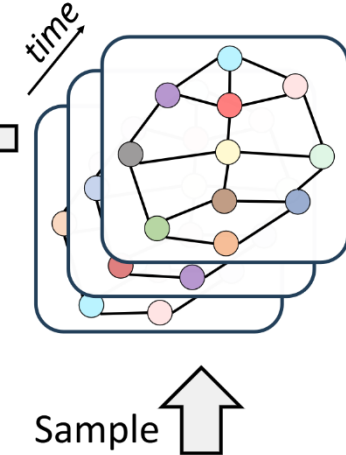
### Temporal Semantic Graph



Spatial GCN

Temporal GCN

### Testing Data



Spatio-temporal Shift

## ◇ Datasets: SD and GBA in LargeST under OOD setting

- ❖ [1/1/2019, 8/31/2019] for training,  
[9/1/2019, 10/31/2019] for validation,  
[11/1/**2020**, 12/31/**2020**] for test, etc.
- ❖ Vertices increases by **5%/10%/15%** and decreases by **5%** in validation and test sets.
- ❖ STONE exhibits a relative improvement of up to nearly **20%**.
- ❖ Result details in paper.





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**Thanks,  
See you Barcelona!**

