

# HKN ECE 120 Midterm 1 Worksheet

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## Binary Representations

### Problem 1

Write these conversions in decimal. Truncate if necessary.

- a. Convert  $100101_2$  to a 6-bit unsigned integer.
- b. Convert  $100101_2$  to a 6-bit signed magnitude integer.
- c. Convert  $100101_2$  to a 6-bit 2's complement integer.
- d. Convert  $011101110_2$  to a 9-bit unsigned integer.
- e. Convert  $011101110_2$  to a 9-bit 2's complement integer.
- f. Convert  $100100101101_2$  to a 11-bit unsigned integer.
- g. Convert  $100100101101_2$  to a 9-bit 2's complement integer.
- h. Convert  $001011101_2$  to a 12-bit unsigned integer.
- i. Convert  $10111_2$  to a 16-bit signed integer.

### Problem 2

Write these conversions in binary. Truncate if necessary.

- a. Convert  $51_{10}$  to a 8-bit unsigned integer.
- b. Convert  $51_{10}$  to a 8-bit signed magnitude integer.
- c. Convert  $51_{10}$  to a 8-bit 2's complement integer.
- d. Convert  $-240_{10}$  to a 9-bit unsigned integer.
- e. Convert  $-240_{10}$  to a 9-bit 2's complement integer.
- f. Convert  $1171_{10}$  to a 11-bit unsigned integer.
- g. Convert  $1171_{10}$  to a 11-bit 2's complement integer.
- h. Convert  $65_{10}$  to a 12-bit unsigned integer.
- i. Convert  $-23309_{10}$  to a 16-bit signed integer.

## Other Representations

### Problem 1

Convert these binary values to hexadecimal.

- a. 0010101101010110
- b. 1001010010001111
- c. 0011110000010010
- d. 1011111011101111
- e. 1111000000001101

### Problem 2

Convert these hexadecimal values to binary.

- a. x37A5
- b. x2009
- c. x1F06
- d. x2FFE
- e. xDEADBEEF

### Problem 3

Convert these hexadecimal values to ASCII.

- a. x4A
- b. x2F
- c. x0D
- d. x4045
- e. x6E6F

### Problem 4

Convert these ASCII characters to binary.

- a. 'h'
- b. '#'
- c. 'M'
- d. '!'
- e. "bob"

## Problem 5

True or False?

- a. An integer with 11 hexadecimal values is at most a 88-bit integer.
- b. The shortest hexadecimal string that we can encode any 69-bit unsigned integer into is 18 characters long.
- c. All uppercase letters in ASCII start with the binary string 0100.
- d. All lowercase letters in ASCII start with the binary string 011.
- e. There is an ASCII character that corresponds with x8A.
- f. ASCII characters are usually stored as signed 8-bit integers.
- g. The control characters in ASCII were originally used as special codes for teletypes, keyboards used for electrical telegraphs.

## Binary Operations

### Problem 1

Perform the following operations.

- a.  $1_2$  AND  $0_2$
- b.  $1_2$  OR  $0_2$
- c.  $10010010_2$  AND  $01111011_2$
- d.  $001010_2$  OR  $111101_2$
- e.  $x8618$  AND  $x7507$
- f.  $1_2$  XOR  $1_2$
- g.  $xCA09$  XOR  $x0990$
- h. NOT  $1001110100110101_2$
- i.  $1001001101_2$  NAND  $0110101110_2$
- j.  $100011_2$  NOR  $001000_2$
- k.  $x908$  NXOR  $xA51$

### Problem 2

Perform the following operations on unsigned integers. Assume the number of bits given. Indicate when there is an overflow.

- a.  $100100_2 + 010101_2$
- b.  $11011010_2 - 011010110_2$
- c.  $1001_2 - 1010_2$
- d.  $011101_2 + 111011_2$
- e.  $1111000_2 \ll 2$
- f.  $1111000_2 \gg 2$
- g.  $000100_2 \gg 2$

### Problem 3

Perform the following operations on signed integers. Assume the number of bits given. Indicate when there is an overflow.

- a.  $110010_2 + 110001_2$
- b.  $11011010_2 + 011010110_2$
- c.  $1001_2 - 1010_2$
- d.  $011101_2 - 111011_2$
- e.  $1111000_2 \ll 2$
- f.  $1111000_2 \gg 2$
- g.  $000100_2 \gg 2$

### Problem 4

Bitmasks.

- a. Suppose you have a 6-bit unsigned integer. What does applying AND  $110000_2$  return? What does it indicate?
- b. Suppose you have a 8-bit signed integer. What does applying AND  $10000000_2$  return? What does it indicate?

Suppose you have a 6-bit unsigned integer that represents 6 lights (1 = on, 0 = off).

- c. What operation and what mask should we use to enable a single light?
- d. What operation and what mask should we use to disable a single light?
- e. What operation and what mask should we use to toggle a single light?
- f. What operation can we use on these masks to form a new mask if we wanted to toggle more than one light?

## K-maps and Optimization

### Problem 1

Find the minimal SOP and POS expressions for the following table.

A	B	C	S
0	0	0	1
0	0	1	1
0	1	0	0
0	1	1	0
1	0	0	0
1	0	1	1
1	1	0	1
1	1	1	1

### Problem 2

Find the minimal SOP and POS expressions for the following table.

A	B	C	S
0	0	0	0
0	0	1	1
0	1	0	X
0	1	1	X
1	0	0	1
1	0	1	0
1	1	0	X
1	1	1	X

### Problem 3

Find the minimal SOP and POS expressions for the following table.

A	B	C	D	S
0	0	0	0	0
0	0	0	1	1
0	0	1	0	1
0	0	1	1	0
0	1	0	0	1
0	1	0	1	1
0	1	1	0	0
0	1	1	1	1
1	0	0	0	1
1	0	0	1	0
1	0	1	0	0
1	0	1	1	0
1	1	0	0	0
1	1	0	1	0
1	1	1	0	0
1	1	1	1	0

### Problem 4

Find the minimal SOP and POS expressions for the following table.

A	B	C	D	S
0	0	0	0	X
0	0	0	1	1
0	0	1	0	0
0	0	1	1	0
0	1	0	0	X
0	1	0	1	X
0	1	1	0	1
0	1	1	1	1
1	0	0	0	1
1	0	0	1	0
1	0	1	0	0
1	0	1	1	0
1	1	0	0	X
1	1	0	1	X
1	1	1	0	X
1	1	1	1	X

### Problem 5

Find the area and delay heuristics for the following expressions. Do not include NOT gates.

- a.  $ABC + A'B'C + C'$
- b.  $A + B + C + D(A + B)$
- c.  $ABCDEFGH IJKLMNOPQRSTUVWXYZ + Z$
- d.  $(AB)'(A + B)'(CD)$

### Problem 6

Implement the following expressions using AND and OR gates, then using NAND and NOR gates only.

- a.  $AB + C$
- b.  $A'B + AB' + ABC' + ABD'$
- c.  $(A + B + C')(A' + B + C)(A + B' + C)$
- d.  $(A + D)(B' + C' + A)$



## **IEEE 754 Floating Point**

### **Problem 1**

- a. item 1

## **C Basics**

### **Problem 1**

- a. item 1

## **C Programming**

### **Problem 1**

- a. item 1