

Data Structures & Algorithms

①

Assignment-1

1. Find the time complexity for the following scenarios.

a) for ($i=1; i \leq n; i++$) \rightarrow inner loop runs for 'n' times
for ($j=i; j \leq n; j++$) $\rightarrow j=i$ (i's value)
printf("Hi"); j (outer loop runs 'n' times)

$$\Rightarrow \frac{n + n}{n^2} \Rightarrow O(n^2)$$

Time complexity = $O(n^2)$

b) for ($i=1; i \leq n; i*=3$)

for ($j=1; j \leq n; j++$)

printf("Hello");

i	j
1	1
3	3
9	9
27	27
⋮	⋮
n	n

$$\text{Time complexity} = 1 + 3 + 9 + 27 + \dots + n \Rightarrow T(n)$$

$$\text{Gp series of } n\text{-terms} = 3^0 + 3^1 + 3^2 + 3^3 + \dots + 3^{\log n}$$

$$S_n = a_1 \left(\frac{1-r^n}{1-r} \right)$$

$$= 1 \left(\frac{1-3^{\log n + 1}}{3-1} \right)$$

$$= 3^{\log n} = n$$

Time complexity = $O(n)$