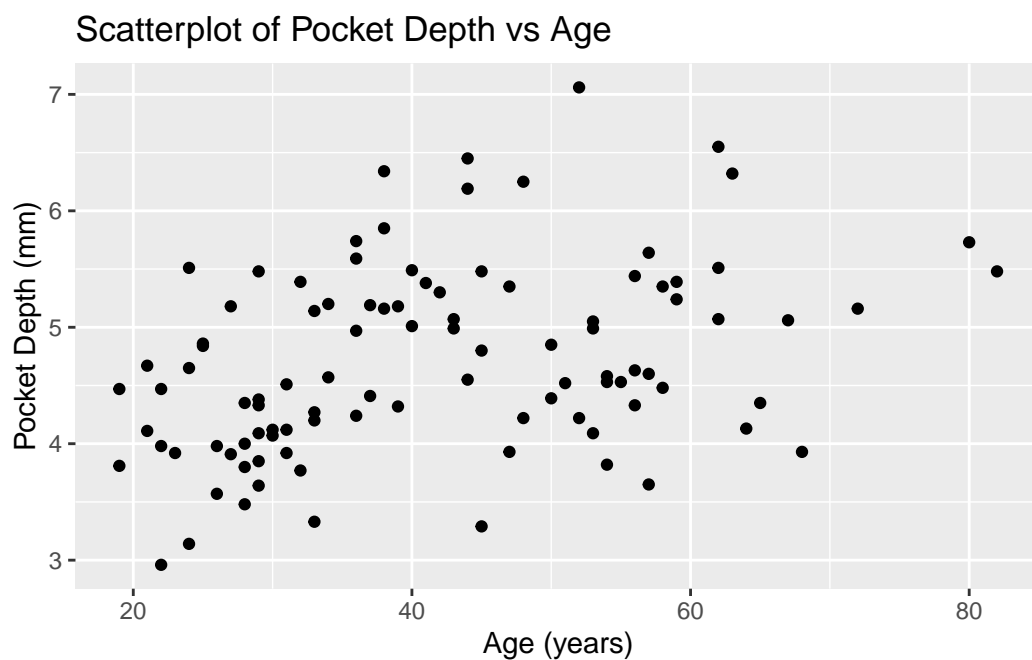


# Medical Statistics – Answers lab 6

## Part 1: Pearson's correlation coefficient and simple linear regression



### Question 1

Based on the scatterplot, is there an indication of a linear association between **age** and **pocketdepth**? If so, is this association positive or negative?

### Answer question 1

The scatterplot suggests that there is a positive linear association between **age** and **pocketdepth**. As age increases, pocket depth tends to increase.

## Pearson's Correlation Coefficient

Pearson's product-moment correlation

```
data: pockets$age and pockets$pocketdepth
t = 3.9647, df = 98, p-value = 0.0001398
alternative hypothesis: true correlation is not equal to 0
95 percent confidence interval:
 0.1891831 0.5295346
sample estimates:
      cor
0.371786
```

### Question 2

What does the correlation coefficient tell us about the relationship between **age** and **pocketdepth**? Does this align with your interpretation of the scatterplot?

### Answer question 2

The correlation coefficient is approximately 0.37, indicating a moderate positive linear relationship between **age** and **pocketdepth**. This aligns with the interpretation of the scatterplot.

### Question 3

What is the p-value for the correlation coefficient test? Based on this p-value, do we have sufficient evidence to reject the null hypothesis?

### Answer question 3

The p-value for the correlation coefficient test is approximately 0.00014, indicating that we have sufficient evidence to reject the null hypothesis of no correlation between **age** and **pocketdepth**.

## Fitting a Simple Linear Regression Model

```
Call:
lm(formula = pocketdepth ~ age, data = pockets)
```

Residuals:

	Min	1Q	Median	3Q	Max
	-1.49289	-0.44376	-0.07903	0.49597	2.13335

Coefficients:

	Estimate	Std. Error	t value	Pr(> t )
(Intercept)	3.85872	0.22862	16.878	< 2e-16 ***
age	0.02054	0.00518	3.965	0.00014 ***

---

Signif. codes: 0 '\*\*\*' 0.001 '\*\*' 0.01 '\*' 0.05 '.' 0.1 ' ' 1

Residual standard error: 0.7535 on 98 degrees of freedom

Multiple R-squared: 0.1382, Adjusted R-squared: 0.1294

F-statistic: 15.72 on 1 and 98 DF, p-value: 0.0001398

#### Question 4

Is the relationship between **age** and **pocketdepth** statistically significant (at  $\alpha = 0.05$ )?

#### Answer question 4

The estimated coefficient for **age** (0.021) is statistically significant with a p-value of 0.00014, indicating that the relationship between **age** and **pocketdepth** is statistically significant at  $\alpha = 0.05$ .

#### Question 5

How does the p-value for **age** in the regression output compare to the p-value for the correlation coefficient test? Are they consistent with each other?

#### Answer question 5

The p-value for **age** in the regression output (0.00014) and the p-value for the correlation coefficient test (0.00014) are consistent with each other. They both indicate a statistically significant relationship between **age** and **pocketdepth**.

#### Question 6

What is the interpretation of the intercept and the coefficient for **age** in the regression output?

#### Answer question 6

The intercept (3.859) represents the estimated pocket depth when age is 0, which may not have a meaningful interpretation in this context. The coefficient for **age** (0.021) represents the estimated change in pocket depth for each additional year of age.

#### Question 7

Based on the fitted model, what is the expected pocket depth for a person who is 40 years old?

#### Answer question 7

The expected pocket depth for a person who is 40 years old can be calculated using the intercept and coefficient from the regression output:  $3.859 + 0.021 * 40 = 4.699$  mm

#### Question 8

How much of the variation in pocket depth is explained by age in this model?

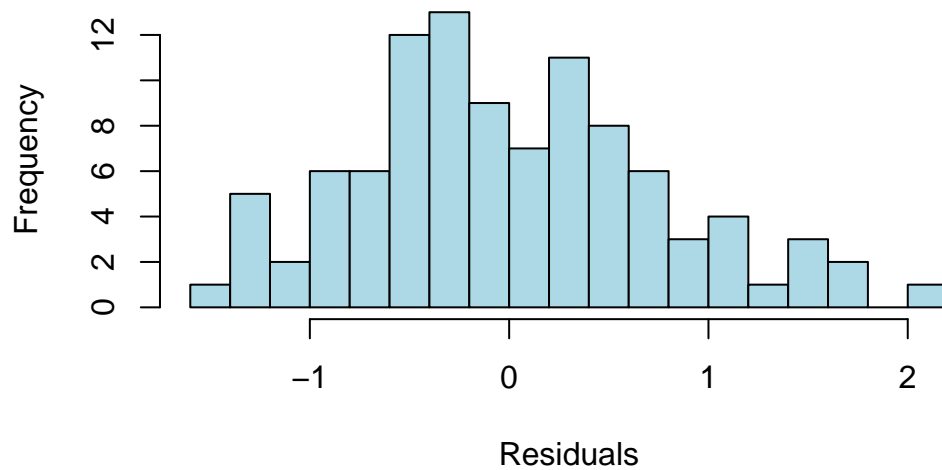
#### Answer question 8

The R-squared value of 0.138 indicates that approximately 14% of the variation in pocket depth is explained by age in this model.

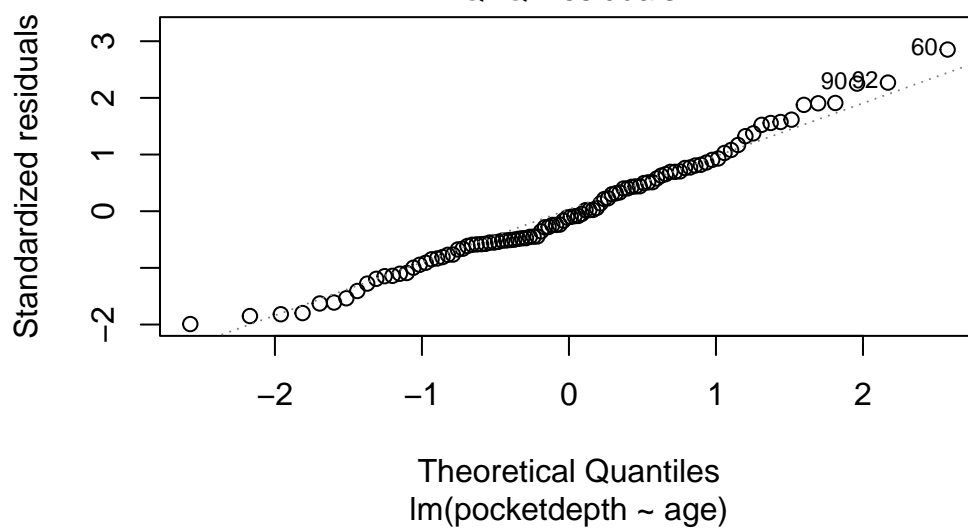
### Assumption Checking

#### Normality of Residuals

### Histogram of Residuals



### Q-Q Residuals



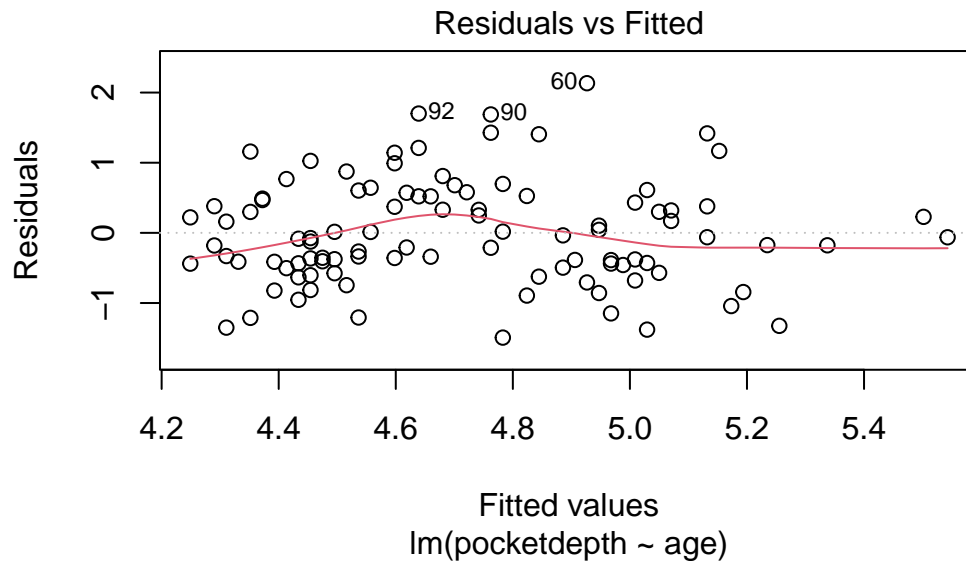
### Question 9

Do the histogram and Q-Q plot suggest that the residuals are reasonably normally distributed?

### Answer question 9

The two plots suggest that the residuals are approximately normally distributed, with the histogram showing a roughly symmetric shape and the Q-Q plot showing the residuals closely following the diagonal line.

### Homoscedasticity and linearity



### Question 10

Does the residual-versus-fitted plot suggest constant variance?

### Answer question 10

The residual-versus-fitted plot suggests that the variance of the residuals is relatively constant across the range of fitted values, indicating homoscedasticity.

### Question 11

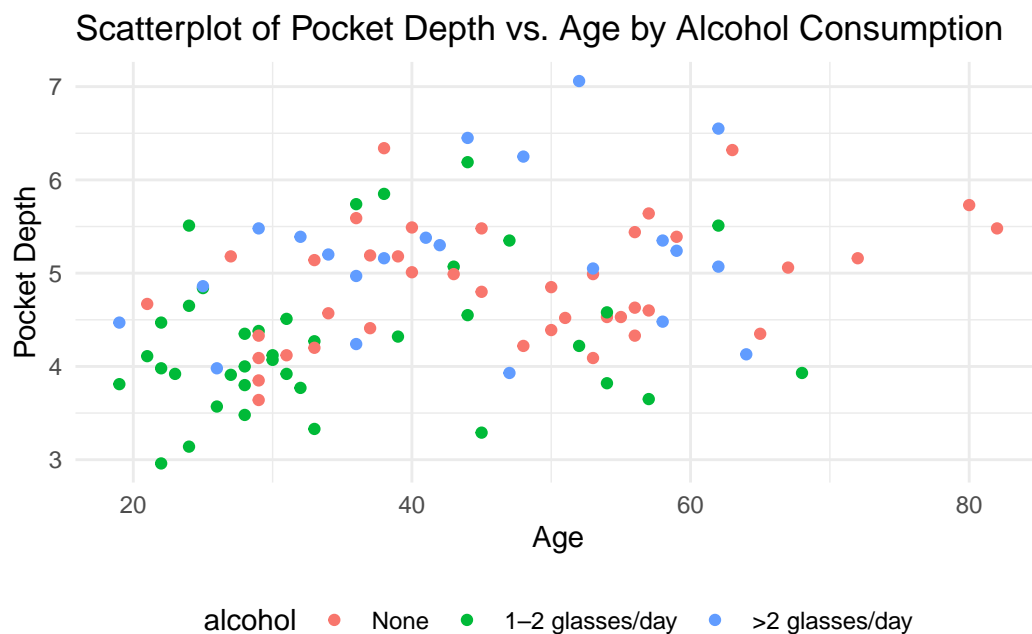
Does the residual-versus-fitted plot suggest any violation of the linearity assumption?

### Answer question 11

There is no obvious pattern or curvature in the residual-versus-fitted plot, indicating that the linearity assumption is not violated.

## Part 2: ANCOVA (Analysis of Covariance)

### Exploratory Data Analysis



### Question 12

What can you infer from the scatterplot about the relationship between `age`, `pocketdepth`, and `alcohol` consumption?

### Answer question 12

As discussed previously, the scatterplot suggests a positive relationship between **age** and **pocketdepth**, with higher pocket depths observed for older individuals. It also suggests that there is a U-shaped relationship between **alcohol** consumption and **pocketdepth**, with individuals consuming “1-2 glasses/day” having lower pocket depths compared to those consuming “None” or “>2 glasses/day”.

## Fitting the ANCOVA Model

### R output

Call:

```
lm(formula = pocketdepth ~ age + alcohol, data = pockets)
```

Residuals:

Min	1Q	Median	3Q	Max
-1.35037	-0.45299	-0.06626	0.39746	1.76573

Coefficients:

	Estimate	Std. Error	t value	Pr(> t )
(Intercept)	4.165461	0.270688	15.388	< 2e-16 ***
age	0.014849	0.005248	2.829	0.00568 **
alcohol1-2 glasses/day	-0.394551	0.172383	-2.289	0.02428 *
alcohol>2 glasses/day	0.364565	0.188347	1.936	0.05586 .

---

Signif. codes: 0 '\*\*\*' 0.001 '\*\*' 0.01 '\*' 0.05 '.' 0.1 ' ' 1

Residual standard error: 0.7069 on 96 degrees of freedom

Multiple R-squared: 0.257, Adjusted R-squared: 0.2338

F-statistic: 11.07 on 3 and 96 DF, p-value: 2.638e-06

### SPSS output



Between-Subjects Factors			
		Value Label	N
Alcohol consumption categories	0	None	40
	1	1–2 glasses/day	38
	2	>2 glasses/day	22

Tests of Between-Subjects Effects					
Dependent Variable: Average pocket depth (mm)					
Source	Type III Sum of Squares	df	Mean Square	F	Sig.
Corrected Model	16,593 <sup>a</sup>	3	5,531	11,068	<,001
Intercept	160,713	1	160,713	321,601	<,001
age	4,001	1	4,001	8,005	,006
alcohol	7,669	2	3,834	7,673	<,001
Error	47,974	96	,500		
Total	2287,218	100			
Corrected Total	64,567	99			

a. R Squared = ,257 (Adjusted R Squared = ,234)

Parameter Estimates						
Dependent Variable: Average pocket depth (mm)						
Parameter	B	Std. Error	t	Sig.	95% Confidence Interval	
					Lower Bound	Upper Bound
Intercept	4,530	,275	16,464	<,001	3,984	5,076
age	,015	,005	2,829	,006	,004	,025
[alcohol=0]	-,365	,188	-1,936	,056	-,738	,009
[alcohol=1]	-,759	,195	-3,888	<,001	-1,147	-,372
[alcohol=2]	0 <sup>a</sup>	.	.	.	.	.

a. This parameter is set to zero because it is redundant.

Figure 1: Screenshot of the SPSS output tables

### Question 13

Based on the ANCOVA model output, what is the expected difference in pocket depth between individuals who consume "None" and those who consume ">2 glasses/day",

while controlling for age?

#### Answer question 13

By default, the reference level for the `alcohol` variable is set to "None" in R and to ">2 glasses/day" in SPSS.

Looking at the R output, the coefficient for ">2 glasses/day" is 0.365, which means that individuals who consume ">2 glasses/day" are expected to have a pocket depth that is 0.365 mm higher than those who consume "None", while controlling for age.

Looking at the SPSS output, the coefficient for "None" is -0.365, which means that individuals who consume "None" are expected to have a pocket depth that is 0.365 mm lower than those who consume ">2 glasses/day", while controlling for age.

Therefore, the expected difference in pocket depth between individuals who consume "None" and those who consume ">2 glasses/day" is 0.365 mm, independent of the reference level chosen.

#### Question 14

Based on the ANCOVA model output, what is the expected difference in pocket depth between individuals who consume "1-2 glasses/day" and those who consume ">2 glasses/day", while controlling for age?

#### Answer question 14

By default, the reference level for the `alcohol` variable is set to "None" in R and to ">2 glasses/day" in SPSS.

Looking at the R output, the coefficient for ">2 glasses/day" is 0.365 and the coefficient for "1-2 glasses/day" is -0.395. This means that individuals who consume ">2 glasses/day" are expected to have a pocket depth that is  $0.365 - (-0.395) = 0.76$  mm higher than those who consume "1-2 glasses/day", while controlling for age.

Looking at the SPSS output, the coefficient for "1-2 glasses/day" is -0.759, which means that individuals who consume "1-2 glasses/day" are expected to have a pocket depth that is 0.759 mm lower than those who consume ">2 glasses/day", while controlling for age.

Therefore, the expected difference in pocket depth between individuals who consume "1-2 glasses/day" and those who consume ">2 glasses/day" is 0.76 mm, independent of the reference level chosen.

Anova Table (Type III tests)

Response: pocketdepth

Sum Sq	Df	F value	Pr(>F)
--------	----	---------	--------

```
(Intercept) 118.337 1 236.8042 < 2.2e-16 ***
age          4.001 1 8.0055 0.0056789 **
alcohol      7.669 2 7.6729 0.0008104 ***
Residuals    47.974 96
```

---

Signif. codes: 0 '\*\*\*' 0.001 '\*\*' 0.01 '\*' 0.05 '.' 0.1 ' ' 1

### Question 15

Based on the ANOVA table, is the `alcohol` variable significantly associated with `pocketdepth` after accounting for `age`?

### Answer question 15

The p-value for the `alcohol` variable in the ANOVA table is less than 0.05, indicating that the `alcohol` variable is significantly associated with `pocketdepth` after accounting for `age`.

## Model Diagnostics

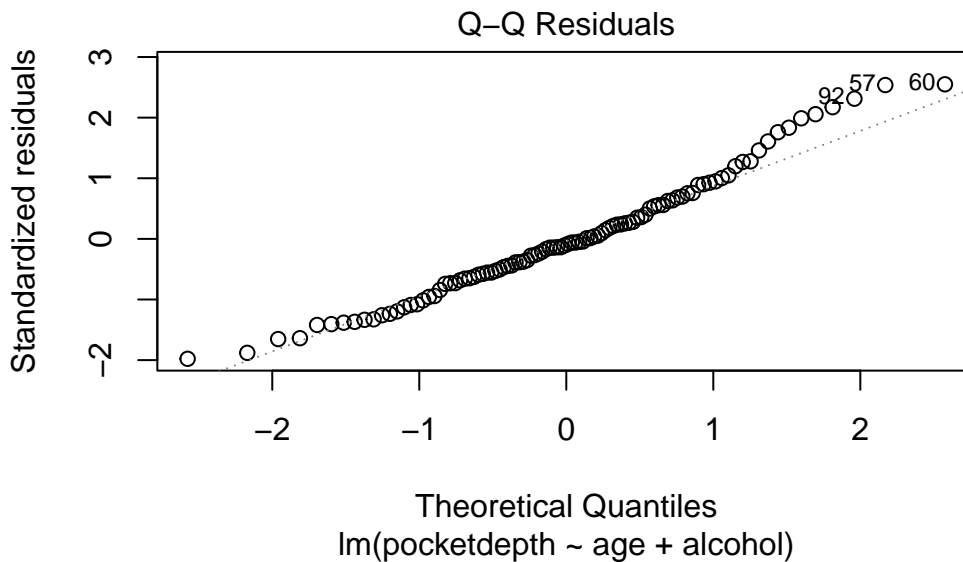
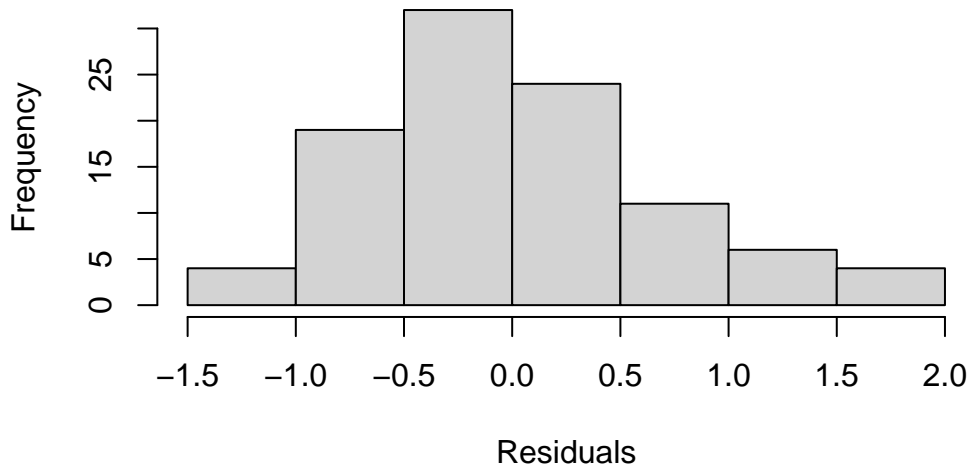
### Exercise

Check the normality of residuals and homoscedasticity assumptions for the ANCOVA model.

### Answer question 15

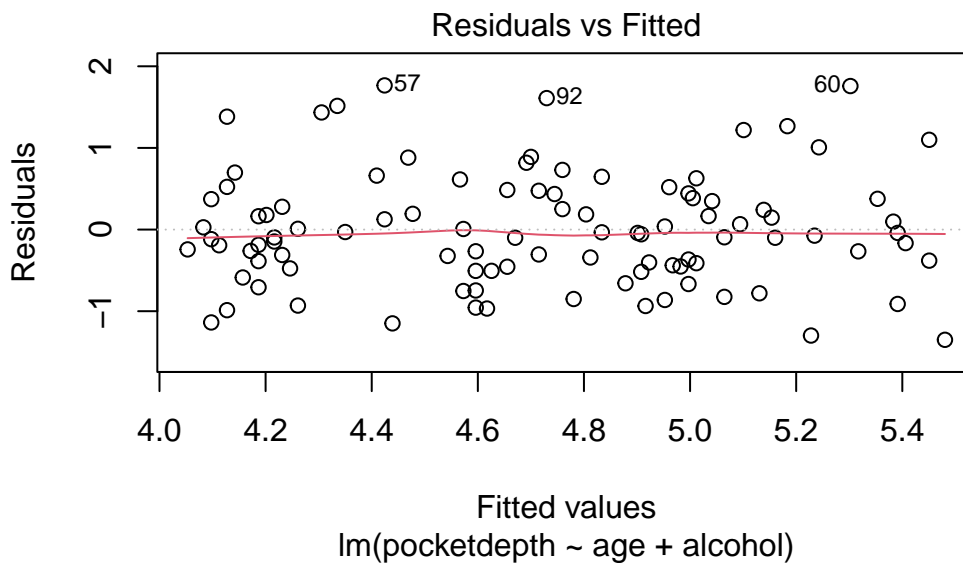
### Normality of Residuals

### Histogram of Residuals



The histogram and normal Q-Q plot of residuals shows that the residuals are approximately normally distributed, indicating that the normality assumption is not violated.

#### **Homoscedasticity**



The residuals vs. fitted plot shows that the residuals are randomly scattered around zero, indicating that the homoscedasticity assumption is not violated.

### Part 3: Interactions in ANCOVA

#### Fitting the Interaction Model

Call:

```
lm(formula = pocketdepth ~ age * alcohol, data = pockets)
```

Residuals:

Min	1Q	Median	3Q	Max
-1.35020	-0.45321	-0.06748	0.39755	1.76684

Coefficients:

	Estimate	Std. Error	t value	Pr(> t )
(Intercept)	4.161e+00	3.811e-01	10.921	<2e-16 ***
age	1.494e-02	7.747e-03	1.928	0.0569 .
alcohol1-2 glasses/day	-3.862e-01	5.142e-01	-0.751	0.4544
alcohol>2 glasses/day	3.690e-01	6.538e-01	0.564	0.5738
age:alcohol1-2 glasses/day	-2.082e-04	1.214e-02	-0.017	0.9863

```
age:alcohol>2 glasses/day -9.585e-05 1.395e-02 -0.007 0.9945
```

---

```
Signif. codes:  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
```

Residual standard error: 0.7144 on 94 degrees of freedom

Multiple R-squared: 0.257, Adjusted R-squared: 0.2175

F-statistic: 6.503 on 5 and 94 DF, p-value: 3.102e-05

Anova Table (Type III tests)

Response: pocketdepth

	Sum Sq	Df	F value	Pr(>F)
(Intercept)	60.865	1	119.2592	< 2e-16 ***
age	1.897	1	3.7169	0.05688 .
alcohol	0.784	2	0.7678	0.46691
age:alcohol	0.000	2	0.0001	0.99985
Residuals	47.974	94		

---

```
Signif. codes:  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
```

#### Question 16

Based on the output in the ANOVA table, is there a significant interaction between **age** and **alcohol** in predicting **pocketdepth**?

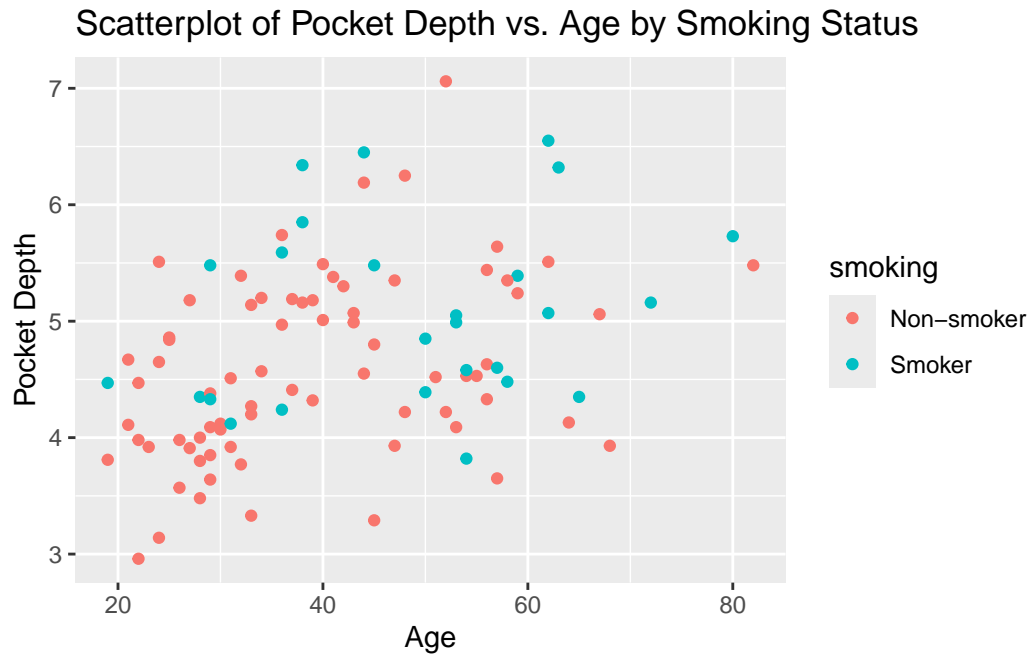
#### Answer question 16

The p-value for the interaction term **age:alcohol** in the ANOVA table is approximately equal to 1, indicating that there is no interaction between **age** and **alcohol** in predicting **pocketdepth**.

## Part 4: Relationship Between Smoking and Pocket Depth

In addition to information about alcohol consumption, the dataset also contains information about smoking habits. Explore the relationship between smoking and pocket depth, and how it interacts with age. You can use the same approach as in the previous sections to fit models, test for significance, and check assumptions.

## Exploratory Data Analysis



## Fitting the ANCOVA Model

Call:

```
lm(formula = pocketdepth ~ age + smoking, data = pockets)
```

Residuals:

Min	1Q	Median	3Q	Max
-1.3995	-0.5308	-0.1453	0.5331	2.2462

Coefficients:

	Estimate	Std. Error	t value	Pr(> t )
(Intercept)	3.89031	0.22660	17.168	< 2e-16 ***
age	0.01776	0.00534	3.326	0.00125 **
smokingSmoker	0.32371	0.17709	1.828	0.07063 .

---

Signif. codes: 0 '\*\*\*' 0.001 '\*\*' 0.01 '\*' 0.05 '.' 0.1 ' ' 1

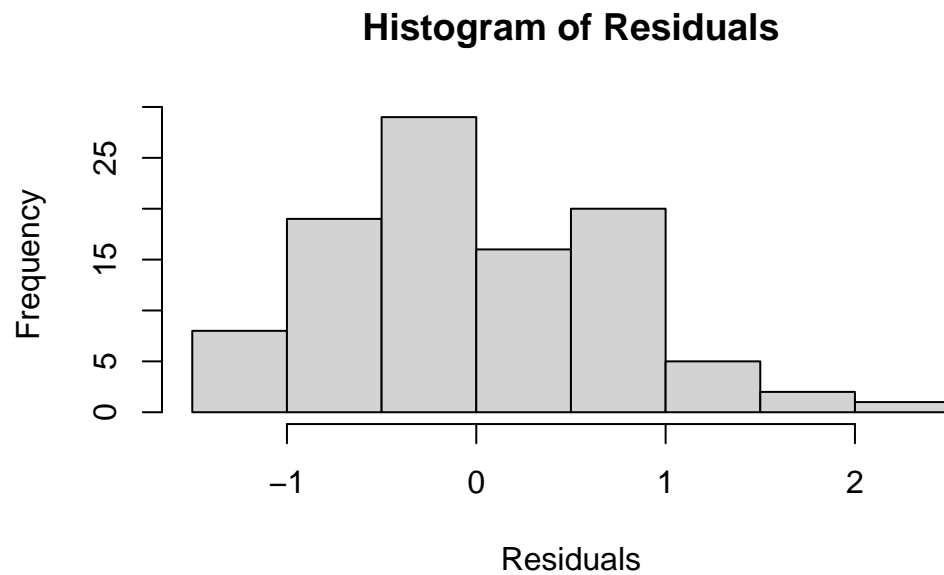
Residual standard error: 0.7447 on 97 degrees of freedom

Multiple R-squared: 0.1669, Adjusted R-squared: 0.1497

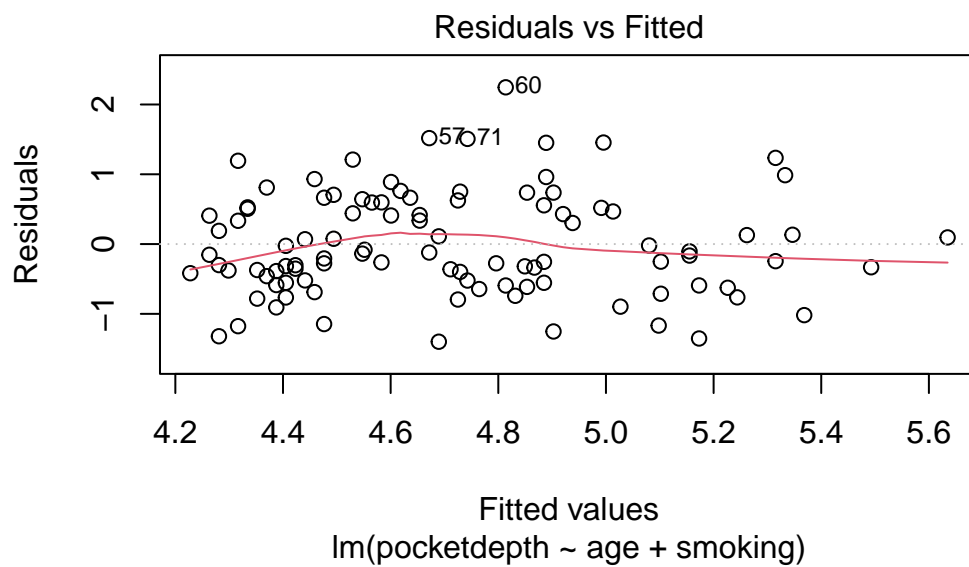
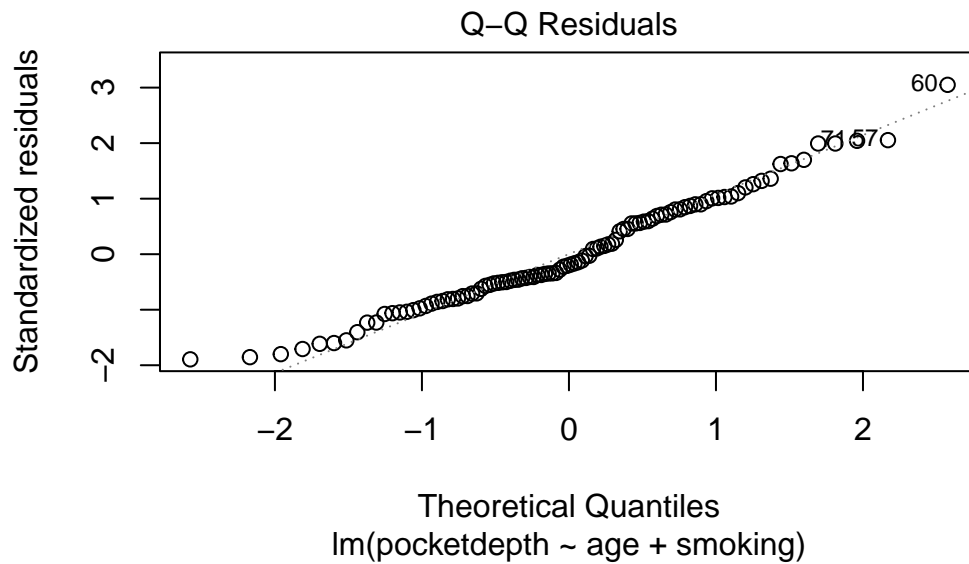
F-statistic: 9.718 on 2 and 97 DF, p-value: 0.0001423

The p-value for the **smoking** variable in the ANOVA table is 0.071, indicating that the **smoking** variable is not significantly associated with **pocketdepth** after accounting for **age**.

### Model Diagnostics







The plots do not show any violations of the normality or homoscedasticity assumptions.

## Fitting the Interaction Model

Call:

```
lm(formula = pocketdepth ~ age * smoking, data = pockets)
```

Residuals:

Min	1Q	Median	3Q	Max
-1.4160	-0.5382	-0.1353	0.5514	2.2096

Coefficients:

	Estimate	Std. Error	t value	Pr(> t )
(Intercept)	3.778052	0.264041	14.309	< 2e-16 ***
age	0.020622	0.006360	3.243	0.00163 **
smokingSmoker	0.772509	0.567866	1.360	0.17690
age:smokingSmoker	-0.009779	0.011755	-0.832	0.40751

---

Signif. codes: 0 '\*\*\*' 0.001 '\*\*' 0.01 '\*' 0.05 '.' 0.1 ' ' 1

Residual standard error: 0.7459 on 96 degrees of freedom

Multiple R-squared: 0.1729, Adjusted R-squared: 0.147

F-statistic: 6.689 on 3 and 96 DF, p-value: 0.0003787

Anova Table (Type III tests)

Response: pocketdepth

	Sum Sq	Df	F value	Pr(>F)
(Intercept)	113.894	1	204.7350	< 2.2e-16 ***
age	5.849	1	10.5145	0.001629 **
smoking	1.029	1	1.8506	0.176898
age:smoking	0.385	1	0.6921	0.407507
Residuals	53.405	96		

---

Signif. codes: 0 '\*\*\*' 0.001 '\*\*' 0.01 '\*' 0.05 '.' 0.1 ' ' 1

The p-value for the interaction term `age:smoking` is 0.407, indicating that there is no significant interaction between `age` and `smoking` in predicting `pocketdepth`.