ECEN 5823-001 Internet of Things Embedded Firmware

Lecture #13 09 October 2018





Agenda

- Class Announcements
- Reading assignment
- Mid-term structure
- Firmware best practices
- Bluetooth Low Energy / Smart





Class Announcements

- Quiz #7 is due at 11:59 on Sunday, October 7th, 2018
- Homework #4: BLE Server + MITM + LCD due on Sunday, October 7th, at 11:59pm
- Homework #5: Client flowchart due on Wednesday, October 10th, at 11:59pm
- Homework #6: Client-Server due on Wednesday, October 17th, at 11:59pm
- Mid-term in class on Thursday the 18th
 - Attendance is required for on-campus students



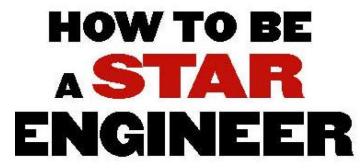
Reading Assignment

ECEN5823-001, -001B – Reading List
Internet of Things Embedded Firmware
Week 7

Note: The material in this reading as well as all lectures and assignments may be on this week's quiz, quiz 7.

- "How to be a Star Engineer," by Robert E. Kelley
- Bluetooth blog: Bluetooth Mesh Networking: Friendship by Kei Ren
 - o http://blog.bluetooth.com/bluetooth-mesh-networking-series-friendship
- Bluetooth blog: Management of Devices in a Bluetooth Network by Martin Wooley
 - o https://blog.bluetooth.com/management-of-devices-bluetooth-mesh-network

Engineers from the best companies helped researchers to dispel the myths about star performers and uncover the surprising secrets of stellar achievement







Mid-term structure

- Attendance is a must for on-campus students Thursday the 18th
 - A zero will be recorded for on-campus students that do not take it in class
 - Be on-time!
- CU Honor Code is in affect
- A single sheet of 8x11 paper, both sides, of notes is allowed
 - These notes must be of your own
 - They will be handed in at the end of the mid-term
 - If the notes are copied or determined not individual work, a zero will be recorded for the mid-term and a CU Honor code violation will be initiated resulting in a "F" in the course
- Distant students will have until 11:59pm on Friday the 19th to complete the exam





Mid-term structure

- Mid-term will comprise of 60 questions taken via Canvas
 - 35 questions from the Quiz 1 thru 7 question banks
 - 25 questions from a mid-term question bank
- If there is a canvas question issue such as no way to input an answer, please submit the issue to me after the exam via slack.
 - I will make a manual adjustment
- You can ask for clarification from the mid-term proctor



In Bluetooth Smart, privacy is the ability to prevent others from devices that you are carrying. (single word answer) by the



The parameter which defines the number of consecutive connection events which the Bluetooth Smart slave is not required to listen to the master and thus turn off its radio and possible go to sleep.

- connEvent
- SlaveLatency
- connInterval
- connLatency



List the sequence in pairing two BLE devices

Announce their input/output capabilities	[Choose]	•
Agree upon a Temporary Key	[Choose]	•
Short Term Key is obtained by both devices	[Choose]	•
the 128-bit Long-Term Key (LTK); the Connection Security Resolving Key (CSRK), the Identity Resolving Key (IRK).	[Choose]	•





When two BLE devices are reconnecting, either device can initiate encryption. Each and every data packet that is transmitted from then will incorporate the following?

- MIC
- Packet size
- Header
- CRC



Select the Bluetooth Smart authentication method based on the following:

device 1: Keyboard only

device 2: No input and no output

Passkey Entry

Just Works



Every Bluetooth connection event starts with a transmission of a package by the master.

True

False



For a Bluetooth Smart application where somewhat a real-time response is required, less than 500ms, which settings would you select? (select all that apply)

- High connInterval
- Low connInterval
- Low SlaveLatency
- High SlaveLatency



The initiator coordinates the medium access by providing information on the Time Division Multiple Access (TDMA) scheme and provides the slave with the frequency hopping algorithm during which transmission?

- Connection event
- Connection request
- Advertising event



The maximum number of slaves that a BLE master can connect to is 7.

True

False



Which algorithms are used to protect against the man-in-the-middle attack during BLE pairing to obtain the Temporary Key?

- Randomization
- Out of Band
- Passkey Entry
- Just Works



Maximum BLE L2CAP payload size?





Which modulation scheme does Bluetooth BLE support?

- Binary Phase Shift Keying
- Frequency Shift Keying
- Amplitude Shift Keying
- Gaussian Frequency Shift Keying
- Phase Shift Keying



- How to make an operation such as a read-modify-write atomic?
 - Interrupts must be disabled before the global variable access
 - And, then interrupts must be enabled after the global variable access
 - What are the downsides of disabling interrupts while an atomic operation is in progress?
 - Increases the system latency (the time to respond to an interrupt)
 - Can have a negative affect in Real-Time Systems





- State Machines can keep your system organized while you have more than one task
- A state machine will have a defined behavior based on the following:
 - "context" (internal state)
 - And, the environment, input variables
- A visual representation of a state machine is a flow chart
 - A next state should be defined for every possible combination of input variables or events, even if it is assumed not to be possible
 - The "not possible" event could specify to remain in the same state or possibly generate a system fault





- State Machines can have global variables that define the current state of the State Machine
 - For example, in the Lifting Accelerometer, there is a state machine that sets the sleep mode of the Leopard Gecko
 - The state machine global variables are controlled by two routines
 - BlockSleepMode()
 - And,

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- UnBlockSleepMode()
- If the global variables are not set or cleared correctly, the next state of the sleep()
 routine could put the Leopard Gecko in an Energy Mode that a required peripheral
 cannot support





 The solution to insuring that the state bits do not change with uncertainty, is to make the change of these state bits atomic

```
Void BlockSleepMode(int EMlevel) {

INT_Disable();

SleepModeBlockLeve (EMlevel) ++;

INT_Enable();
}
```



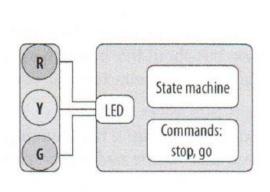


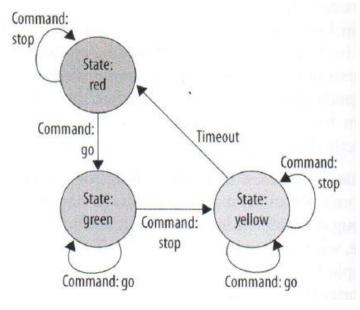
- State Machines make code testing and verification easier
 - Each state has a fixed possible combinations based on the events to the current context, internal state
 - Having a manageable possible combination of next states, enables code verification at the design, testing, and verification stages
 - Significantly reducing possible errors
 - During the design phase, check whether the state changes based on events match the flow chart of the state machine





• Flow diagram example:







Current State	Event (1 = Go, 0 = Stop)	Time Out	Next State
00 (Red)	0 (Stop)	0 (False)	00 (Red)
00 (Red)	0 (Stop)	1 (True)	00 (Red)
00 (Red)	1 (Go)	0 (False)	00 (Go)
00 (Red)	1 (Go)	1 (True)	00 (Go)
01 (Green)	0 (Stop)	0 (False)	00 (Yellow)
01 (Green)	0 (Stop)	1 (True)	00 (Yellow)
01 (Green)	1 (Go)	0 (False)	01 (Green)
01 (Green)	1 (Go)	1 (True)	01 (Green)
11 (Yellow)	0 (Stop)	0 (False)	11 (Yellow))
11 (Yellow)	0 (Stop)	1 (True)	00 (Red)
11 (Yellow)	1 (Go)	0 (False)	11 (Yellow)
11 (Yellow)	1 (Go)	1 (True)	00 (Red)





- A watchdog timer (sometimes called a computer operating properly or COP timer, or simply a watchdog) is an electronic timer that is used to detect and recover from computer malfunctions.
 - During normal operation, the computer regularly resets the watchdog timer to prevent it from elapsing, or "timing out".
 - If, due to a hardware fault or program error, the computer fails to reset the watchdog, the timer will elapse and generate a timeout signal.
 - The timeout signal is used to initiate corrective action or actions.
 - The corrective actions typically include placing the computer system in a safe state and restoring normal system operation. (source: Wikipedia)





- The watchdog timer's goal is to fail in a save manner if it fails
 - Goal is to have the watchdog service routing in a part of the code that is demonstrating that all systems are running as expected
 - Generally, this is the main loop
 - For board bring up, watchdog timer can cause issues in the debugger at or after bring up
 - Its good practice to have a watchdog timer to fail in a safe manner
 - And, its good practice to disable the watchdog timer during board bring up





- Data Handling
 - Data-driven systems
 - Get data
 - Process it
 - Do something with the results
 - Repeat
 - Implementing data-driven system is straight forward because the process of the data is repetitive
 - Example
 - A producer of data such as an ambient light sensor
 - The consumer, MCU, processes the data
 - Sending the data to the greater system
 - Repeat
 - Most system have elements of both an event-driven and data-driven system





- In a data-driven system, if data is produced at one data-rate while it is consumed at a different-rate, what data structure or technique is commonly used?
- Circular Buffers is a key implementation among data-driven systems
 - They are First In First Out (Buffers)
 - A producer puts data in the circular buffer at some rate
 - And, the consumer take data out of the circular buffer at a rate equivalent or faster than the producers put it in
- The Circular Buffer needs to keep track of the next elements
 - Where to put, write, the next buffer
 - Circular_Write_Ptr
 - Where to take, read, the current buffer
 - Circular_Read_Ptr



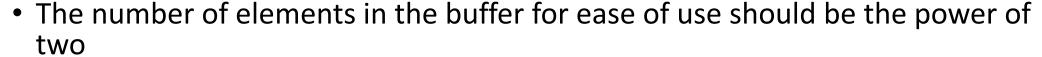


- Both the producers and consumers are accessing the circular buffer, the buffer is a global variable
 - To prevent data race contentions to the buffers, the read and write pointers are used and must not point to the same buffer location
- Also, both Circular_Write_Ptr and Circular_Read_Ptr are shared between multiple tasks, thus, the pointers are global variables
 - With the pointers being global variables, the update of these variables must be atomic
- The pointers being atomic, insures that the data circular buffers are atomic as well





- Circular buffers
 - The buffer is empty when the read pointer is equal to the write pointer
 - But, when the buffer is full, the read pointer is equal to the write pointer as well due to being a circular buffer
 - A common workaround is to call the circular buffer full when the write buffer is one away from the read pointer



- Enabling a simple mask to allow the pointers to rollover
 - Example: 4 elements in the circular buffer
 - Pseudo code:
 - Write Ptr = (Write Ptr++) & 0x03;
 - Will result in pointer values of 00, 01, 10, 11, 00, 01, 10, 11





- Circular buffers with their "atomic" pointers are a very good way of sharing streams of data between two or more tasks
- Try to size the elements in the buffer to a reasonable size that will minimize the chances of possible buffer overflow conditions



Firmware Best Practices (Circular Buffer ex.)

```
void Atomic_Print(char *outputstring){
  INT_Disable();
  TX_Buffer_Write_Ptr = (TX_Buffer_Write_Ptr + 1) % NUM_TX_Buffers;
  strncpy(BluetoothTransmitBuffer[TX_Buffer_Write_Ptr],"",BluetoothMaxTXBufferSize);
strncpy(BluetoothTransmitBuffer[TX_Buffer_Write_Ptr],outputstring,BluetoothMaxTXBufferSize);
  if (!TransmittingData) Print Bluetooth Out();
  INT Enable();
```





Firmware Best Practices (Circular Buffer ex.)

```
void LEUARTO_TX_dmaTransferDone(unsigned int channel, bool primary, void *user) {
INT_Disable();
  DMA->IFC = LEUARTO_TX_DMA_Channel;
  LEUARTO->CTRL &= ~LEUART CTRL TXDMAWU;
  strncpy(BluetoothTransmitBuffer[TX_Buffer_Transmit_Ptr],"",BluetoothMaxTXBufferSize); //
after transmit, initialize to ""
  TransmittingData=false;
  if (TX_Buffer_Transmit_Ptr != TX_Buffer_Write_Ptr) Print_Bluetooth_Out();
  INT Enable();
```





Firmware Best Practices (Circular Buffer ex.)

```
void Print Bluetooth Out(void){
 INT Disable();
 TransmittingData = true;
 TX Buffer Transmit Ptr = (TX Buffer Transmit Ptr + 1) % NUM TX Buffers;
 str length = strlen(BluetoothTransmitBuffer[TX Buffer Transmit Ptr]);
 str ptr = &BluetoothTransmitBuffer[TX Buffer Transmit Ptr][0];
 LEUARTO->CTRL |= LEUART CTRL TXDMAWU;
 DMA ActivateBasic(
      LEUARTO TX DMA Channel, // LEUARTO transmit channel
                        // Use primary descriptors
      true,
                       // No burst mode, LEUARTO does not support it
      false,
      (void *)&LEUARTO->TXDATA,
      (void *)str ptr, // Beginning of output string
     str length - 1); // Transmit length
 INT Enable();
```



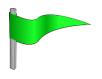


- Int a;
- Are these three expression equivalent in c-code? NO

Integer Math



- Another example
- In "real" math, (5/2) * 3 = 7.5
- In Integer math, ordering matters towards precision. What operation in the above example should be done first?



If staying strictly in Integer Math, always do the multiplication first. Will limit the loss of accuracy



- Speeding up your Math
 - Know your compiler and processor
 - Additions and Subtractions are fast
 - Division is very slow, and floating point math is "dead slow"





Cortex-M3: Integer vs floating point addition

```
C-code for integer addition:
```

```
int ramBufferData[BufferSize];
int Summation;

Summation = 0;
for(j=0;j<BufferSize;j++) {
    Summation = Summation + ramBufferData[j];
}</pre>
```

Assembly code equivalent:

```
Summation = Summation + ramBufferData[j];

00005450: ldr r3,[pc,#0x7c]; 0x54cc

00005452: ldr r2,[sp,#0x1c]

00005454: ldrh.w r3,[r3,r2,lsl #1]

00005458: ldr r2,[sp,#0x18]

0000545a: add r3,r2

0000545c: str r3,[sp,#0x18]
```

6 Assembly Instructions



88 Assembly Instuctions!



Cortex-M3: Integer vs floating point addition

```
000056f2: beq 0x000000000005774
C-code for float addition:
                                                                                                                            0000569e: itttt ne
                                                                                00005804: ands r3,r0,#0x80000000
                                                                                                                                                                   000056f4: sub.w r2,r2,#0x1
           int ramBufferData[BufferSize];
                                                                                                                            000056a0: lsls.w r3,r1,#1
                                                                                00005808: it mi
                                                                                                                                                                   000056f8: asr.w r12,r1,r3
                                                                                                                            000056a4: teg r2,r3
           float Summation;
                                                                                0000580a: rsbs r0,r0,#0
                                                                                                                                                                   000056fc: adds.w r0,r0,r12
                                                                                                                            000056a8: mvns.w r12,r2,asr#24
                                                                                0000580c: movs.w r12,r0
                                                                                                                                                                   00005700: rsb.w r3,r3,#0x20
                                                                                                                            000056ac: mvns.w r12.r3.asr#24
          Summation = 0;
                                                                                00005810: it
                                                                                                                                                                   00005704: lsl.w r1,r1,r3
                                                                                                                            000056b0: beg 0x000000000005788
          for(j=0;j<BufferSize;j++) {
                                                                                00005812: bx
                                                                                                                            000056b2: lsr.w r2,r2,#24
                                                                                                                                                                   00005708: and r3,r0,#0x80000000
              Summation = Summation + ramBufferData[i];
                                                                                                                            000056b6: rsbs r3,r2,r3,lsr#24
                                                                                00005814: orr r3,r3,#0x4b000000
                                                                                                                                                                   0000570c: bpl 0x000000000005714
                                                                                                                            000056ba: itttt gt
                                                                                00005818:
                                                                                           mov r1,r0
                                                                                                                                                                   0000570e: rsbs r1,r1,#0
                                                                                                                            000056bc: adds r2,r2,r3
                                                                                00005814: mov.w r0.#0x0
                                                                                                                                                                   00005710: sbc.w r0,r0,r0,lsl#1
                                                                                                                            000056be: eors r1,r0
                                                                                0000581e: b
                                                                                               0x000000000000585a
                                                                                                                                                                  00005714: cmp.w r0,#0x800000
                                                                                                                            000056c0: eors r0,r1
Assembly code equivalent:
                                                                                2000585a: sub.w r3,r3,#0x800000
                                                                                                                                                                   00005718: bcc 0x000000000005742
                                                                                                                            000056c2: eors r1,r0
                                                                                0000585e: clz r2,r12
        Summation = Summation + ramBuff_rAdcData[i];
                                                                                                                            000056c4: it lt
                                                                                                                                                                   0000571a: cmp.w r0,#0x1000000
                                                                                00005862: subs r2,#0x8
                                                                                                                            000056c6: rsbs r3,r3,#0
        00005452: ldr r3,[pc,#0x90]; 0x54e0
                                                                                                                                                                   0000571e: bcc 0x00000000000572e
                                                                                                                                          r3,#0x19
                                                                                                                            000056c8: cmp
                                                                                00005864: sub.w r3,r3,r2,lsl #23
                                                                                                                                                                  0000572e: cmp.w r1.#0x80000000
        00005454: ldr r2,[sp,#0x1c]
                                                                                                                            000056ca: it hi
                                                                                00005868: blt 0x00000000000588c
                                                                                                                                                                   00005732: adc.w r0,r0,r2,lsl #23
        00005456: ldrh.w r3,[r3,r2,lsl #1]
                                                                                                                            000056cc: bx Ir
                                                                                0000586a: lsl.w r12,r1,r2
                                                                                                                                                                   00005736: it eq
        0000545a: mov
                            r0,r3
                                                                                                                            000056ce: tst r0.#0x80000000
                                                                                0000586e: add
                                                                                                r3,r12
                                                                                                                                                                   00005738: bic r0,r0,#0x1
                                                                                                                            000056d2: orr r0,r0,#0x800000
        0000545c: bl
                          0x00005804
                                                                                00005870: lsl.w r12,r0,r2
                                                                                                                            000056d6: bic r0,r0,#0xff000000
                                                                                                                                                                   0000573c: orr.w r0,r0,r3
        00005460: mov
                            r3.r0
                                                                                00005874: rsb.w r2,r2,#0x20
                                                                                                                            000056da: it ne
                                                                                                                                                                   00005740: bx lr
        00005462: ldr
                           r0,[sp,#0x18]
                                                                                00005878: cmp.w r12,#0x80000000
                                                                                                                            000056dc: rsbs r0,r0,#0
        00005464: mov
                           r1.r3
                                                                                                                            000056de: tst r1.#0x80000000
                                                                                0000587c: lsr.w r2,r0,r2
        00005466: bl
                          0x0000569c
                                                                                                                            000056e2: orr r1,r1,#0x800000
                                                                                00005880: adc.w r0,r3,r2
                                                                                                                            000056e6: bic r1,r1,#0xff000000
        0000546a: mov
                            r3.r0
                                                                                00005884: it
                                                                                               eq
                                                                                                                            000056ea: it ne
                          r3,[sp,#0x18]
        0000546c: str
                                                                                00005886: bic
                                                                                               r0,r0,#0x1
                                                                                                                            000056ec: rsbs r1.r1.#0
                                                                                0000588a: bx
                                                                                                                            000056ee: teq r2,r3
```



0000569c: lsls r2.r0.#1



- Speeding up your Math
 - Know your compiler and processor
 - Additions and Subtractions are fast
 - Division is very slow, and floating point math is "dead slow"
 - Many processors have hardware support for multiplication





- Speeding up your Math
 - As the previous example, a single line of code can explode into many assembly instructions if the hardware does not support in hardware the operation
 - Division is the most common basic operation not supported in hardware
 - Modulo math is very helpful in circular buffers, used by the write and read pointers to wrap around the pointer values
 - What type of common operation is modulo math related to?
 - %, modulo operative, is actually a division





- Speeding up your Math
 - Write_Ptr = Write_Ptr++ % 0x04;
 - Costly in energy, time, and possibly code space
 - Modulo math can be replaced with a very fast and possible a single or two assembly instruction
 - What fast and low energy operation can we use instead of module math?
- Write_Ptr = Write_Ptr++ & 0x03;
 - Best practice is to replace modulo operations with bit-wise "AND" operation where possible





- Speeding up your Math
 - Multiplication and Divisions by power of 2 are usually single operations
 - How can power of 2 multiplications and divisions be a single operation?
 - Multiplication, shift to the left
 - Division, shift to the right







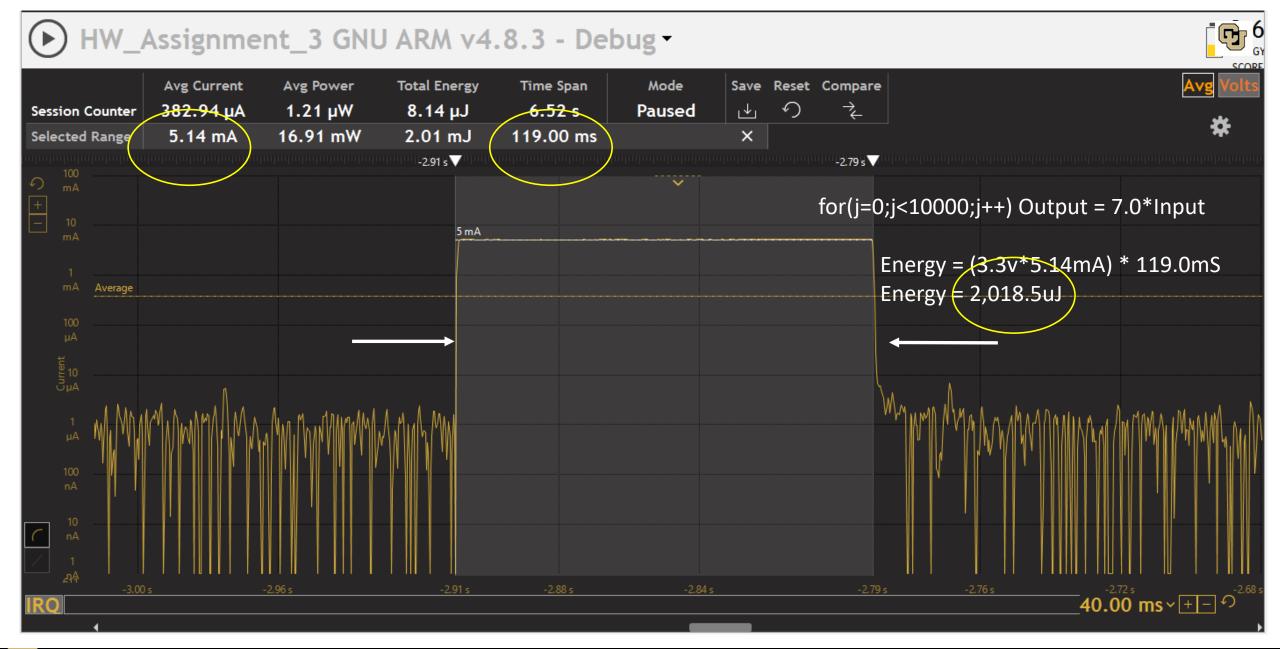
- Speeding up your Math
 - Constants are faster than using variables
 - They can be imbedded in assembly instructions
 - They must be "real" constants, and not variables
 - "real" constants in C are #define, not constant variables (const)
- Putting constants in #define is good programming practice for readability and for Speeding up your Math



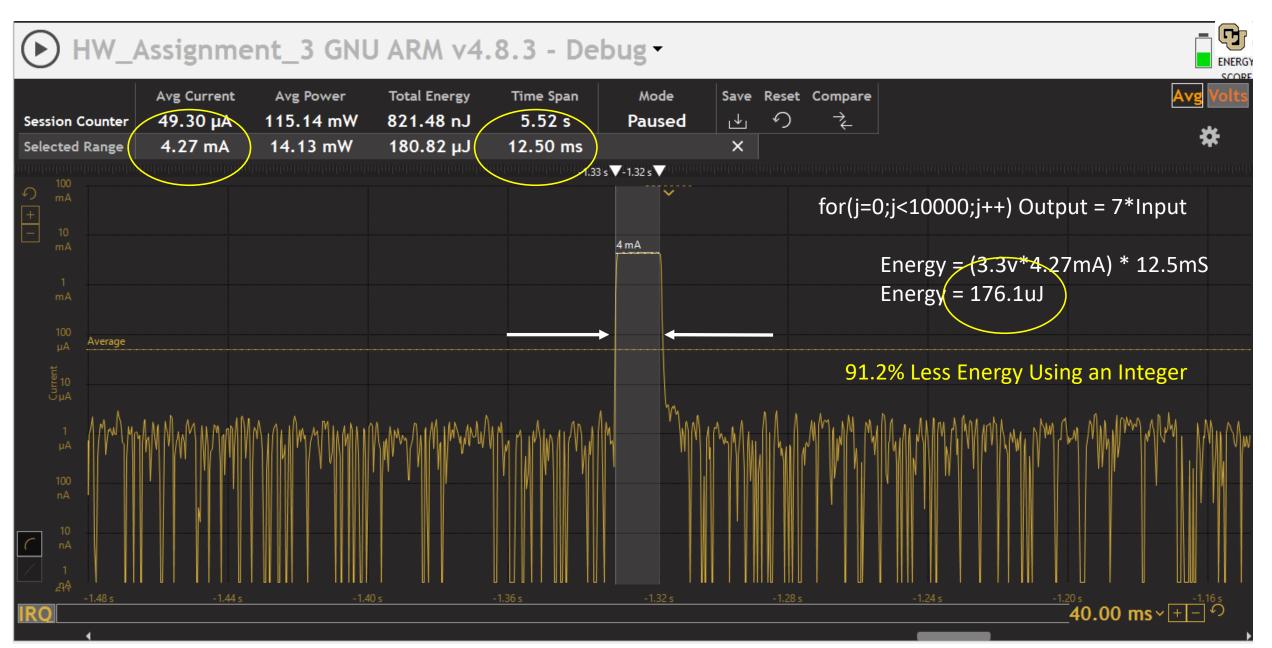


- Speeding up your Math
 - A floating point constant will generate a floating point instruction as much as a float variable
 - If a constant does not need to be float, make it an integer
 - Example:
 - Lets take a look at the constant 7 on a Cortex-M3 integer based MCU
 - The constant will be defined as 7.0 and 7













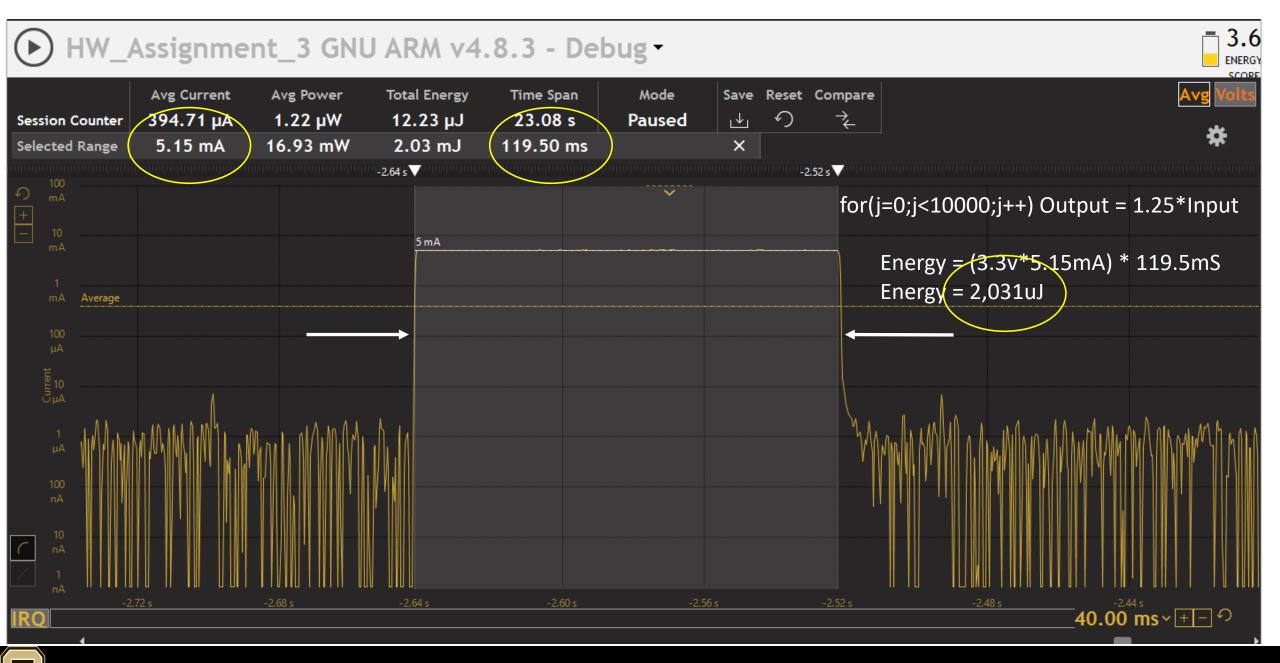
- Speeding up your Math
 - Using an integer 7 over the float 7.0 resulted in the following savings:
 - 2018.5uJ / 176.1uJ = 11.46x savings in Energy
 - 119mS / 12.5mS = 9.52x savings in Time
 - Where possible, specify constants in whole integers

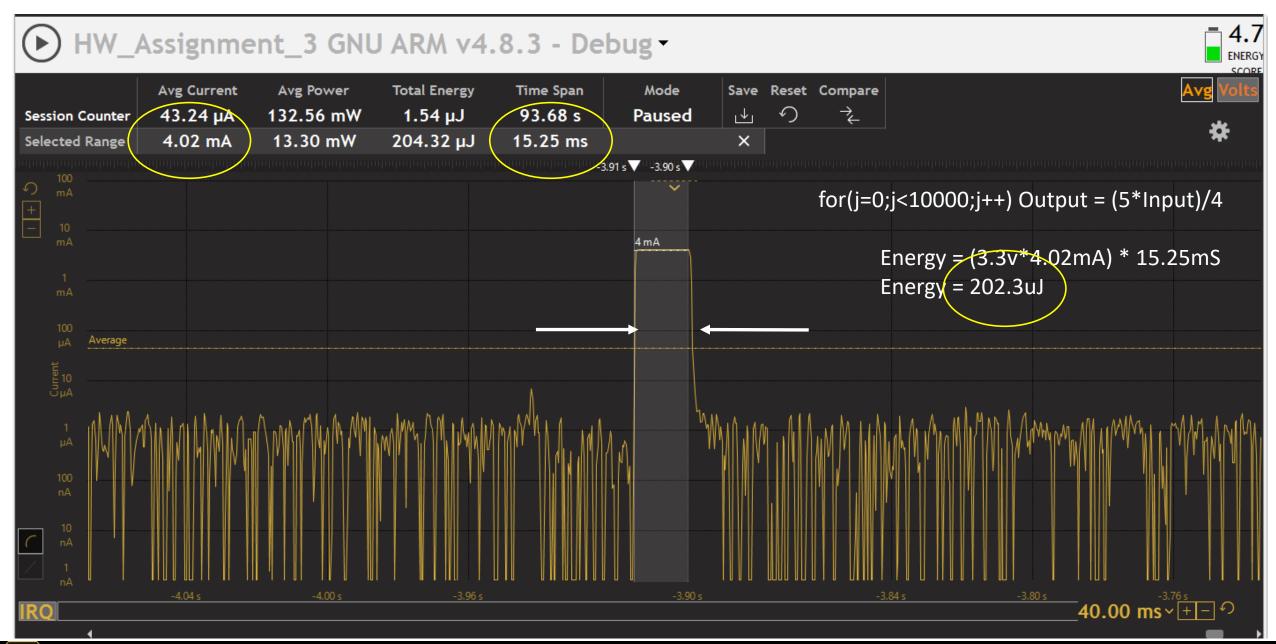




- Speeding up your Math
 - Convert rational numbers into fractions when the divisor is a power of 2
 - For example, a constant of 1.25 could be represented by 5/4
 - Is Output = 1.25*Input equivalent to 5/4*Input in Integer math? NO!
 - In 1.25*Input, the rounding occurs after the multiplication (Input = 5, Output = 6)
 - 5/4*Input, the rounding occurs after 5/4 (Input = 5, Output = 5)
 - (5*Input) / 4 is equivalent. (Input = 5, Output = 6)











Assembly code for Output = 1.25*Input

```
r0,[sp,#0x4]
000055a2: ldr
               0x00005978
000055a4:
000055a8: mov r2.r0
000055aa: mov
                r3,r1
000055ac: mov
                r0.r2
000055ae: mov
                r1,r3
000055b0: mov.w r2,#0x0
000055b4: ldr
               r3,[pc,#0x30]; 0x55e4
000055b6: bl
               0x00005a44
000055ba: mov
                r2,r0
000055bc: mov
                r3,r1
000055be: mov
                r0.r2
000055c0: mov r1,r3
000055c2:
              0x0Ó005e68
000055c6: mov r3,r0
000055c8:
               r3,[sp,#0xc]
         str
00005978: tea
              r0,#0x0
0000597c: itt
0000597e: movs 'r1.#0x0
00005980:
00005982: push {r4,r5,lr}
00005984:
          mov.w `r4,#0x400
00005988:
          add.w r4,r4,#0x32
0000598c: ands r5,r0,#0x80000000
00005990:
              mi
00005992: rsbs r0,r0,#0
00005994: mov.w r1,#0x0
00005998: b
               0x000000000005818
00005818: teq
              r1,#0x0
0000581c: itt
0000581e:
         mov r1,r0
00005820: movs r0,#0x0
00005822: clz
```

```
00005826: it
00005828: adds r3,#0x20
0000582a: sub.w r3,r3,#0xb
0000582e:
             subs.w r2,r3,#0x20
00005832: bge
000584e: it le 00005850: rsb.w r12,r2,#0x20
00005854:
             lsl.w r1,r1,r2
00005858:
             lsr.w r12,r0,r12
0000585c:
0000585e: orr.w r1,r1,r12
00005862: lsls r0,r2
00005864: subs r4,r4,r3
00005866:
00005868:
             ittt ge
             add.w r1,r1,r4,lsl #20
0000586c:
             orrs r1,r5
0000586e: pop {r4,r5,pc}
00005a44: push {r4,r5,r6,lr}
00005a44: push {r4,r5,r6,lr
00005a46: mov.w r12,#0xff
00005a4a: orr r12,r12,#0x700
00005a4e: ands.w r4,r12,r1,lsr #20
00005a52:
00005a54:
             ittte ne
             ands.w r5,r12,r3,lsr #20
00005a58:
                    r4,r12
00005a5c: teg
                   r5,r12
                   0x000000000005c20
00005a60:
             bl ˈ
00005a64: add r4,r5
00005a66: eor.w r6,r1,r3
00005a6a:
             bic.w r1,r1,r12,lsl #21
00005a6e:
00005a72:
             bic.w r3,r3,r12,lsl #21
             orrs.w r5,r0,r1,lsl #12
```

ne

00005a78: orrs.w r5,r2,r3,lsl #12

```
r1,r1,#0x100000
                            00005a7c: orr
                           00005a80: orr r3,r3,#0x100000
00005a84: beq 0x00000000000
                                        beg 0x000000000005af8
.w r2,r3,#0x20 00005a86: umull r12,lr,r0,r2 0x000000000000584e0 00005a8a: mov.w r5,#0x0
                            00005a8e:
                                        umlal lr,r5,r1,r2
                           00005a92:
                                        and r2,r6,#0x80000000
                           00005a96: umlal lr,r5,r0,r3
00005a9a: mov.w r6,#0x0
00005a9e: umlal r5,r6,r1,r3
                                         umlal lr,r5,r0,r3
                                         umlal r5,r6,r1,r3
                            00005aa2:
                                               r12,#0x0
                            00005aa6:
                                        it
                           00005aa8: orr lr,lr,#0x1
00005aac: sub.w r4,r4,#0xff
                           00005ab0: cmp.w r6,#0x200
00005ab4: sbc r4,r4,#0x300
                            00005ab8: bcs 0x000000000005ac4
                            00005aba:
                                        IsIs.w Ir,Ir,#1
                           00005abe: adcs r5,r5
                           00005ac0: adc.w r6,r6,r6
                            00005ac4: orr.w r1,r2,r6,lsl #11
                            00005ac8: orr.w r1,r1,r5,lsr #21
                           00005acc: lsl.w r0,r5,#11
                            00005ad0:
                                         orr.w r0,r0,lr,lsr #21
                            00005ad4:
                                         lsl.w lr,lr,#11
                            00005ad8:
                                         subs.w r12,r4,#0xfd
                            00005adc:
                                        it hi
                            00005ade:
                                        cmp.w r12,#0x700
                            00005ae2:
                                         bhi 0x000000000005b22
                            00005ae4:
                                         cmp.w lr,#0x80000000
                           00005ae8:
```

00005aea: lsrs.w lr,r0,#1

00005aee: adcs r0,r0,#0x0

```
00005af2:
          adc.w r1,r1,r4,lsl #20
00005af6:
          gog
                {r4,r5,r6,pc}
00005e68:
          'lsl.w r2,r1,#1
00005e6c:
          adds.w r2,r2,#0x200000
00005e70:
                0x0000000000005e9e
00005e72:
          bpl
                0x0000000000005e98
00005e74: mvn r3,#0x3e0
00005e78:
          subs.w r2,r3,r2,asr #21
00005e7c: bls
               0x0000000000005ea4
00005e7e: lsl.w r3,r1,#11
00005e82: orr
               r3,r3,#0x80000000
00005e86:
          orr.w r3,r3,r0,lsr #21
00005e8a:
          tst r1,#0x80000000
00005e8e:
00005e92:
           Isr.w rÓ,r3,r2
           it
              ne
00005e94: rsbs r0,r0,#0
00005e96: bx
```

assembly nstructions



00005a76:



Assembly code for Output = (5*Input)/4

```
000055ca: ldr
                  r2,[sp,#0x4]
                                        Multiplication of 5 is:
000055cc:
                   r3,r2
            mov
                                        Left shift by 2 (multiplication by 4)
000055ce:
                  r3,r3,#2
            Isls
                                         Add input (now equivalent of multiplication by 5)
000055d0:
                   r3,r2 •
            add
000055d2:
                  r3,#0x0
            cmp
                                        Now, shift to the right by 2 to divide by 4
000055d4:
                   0x000055d8
             bge
000055d6: adds r3,#0x3
                                       Store result of (5*Input) / 4
                   r3,r3,#0x2
000055d8:
            asrs
                  r3,[sp,#0xc]
000055da:
            str
```

Only 9 assembly instructions





- Speeding up your Math
 - Fractional math where the divisor is a power of 2 provided the following savings over the floating constant:
 - 2031uJ / 202.3uJ = 10.04x savings in Energy
 - 119.5mS / 15.25mS = 7.84x savings in Time
 - Where possible, use correct ordering of fractions where the divisor can be of power 2 instead of a rational multiplication

