EXPLORING MODEL KINSHIP FOR MERGING LARGE LANGUAGE MODELS

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ABSTRACT

Model merging has become one of the key technologies for enhancing the capabilities and efficiency of Large Language Models (LLMs). However, our understanding of the expected performance gains and principles when merging any two models remains limited. In this work, we introduce *model kinship*, the degree of similarity or relatedness between LLMs, analogous to **biological evolution**. With comprehensive empirical analysis, we find that there is a certain relationship between model kinship and the performance gains after model merging, which can help guide our selection of candidate models. Inspired by this, we propose a new model merging strategy: Top-k Greedy Merging with Model Kinship, which can yield better performance on benchmark datasets. Specifically, we discover that using model kinship as a criterion can assist us in continuously performing model merging, alleviating the degradation (local optima) in model evolution, whereas model kinship can serve as a guide to escape these traps.

1 INTRODUCTION

Fine-tuning pre-trained models (PTMs) for downstream tasks has become a popular practice, particularly demonstrating significant effectiveness in Large Language Models (LLMs) (Kolesnikov et al., 2020; Qiu et al., 2020; Askell et al., 2021; Ouyang et al., 2022; Zhao et al., 2023). However, deploying separate fine-tuned models for each task can be resource-intensive (Fifty et al., 2021), which drives the increasing demand for multitask learning solutions (Zhang & Yang, 2022; Lu et al., 2024; Liu et al., 2024). Recent studies suggest that model merging (Singh & Jaggi, 2020; Sung et al., 2023; Goddard et al., 2024; Matena & Raffel, 2022; Yang et al., 2024a; Jang et al., 2024) offers a viable approach for achieving multitask objectives by integrating multiple expert models. Furthermore, advancements in model merging toolkits (Goddard et al., 2024; Tang et al., 2024) enable users with limited expertise to easily conduct merging experiments, leading to an evolution of LLMs for the community.

To date, through model merging techniques, researchers have developed many more powerful LLMs through iterative model merging (Beeching et al., 2023), and to some extent, have achieved model evolution (Figure 1(c)). Despite these successes, progress has predominantly relied on trial and error, along with extensive human expertise, but lacks formalized guidance and standardized procedures. As the merging iterations progress, achieving further generalization gains becomes increasingly challenging (More details in Section 3). For example, as shown in Figure 1, model merging often resembles **the process of hybrid evolution in biology**, where the next generation may not show significant improvements or may even regress, highlighting the imperative for a deeper exploration of the underlying mechanisms driving these advancements.

To address this, we introduce *model kinship*, a metric inspired by the concept of kinship (Sahlins, 2013) from evolutionary biology (Figure 1(a)). This metric is designed to estimate the degree of similarity or relatedness between LLMs during the iterative model merging process, providing insights intended to enhance the effectiveness of the merging strategy. We utilize the model kinship to conduct a comprehensive analysis of model merging experiments from two perspectives: the overall merging process, including various independent merge experiments and the evolution path of specific models, demonstrating the complete merging trajectory.

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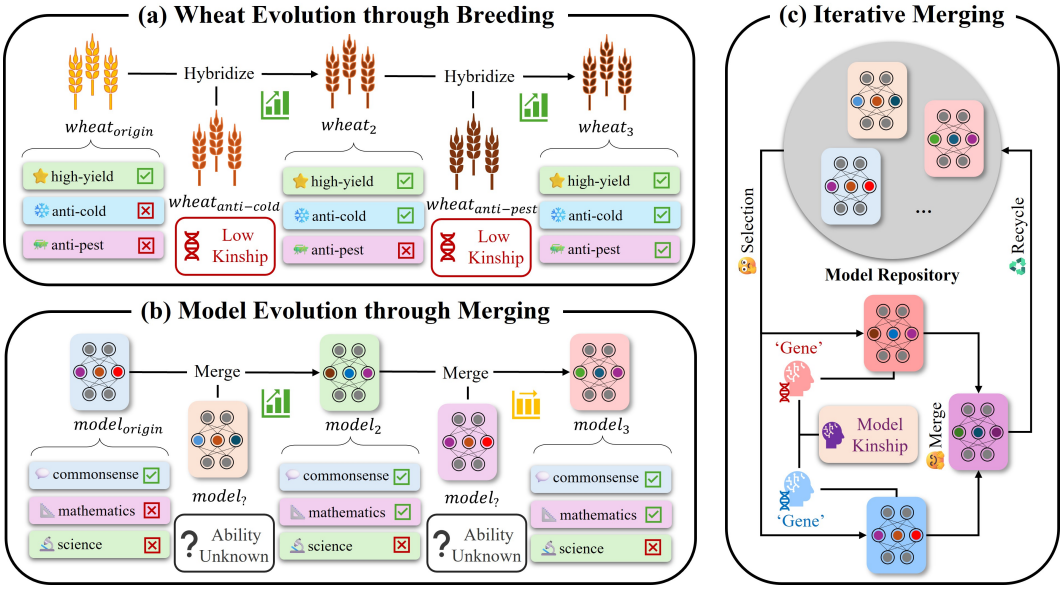

Figure 1: **An intuitive comparison between wheat evolution and model evolution**. An interesting parallel can be drawn between biological reproduction **(Part a)** and the process of model evolution **(Part b)**. In biological systems, offspring inherit genetic material from both parents, forming a new genotype through the combination of parental traits. Similarly, in model merging, the merged model inherits parameters or weights from the contributing models. **Part c** demonstrates the iterative execution of model evolution. Starting with a group of LLMs, the repository evolves through a Selection-Merge-Recycle iteration. Notably, *model kinship* can serve as an effective tool to guide this iterative model merging process (e.g., infer whether there may be gains after model merging.).

Model kinship correlates with average performance gain in model merging. Empirically, we find that there is a strong correlation between variations in multitask capability, estimated by average task performance, and model kinship, which can help guide our selection of candidate models. We also observe that the model merging process consists of two stages: the learning stage, where models experience significant performance improvements, and the saturation stage, where further improvements diminish and eventually stagnate. We think that the stagnation of improvements may be due to convergence in weight space, suggesting the presence of optimization challenges like local optima traps.

Inspired by this, we propose a new model merging strategy: Top-k Greedy Merging with Model Kinship [1]. Specifically, we find that leveraging model kinship as a criterion enables more effective model merging, helping mitigate degradation and avoid local optima during model evolution. Model kinship also proves useful as an early stopping criterion, improving the efficiency of the merging process. In general, this paper makes **three key contributions**:

1. **Introduction of *Model Kinship*:** We introduce model kinship, designed to assess the degree of similarity or relatedness between LLMs during the merging process, which can guide model merging strategies and holds promise for advancing auto-merging research.
2. **Empirical Analysis of Model Evolution:** We present a comprehensive empirical analysis of model evolution through iterative merging. Our findings highlight the dynamics of multitask performance improvement and stagnation. Additionally, we propose a preliminary explanation of the underlying mechanisms using model kinship.
3. **Practical Model Merging Strategies using *Model Kinship*:** We demonstrate how model kinship guides the model merging process to tackle optimization challenges, and provide practical strategies: Top-k Greedy Merging with Model Kinship, to enhance efficiency and effectiveness of model evolution.

[1] Our code is publicly available at https://github.com/zjunlp/MergeEval. Experimental models can be found at https://huggingface.co/zjunlp.

2 BACKGROUND

2.1 MODEL MERGING: FUNDAMENTALS

Model merging aims to integrate two or more domain-specific models into a unified framework, thereby harnessing their composite capabilities across multiple tasks (Sung et al., 2023). While this approach shares conceptual similarities with ensemble methods (Dietterich et al., 2002; Dong et al., 2020; Jiang et al., 2023b), model merging generates a single, generalized model, avoiding the increased inference time associated with ensembles. Let f_i represent the i-th model for merging, each with its unique parameters θ_i. If the merging process follows method $\mathcal{F}$, the prediction $\hat{y}$ of the merged model f_{merge} for input x is:

$$\hat{y} = f_{\text{merge}}(x) = \mathcal{F}\left(f_1(x;\theta_1), f_2(x;\theta_2), \ldots, f_n(x;\theta_n)\right) \tag{1}$$

2.2 ITERATIVE MERGING: EFFECTS AND CHALLENGES

Parameter averaging methods allow the merged model to retain the same architecture and parameter size as the original models, allowing for reuse in future merging processes. By benefiting from this feature, the community iteratively enhances models through repeated applications of model merging, a process we term **"Model Evolution"**. Empirical evidence from the open LLM leaderboard (Beeching et al., 2023) demonstrates that model evolution can produce highly generalized models, often surpassing those created through a single merging step (Maxime Labonne , 2024).

However, one of the main challenges limiting the effectiveness of iterative merging is the merging strategy. The community relies primarily on two approaches: **1) Random Merging:** This intuitive strategy involves merging randomly selected models without considering their task capabilities. The primary advantage of this approach lies in its simplicity and ability to facilitate broad exploration. However, the absence of informed selection often results in high computational costs and may even degrade in capability due to conflicting parameter distributions. **2) Task Capability-Based Merging:** This approach uses task capabilities, as evaluated by benchmarking tools (Gao et al., 2024; Li et al., 2023c), to guide model evolution, compensating for one model's deficiencies by leveraging the strengths of the other. While effective in principle, this strategy heavily relies on human judgment and becomes impractical in complex merging scenarios involving more than two tasks.

Therefore, a problem raised.

Problem: *Is there another strategy or metric we can use to better achieve model evolution?*

2.3 MODEL KINSHIP: CONCEPT AND FORMULATION

In this paper, we are exploring a new approach or metric that can identify differences related to the task between models to maximize the results of merging, without the need for costly evaluations. Drawing inspiration from the parallel between artificial selection and model evolution (as detailed in Appendix H), we hypothesize that a concept analogous to *kinship*, which is central to understanding breeding relationships in evolutionary biology (Thompson, 1985), can be applied. Therefore, we propose the concept of *model kinship*.

Model kinship builds on the cosine similarity analysis introduced in the Task Arithmetic paper (Ilharco et al., 2023). It is designed to evaluate the degree of similarity or relatedness between the task capabilities of large language models (LLMs) solely based on their "genetic" information (i.e., the changes in weights) during model evolution. Considering two models m_i, m_j involved in a model evolution originated from the pre-trained model m_{base}, the weights of m_i, m_j are denoted as $\theta_{\text{i}}, \theta_{\text{j}} \in \mathbb{R}^d$. Similarly, $\theta_{\text{base}} \in \mathbb{R}^d$ represents the weights of the pre-trained model. Since the differences between models emerge after fine-tuning and merging, the variation of weights during model evolution is crucial. It is calculated as:

$$\delta_{\text{i}} = \theta_{\text{i}} - \theta_{\text{base}}, \delta_{\text{j}} = \theta_{\text{j}} - \theta_{\text{base}} \tag{2}$$

Model kinship r is designed to capture the similarity of task capabilities between models. In this paper, we explore multiple potential metrics for evaluating similarity. For the calculation, $sim(\cdot,\cdot)$

denotes the similarity metric function used. Considering two cases merging of 2 models and merging of n models, we formally define model kinship r as:

$$r = \begin{cases} sim(\delta_1, \delta_2), & \text{for merging 2 models} \\ \frac{2}{n(n-1)} \sum_{1 \le i < j \le n} sim(\delta_{\text{i}}, \delta_{\text{j}}), & \text{for merging } n \text{ models} \end{cases} \tag{3}$$

3 Preliminary Analysis of Model Kinship

In this section, we present a preliminary analysis of community merging experiments on LLMs to explore how model kinship can inform and enhance model evolution.

3.1 Evaluation Metrics

Let T be the set of tasks in the task group, where $T = \{T_1, T_2, \ldots, T_n\}$. Each task T_i in the set T is associated with a performance measure P_i for the LLM. For a multitask objective, the Average Task Performance (Avg.) $\bar{P}$ is calculated using the equation:

$$\bar{P} = \frac{1}{n} \sum_{i=1}^{n} P_{\text{i}} \tag{4}$$

To evaluate the effectiveness of a single merge, we propose the merge gain metric. Assume we have two models m_{pre-1} and m_{pre-2} and their average task performance are $\bar{P}_{pre-1}$ and $\bar{P}_{pre-2}$, intuitively, we believe the $\bar{P}_{\text{merged}}$ lie around the mean of $\bar{P}_{pre-1}$ and $\bar{P}_{pre-2}$. The merge gain is calculated as the difference of $\bar{P}_{\text{merged}}$ from the mean value of $\bar{P}_{pre-1}$ and $\bar{P}_{pre-2}$. For a merging recipe with k models, the merge gain is:

$$Gain = \bar{P}_{\text{merged}} - \frac{1}{k} \sum_{i=1}^{k} \bar{P}_{\text{pre-i}} \tag{5}$$

In the following analysis, we use the task group T = {*ARC, HellaSwag, MMLU, TruthfulQA, Winogrande, GSM8K*}. All models are either fine-tuned or merged from the *Mistral-7B* architecture.

3.2 Correlation Analysis of Model Kinship and Performance Gain

Table 1: **Correlation** of Model Kinship based on different correlation function $sim(\cdot, \cdot)$ with Merge Gain, along with their corresponding p-values.

Metric	**Correlation** (Normal Value)	**Correlation (Absolute Value)**
PCC	-0.50	**-0.59**
P-value	0.063	**0.023**
CS	-0.45	**-0.66**
P-value	0.098	**0.008**
ED	0.46	**0.67**
P-value	0.091	**0.007**

In this analysis, we examine the distribution of merge gain and model kinship based on *Pearson Correlation Coefficient (PCC)*, *Cosine Similarity (CS)* and *Euclidean Distance (ED)* in open-sourced LLMs, originating from the *Mistral-7B* (Jiang et al., 2023a). Those models are obtained from the HuggingFace, with assistance from the Open LLM Leaderboard (Details in Appendix B.).

3.2.1 Results

Figure 2 illustrates the distribution of model kinship based on three similarity metrics (PCC, CS, ED) in relation to merge gain. The scatter plots reveal a moderate correlation between model kinship and merge gain, as indicated by the trend lines. To further quantify these relationships, the correlation value (use Pearson Correlation Coefficient) between model kinship and merge gain are calculated, as detailed in the second column of Table 1. While moderate correlations are observed for all three metrics (negative correlation for PCC and CS, and positive correlation for ED), the corresponding p-values indicate a weak level of statistical significance, ranging from 0.05 to 0.1. In contrast, when examining absolute merge gain, we find stronger and statistically significant correlations, as shown in the third column of Table 1. These results suggest that model kinship alone is insufficient to predict whether a model can acquire enhanced generalized performance through

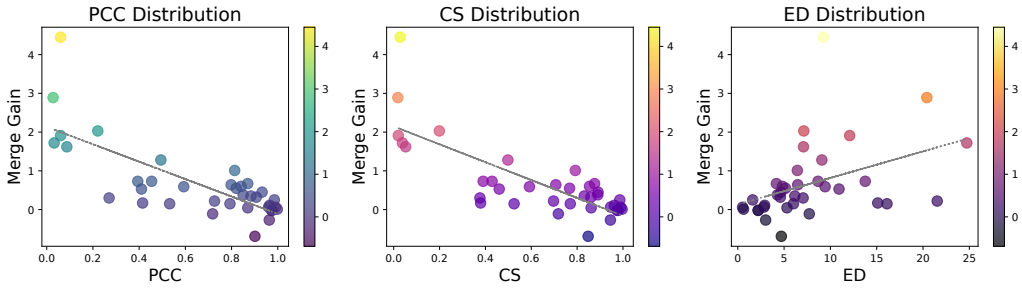

Figure 2: **Distribution of Sample Experiments**: Relationship Between Model Kinship (X-axis) and Merge Gain (Y-axis). Model Kinships are calculated using the Pearson Correlation Coefficient (PCC), Cosine Similarity (CS) and Euclidean Distance (ED).

merging. However, it may serve as a factor in determining the upper limit of merge gains, highlighting the potential outcomes of merging. Since no significant differences are observed among the three metrics, we will focus solely on model kinship based on PCC in the following sections to simplify the demonstration.

3.3 Sequence Analysis of Model Evolution Paths

In this analysis, we examine changes in performance and model kinship across independent model evolution paths to identify the phased pattern of the merging process. We focus on the *yamshadow experiment 28-7B* (Labonne, 2024), a Mistral 7B architecture model ranked as the top 7B merged model on the Open LLM Leaderboard. From its model family tree, we extract two primary merging paths: **Path 1** and **Path 2**.

3.3.1 Results

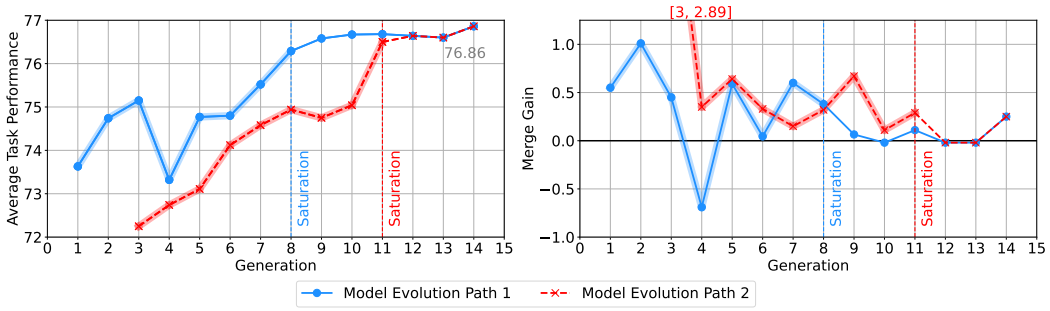

Figure 3: **Change in Average Task Performance and Merge Gain across the Model Evolution process:** The selected paths originate from two distinct initial models, with the saturation stage observed after the vertical line. Note that the generation of Path 2 is aligned with Path 1 for demonstration purposes.

We first focus on the average task performance and merge gains throughout the model evolution path (Figure 3.) Detailed data and branch information are summarized in Appendix B). Our observations indicate that the performance improvements of the iterative merging process are not linear and can be divided into two stages:

- **Learning Stage.** In this stage, the average task performance generally experiences a rapid increase. Noticeable merge gains suggest that the merged models are continually acquiring multitask capabilities through the merging process.
- **Saturation Stage.** As the process continues, improvements begin to plateau. During this stage, the merge gains approach zero, indicating that the model can no longer benefit from the merging process and has ceased to improve.

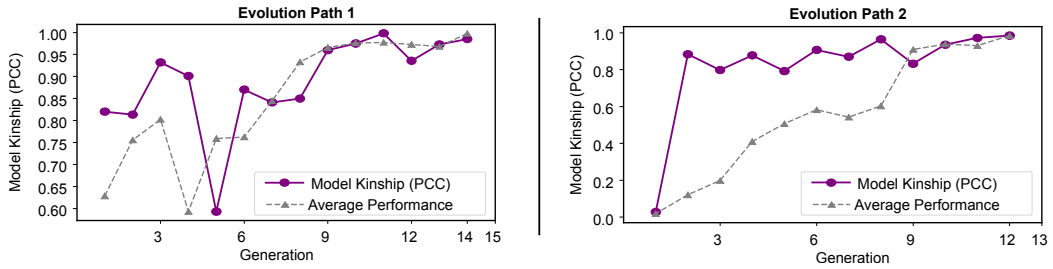

Figure 4: **Comparision** between Model Kinship (measured by Pearson Correlation Coefficient) and Average Task Performance (normalized to the same value scale).

Additionally, we compare the trend of model kinship with average task performance. Figure 4 illustrates the changes in model kinship alongside average task performance (normalized to the same range as the corresponding metric) throughout the model evolution paths. We observe model kinship exhibits a similar stage-specific pattern, particularly evident in the saturation stage, suggesting a potential relationship with the underlying cause of saturation.

3.4 Additional Analysis of the Model Kinship

In this section, we present two additional experiments to further investigate model kinship:

Model Kinship across Different Merging Stages We analyze the evolution of model kinship at various stages of the merging process (a detailed analysis is provided in Appendix D). The results indicate that the findings from Section 3.3 are consistent and can be generalized to the broader model evolution process, which encompasses multiple merging paths.

Task-Relatedness We examine the relationship between task performance and model kinship (a full analysis is available in Appendix E). The results reveal strong correlations, supporting the notion that model kinship is closely tied to task-related differences.

4 Using Model Kinship to Improve Model Merging

Inspired by the above findings, we further leverage the model kinship to enhance the model merging process. We first conduct experiments employing a performance-prior greedy merging strategy. However, as this approach may fall in local optima, we propose a viable alternative: the Top-k Greedy Merging with Model Kinship (Algorithm 1). Experiments are conducted on two architectures. Results from the *Mistral-7B* experiment are highlighted, while details of the *Llama-2* experiment are provided in Appendix I. Our results indicate that while the greedy strategy focuses on short-term gains, it can lead to parameter convergence and suboptimal outcomes. By integrating model kinship, we can help the strategy avoid local optima and gain further improvements.

4.1 Experiment Setup

LLMs. We select three fine-tuned, open-source LLMs based on the *Mistral-7B* architecture from HuggingFace: ***mistral-7b-instruct-v0.2***, ***metamath-mistral-7b***, and ***open-chat-3.5-1210***.

Datasets. Evaluation is conducted using three task-specific benchmark datasets: Winogrande, GSM8k, and TruthfulQA.[2] These benchmarks demonstrate the distinct strengths of the three selected fine-tuned models. Further details on the tasks are provided in Appendix B.3.

[2]The evaluation configurations are as follows: Winogrande (5-shot), GSM8K (5-shot), and TruthfulQA MC2 (0-shot). We utilize the Language Model Evaluation Harness (Gao et al., 2024), a widely adopted framework for testing LLMs.

Algorithm 1 Top k Greedy Merging with Model Kinship.

Require: A set M of n foundation models $\{m_1, m_2, \ldots, m_n\}$, Evaluation function f, Similarity metric function $sim(\cdot, \cdot)$ for model kinship.

1: Generate the first generation of merged models G_1 by merging each pair in set M, and set generation $i = 1$.
2: Combine the set G_1 into set M.
3: Evaluate each model m in set M, and select the top k models. Denote this set as $S = \{m_1, m_2, \ldots, m_k\}$.
4: Initialize a variable $S_{\text{prev}} = \emptyset$ to store the top k models from the previous iteration.
5: **while** $S \neq S_{\text{prev}}$ **do**
6: i++
7: Set $S_{\text{prev}} = S$.
8: Select each model pair from S. Denote this set as $P = \{p_1, p_2, \ldots, p_j\}$.
9: Merge every selected pair in set P as merged model set $G_i = \{m_1, m_2, \ldots, m_j\}$ for generation i, and add each merged model into set M.
10: Identify the current best model $m_{best} \in S$.
11: Identify the model $m_f \in S$ with the lowest model kinship to m_{best} from the G_{i-1} according to the similarity metric $sim(\cdot, \cdot)$.
12: Merge m_f with m_{best} to generate a new model m_{exp}, and add m_{exp} into set G_i and set M.
13: Evaluate each new model $m \in G_i$ using f and update S.
14: Evaluate m_{exp} using f and update S.
15: **end while**

Note: The blue-highlighted steps are only executed in modified experiments incorporating model kinship-based exploration. To distinguish between different models in the subsequent experiments, each model generated in a given generation is named as **model-generation-id**.

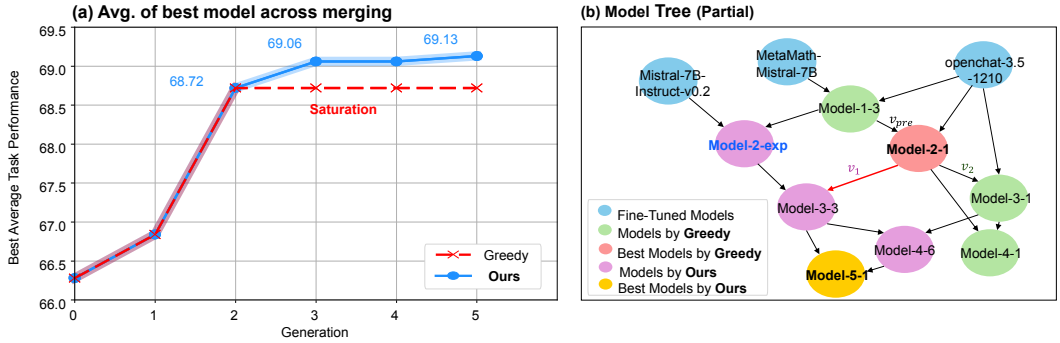

Figure 5: **Left (a)**: The comparison of task performance improvement across merging generations. The **red curve** (greedy strategy) saturates by generation 2, while the **blue curve** (modified strategy) escapes the local optima at generation 2 and continues improving multitask capabilities. **Right (b)**: The partial model family tree from the controled experiments. The **red arrow** shows the critical change between experiment 1 and experiment 2 in the evolution path.

Merging Method. Iterative merging experiments utilize the SLERP (Spherical Linear Interpolation) (Shoemake, 1985) for the single merging step. For implementation, we employ Mergekit (Goddard et al., 2024), a comprehensive toolkit that offers simple access to state-of-the-art model merging techniques.

Top k Greedy Merging. This strategy utilizes the vanilla Top-k Greedy Merging approach on n LLMs (as outlined in the black section of Algorithm 1). This approach has been widely adopted in the community and has demonstrated notable success. In Figure 5 (b), models generated by the greedy strategy are indicated in green, while the best-performing models are highlighted in red.

Top k Greedy Merging with Model Kinship. The proposed strategy simply introduces an additional exploration step, based on model kinship, to the original greedy strategy (highlighted by the

blue part in Algorithm 1). This approach aims to merge the best-performing model with the model that has the most distinct task capabilities, in order to discover potentially better solutions. In Figure 5 (b), models generated by our strategy are marked in purple, while the best-performing models are marked in yellow.

4.2 Results and Discussion

Table 2: Results of merging experiments comparing the vanilla greedy strategy and our proposed approach. The first three models serve as the foundation models in both experiments.**Note**: The model kinship experiment was terminated at generation 5, as it has already outperformed the greedy strategy by that point.

Greedy Strategy				+ Model Kinship			
Model	**Avg.**	**Gain**	**Kinship**	**Model**	**Avg.**	**Gain**	**Kinship**
MetaMath	63.72	/	/	**MetaMath**	63.72	/	/
Instruct	61.82	/	/	**Instruct**	61.82	/	/
Open-chat	66.28	/	/	**Open-chat**	66.28	/	/
model-1-1	62.17	-0.6	0.01	model-1-1	62.17	-0.6	0.01
model-1-2	64.02	-0.03	-0.02	model-1-2	64.02	-0.03	-0.02
model-1-3	66.84	+1.84	0.05	model-1-3	66.84	+1.84	0.05
model-2-1	**68.72**	**+2.16**	**0.93**	model-2-1	68.72	**+2.16**	0.93
model-2-2	61.47	-3.96	0.57	model-2-2	61.47	-3.96	0.57
model-2-3	61.32	-3.83	0.58	model-2-3	61.32	-3.83	0.58
model-3-1	68.59	+1.09	0.95	model-3-2	67.74	+1.09	0.93
model-3-2	67.74	-0.04	0.93	model-3-3	69.06	+0.74	0.24
	-	-	-	model-3-4	68.61	+1.13	0.32
model-4-1	68.51	-0.14	0.98	model-4-4	68.75	-0.14	0.54
model-4-2	68.04	-0.19	0.98	model-4-5	68.39	-0.27	0.66
model-4-3	68.53	+0.37	0.94	model-4-6	69.03	+0.15	0.52
	-	-	-	**model-5-1**	**69.13**	**+0.04**	**0.65**
	-	-	-	model-5-2	68.98	+0.07	0.65
	-	-	-	model-5-3	68.63	-0.37	0.98

Figure 5 (a) illustrates the improvements in top average task performance across merging generations. Table 2 provides the model average task performance, merge gain, and model kinship for each generation, comparing the original greedy merging strategy with our kinship-based method. Both strategies achieve the multitask goals. However, the *vanilla greedy strategy* stops improving after Generation 2, stabilizing at an average task performance of **68.72**. In contrast, Experiment 2, utilizing model kinship-based exploration, escapes the local optima (Model-2-1) and continues to improve, reaching **69.13** by Generation 5.

Merging Models with Low Kinship can Boost Exploration. Figure 5 (b) highlights the key branch of the model family tree. To investigate how merging models with low kinship helps escape local optima traps observed during the saturation stage, we focus on the bifurcation point and analyze the weight changes: v_1 (from *Model-2-1* to *Model-3-1*) and v_2 (from *Model-2-1* to *Model-3-3*) in two separate experiments. The previous weight change, v_{pre} (from *Model-1-3* to *Model-2-1*), serves as a baseline. Figure 6 reveals that merging with the exploration model resulted in significant weight changes in a distinct direction, introducing novel variations into the weight space. In contrast, v_1 shows minimal weight change, as the merging effect is reduced due to the high similarity between the weights of *openchat-3.5* and *Model-2-1*.

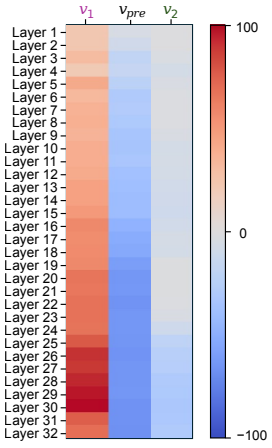

Figure 6: **Weight Change**.

Early Stopping at High Kinship can Improve Efficiency. The iterative merging process can be resource-intensive. Based on observations from community experiments, **5 out of 14** merges in evolution path 1 resulted in an average improvement of just **0.57**, while **3 out of 12** merges in evolution Path 2 yields an average improvement of **0.36**. In our own experiments, applying a greedy strategy to a simple task lead to saturation after **2 out of 4** merges, with no further gains. We find that the model kinship may serve as an effective early stopping signal. When the merging process converges, the model kinship between top-performing models is typically high (e.g., exceeding **0.9** based on PCC). **Halting the merging process at this stage improves the efficiency of time by approximately 30%**, with little to no performance reduction.

5 Related work

Weight averaging is one of the most widely used techniques in model merging, with its origins traced back to Utans (1996). Since the 2010s, weight averaging has found numerous applications in deep neural networks, including combining checkpoints to enhance the training process (Nagarajan & Kolter, 2019; Tarvainen & Valpola, 2017; Izmailov et al., 2018; Li et al., 2023b; Stoica et al., 2023; Padmanabhan et al., 2023; Jang et al., 2023), leveraging task-specific information (Li et al., 2023a; Smith & Gashler, 2017; Ilharco et al., 2022; Izmailov et al., 2018), and parallel training of large language models (LLMs) (Li et al., 2022). Discovery of Linear Mode Connectivity (LMC) (Garipov et al., 2018; Frankle et al., 2020; Entezari et al., 2022) further expands the use of weight averaging in fusing fine-tuned models through averaging methods (Neyshabur et al., 2020; Wortsman et al., 2022). Further studies have explored optimizable weights for merging, such as Fisher-Merging (Matena & Raffel, 2022), RegMean (Jin et al., 2023), AdaMerging (Yang et al., 2024b), MaTS (Tam et al., 2024). Ilharco et al. (2023) introduce task vectors, representing the weight difference between a fine-tuned model and its base. Further research on parameter interference led to TIES (Yadav et al., 2023), which preserves important weights and reduces sign conflicts, and DARE (Yu et al., 2024), which prevents interference by randomly dropping weights. The Model Breadcrumbs (Davari & Belilovsky, 2023) show that the removal of outliers in parameters can reduce noise in model merging. Merging models with different initializations requires additional considerations. Common methods exploit the permutation symmetry of neural networks (Ainsworth et al., 2022; Tatro et al., 2020; Singh & Jaggi, 2020; Guerrero-Peña et al., 2023), using alignment techniques to mitigate the interpolation barrier (Xu et al., 2024; Navon et al., 2024). While weight averaging cannot be directly applied to models with different architectures, it can still be used to enhance feasible fusion methods. Recent work, such as FuseChat (Wan et al., 2024b), combines weight averaging with Knowledge Fusion (Wan et al., 2024a) to develop innovative fusion techniques.

Recently, there have been some works exploring "model evolution". Tellamekala et al. (2024) propose the CoLD Fusion method, showing that iterative fusion can create effective multitask models. Labonne (2024) develop a tool to automatically merge models on Hugging Face. Akiba et al. (2024) introduce Evolutionary Model Merge, employing evolutionary techniques to optimize model combinations.

6 Conclusion

In this paper, we introduce model kinship, the degree of relatedness between LLMs which can help guide our selection of candidate models for merging. We conduct comprehensive experiments to demonstrate its effectiveness in understanding the model evolution process. We further propose a new model merging strategy: Top-k Greedy Merging with Model Kinship. We show that model kinship plays a crucial role in model evolution by guiding the process to escape local optima traps (in saturation stage), enabling further improvements. Additionally, we demonstrate that model kinship can detect the onset of convergence, allowing for early stopping and reducing the waste of computational resources in the merging process.

In a broad sense, our work explores how models can achieve autonomous evolution through model merging. Model merging can, to some extent, be likened to biological hybridization. Biological organisms have undergone billions of years of evolution to reach their current state. However, how silicon-based intelligence, represented by LLMs, evolves remains an unresolved mystery. We aspire that this work offer guidance and insights for the future merging and evolution of LLMs.

Reproducibility Statement

The experimental setup can be found in Section 4.1. All model checkpoints are available on HuggingFace, with detailed information provided in Appendices B.

References

Samuel K. Ainsworth, Jonathan Hayase, and Siddhartha S. Srinivasa. Git re-basin: Merging models modulo permutation symmetries. *CoRR*, abs/2209.04836, 2022. doi: 10.48550/ARXIV.2209.04836. URL https://doi.org/10.48550/arXiv.2209.04836.

Takuya Akiba, Makoto Shing, Yujin Tang, Qi Sun, and David Ha. Evolutionary optimization of model merging recipes. *CoRR*, abs/2403.13187, 2024. doi: 10.48550/ARXIV.2403.13187. URL https://doi.org/10.48550/arXiv.2403.13187.

Amanda Askell, Yuntao Bai, Anna Chen, Dawn Drain, Deep Ganguli, Tom Henighan, Andy Jones, Nicholas Joseph, Benjamin Mann, Nova DasSarma, Nelson Elhage, Zac Hatfield-Dodds, Danny Hernandez, Jackson Kernion, Kamal Ndousse, Catherine Olsson, Dario Amodei, Tom B. Brown, Jack Clark, Sam McCandlish, Chris Olah, and Jared Kaplan. A general language assistant as a laboratory for alignment. *CoRR*, abs/2112.00861, 2021. URL https://arxiv.org/abs/2112.00861.

Edward Beeching, Clémentine Fourrier, Nathan Habib, Sheon Han, Nathan Lambert, Nazneen Rajani, Omar Sanseviero, Lewis Tunstall, and Thomas Wolf. Open llm leaderboard. https://huggingface.co/spaces/open-llm-leaderboard-old/open_llm_leaderboard, 2023.

MohammadReza Davari and Eugene Belilovsky. Model breadcrumbs: Scaling multi-task model merging with sparse masks. *CoRR*, abs/2312.06795, 2023. doi: 10.48550/ARXIV.2312.06795. URL https://doi.org/10.48550/arXiv.2312.06795.

Thomas G Dietterich et al. Ensemble learning. *The handbook of brain theory and neural networks*, 2(1):110–125, 2002.

Xibin Dong, Zhiwen Yu, Wenming Cao, Yifan Shi, and Qianli Ma. A survey on ensemble learning. *Frontiers Comput. Sci.*, 14(2):241–258, 2020. doi: 10.1007/S11704-019-8208-Z. URL https://doi.org/10.1007/s11704-019-8208-z.

Rahim Entezari, Hanie Sedghi, Olga Saukh, and Behnam Neyshabur. The role of permutation invariance in linear mode connectivity of neural networks. In *The Tenth International Conference on Learning Representations, ICLR 2022, Virtual Event, April 25-29, 2022*. OpenReview.net, 2022. URL https://openreview.net/forum?id=dNigytemkL.

Chris Fifty, Ehsan Amid, Zhe Zhao, Tianhe Yu, Rohan Anil, and Chelsea Finn. Efficiently identifying task groupings for multi-task learning. In Marc'Aurelio Ranzato, Alina Beygelzimer, Yann N. Dauphin, Percy Liang, and Jennifer Wortman Vaughan (eds.), *Advances in Neural Information Processing Systems 34: Annual Conference on Neural Information Processing Systems 2021, NeurIPS 2021, December 6-14, 2021, virtual*, pp. 27503–27516, 2021. URL https://proceedings.neurips.cc/paper/2021/hash/e77910ebb93b511588557806310f78f1-Abstract.html.

Jonathan Frankle, Gintare Karolina Dziugaite, Daniel M. Roy, and Michael Carbin. Linear mode connectivity and the lottery ticket hypothesis. In *Proceedings of the 37th International Conference on Machine Learning, ICML 2020, 13-18 July 2020, Virtual Event*, volume 119 of *Proceedings of Machine Learning Research*, pp. 3259–3269. PMLR, 2020. URL http://proceedings.mlr.press/v119/frankle20a.html.

Leo Gao, Jonathan Tow, Baber Abbasi, Stella Biderman, Sid Black, Anthony DiPofi, Charles Foster, Laurence Golding, Jeffrey Hsu, Alain Le Noac'h, Haonan Li, Kyle McDonell, Niklas Muennighoff, Chris Ociepa, Jason Phang, Laria Reynolds, Hailey Schoelkopf, Aviya Skowron, Lintang Sutawika, Eric Tang, Anish Thite, Ben Wang, Kevin Wang, and Andy Zou. A framework for few-shot language model evaluation, 07 2024. URL https://zenodo.org/records/12608602.

Timur Garipov, Pavel Izmailov, Dmitrii Podoprikhin, Dmitry P. Vetrov, and Andrew Gordon Wilson. Loss surfaces, mode connectivity, and fast ensembling of dnns. In Samy Bengio, Hanna M. Wallach, Hugo Larochelle, Kristen Grauman, Nicolò Cesa-Bianchi, and Roman Garnett (eds.), *Advances in Neural Information Processing Systems 31: Annual Conference on Neural Information Processing Systems 2018, NeurIPS 2018, December 3-8, 2018, Montréal, Canada*, pp. 8803–8812, 2018. URL https://proceedings.neurips.cc/paper/2018/hash/be3087e74e9100d4bc4c6268cdbe8456-Abstract.html.

Charles Goddard, Shamane Siriwardhana, Malikeh Ehghaghi, Luke Meyers, Vlad Karpukhin, Brian Benedict, Mark McQuade, and Jacob Solawetz. Arcee's mergekit: A toolkit for merging large language models. *CoRR*, abs/2403.13257, 2024. doi: 10.48550/ARXIV.2403.13257. URL https://doi.org/10.48550/arXiv.2403.13257.

Albert Gu and Tri Dao. Mamba: Linear-time sequence modeling with selective state spaces. *CoRR*, abs/2312.00752, 2023. doi: 10.48550/ARXIV.2312.00752. URL https://doi.org/10.48550/arXiv.2312.00752.

Fidel A. Guerrero-Peña, Heitor Rapela Medeiros, Thomas Dubail, Masih Aminbeidokhti, Eric Granger, and Marco Pedersoli. Re-basin via implicit sinkhorn differentiation. In *IEEE/CVF Conference on Computer Vision and Pattern Recognition, CVPR 2023, Vancouver, BC, Canada, June 17-24, 2023*, pp. 20237–20246. IEEE, 2023. doi: 10.1109/CVPR52729.2023.01938. URL https://doi.org/10.1109/CVPR52729.2023.01938.

Gabriel Ilharco, Mitchell Wortsman, Samir Yitzhak Gadre, Shuran Song, Hannaneh Hajishirzi, Simon Kornblith, Ali Farhadi, and Ludwig Schmidt. Patching open-vocabulary models by interpolating weights. In Sanmi Koyejo, S. Mohamed, A. Agarwal, Danielle Belgrave, K. Cho, and A. Oh (eds.), *Advances in Neural Information Processing Systems 35: Annual Conference on Neural Information Processing Systems 2022, NeurIPS 2022, New Orleans, LA, USA, November 28 - December 9, 2022*, 2022. URL http://papers.nips.cc/paper_files/paper/2022/hash/bc6cddcd5d325e1c0f826066c1ad0215-Abstract-Conference.html.

Gabriel Ilharco, Marco Túlio Ribeiro, Mitchell Wortsman, Ludwig Schmidt, Hannaneh Hajishirzi, and Ali Farhadi. Editing models with task arithmetic. In *The Eleventh International Conference on Learning Representations, ICLR 2023, Kigali, Rwanda, May 1-5, 2023*. OpenReview.net, 2023. URL https://openreview.net/forum?id=6t0Kwf8-jrj.

Pavel Izmailov, Dmitrii Podoprikhin, Timur Garipov, Dmitry P. Vetrov, and Andrew Gordon Wilson. Averaging weights leads to wider optima and better generalization. In Amir Globerson and Ricardo Silva (eds.), *Proceedings of the Thirty-Fourth Conference on Uncertainty in Artificial Intelligence, UAI 2018, Monterey, California, USA, August 6-10, 2018*, pp. 876–885. AUAI Press, 2018. URL http://auai.org/uai2018/proceedings/papers/313.pdf.

Dong-Hwan Jang, Sangdoo Yun, and Dongyoon Han. Model stock: All we need is just a few fine-tuned models. In Ales Leonardis, Elisa Ricci, Stefan Roth, Olga Russakovsky, Torsten Sattler, and Gül Varol (eds.), *Computer Vision - ECCV 2024 - 18th European Conference, Milan, Italy, September 29-October 4, 2024, Proceedings, Part XLIV*, volume 15102 of *Lecture Notes in Computer Science*, pp. 207–223. Springer, 2024. doi: 10.1007/978-3-031-72784-9_12. URL https://doi.org/10.1007/978-3-031-72784-9_12.

Joel Jang, Seungone Kim, Bill Yuchen Lin, Yizhong Wang, Jack Hessel, Luke Zettlemoyer, Hannaneh Hajishirzi, Yejin Choi, and Prithviraj Ammanabrolu. Personalized soups: Personalized large language model alignment via post-hoc parameter merging. *arXiv preprint arXiv:2310.11564*, 2023.

Albert Q. Jiang, Alexandre Sablayrolles, Arthur Mensch, Chris Bamford, Devendra Singh Chaplot, Diego de Las Casas, Florian Bressand, Gianna Lengyel, Guillaume Lample, Lucile Saulnier, Lélio Renard Lavaud, Marie-Anne Lachaux, Pierre Stock, Teven Le Scao, Thibaut Lavril, Thomas Wang, Timothée Lacroix, and William El Sayed. Mistral 7b. *CoRR*, abs/2310.06825, 2023a. doi: 10.48550/ARXIV.2310.06825. URL https://doi.org/10.48550/arXiv.2310.06825.

Dongfu Jiang, Xiang Ren, and Bill Yuchen Lin. Llm-blender: Ensembling large language models with pairwise ranking and generative fusion. In Anna Rogers, Jordan L. Boyd-Graber, and Naoaki Okazaki (eds.), *Proceedings of the 61st Annual Meeting of the Association for Computational Linguistics (Volume 1: Long Papers), ACL 2023, Toronto, Canada, July 9-14, 2023*, pp. 14165–14178. Association for Computational Linguistics, 2023b. doi: 10.18653/V1/2023.ACL-LONG.792. URL https://doi.org/10.18653/v1/2023.acl-long.792.

Xisen Jin, Xiang Ren, Daniel Preotiuc-Pietro, and Pengxiang Cheng. Dataless knowledge fusion by merging weights of language models. In *The Eleventh International Conference on Learning Representations, ICLR 2023, Kigali, Rwanda, May 1-5, 2023*. OpenReview.net, 2023. URL https://openreview.net/forum?id=FCnohuR6AnM.

Alexander Kolesnikov, Lucas Beyer, Xiaohua Zhai, Joan Puigcerver, Jessica Yung, Sylvain Gelly, and Neil Houlsby. Big transfer (bit): General visual representation learning. In Andrea Vedaldi, Horst Bischof, Thomas Brox, and Jan-Michael Frahm (eds.), *Computer Vision - ECCV 2020 - 16th European Conference, Glasgow, UK, August 23-28, 2020, Proceedings, Part V*, volume 12350 of *Lecture Notes in Computer Science*, pp. 491–507. Springer, 2020. doi: 10.1007/978-3-030-58558-7_29. URL https://doi.org/10.1007/978-3-030-58558-7_29.

Maxime Labonne. Automerger experiments, 2024. URL https://huggingface.co/automerger.

Margaret Li, Suchin Gururangan, Tim Dettmers, Mike Lewis, Tim Althoff, Noah A. Smith, and Luke Zettlemoyer. Branch-train-merge: Embarrassingly parallel training of expert language models. *CoRR*, abs/2208.03306, 2022. doi: 10.48550/ARXIV.2208.03306. URL https://doi.org/10.48550/arXiv.2208.03306.

Weishi Li, Yong Peng, Miao Zhang, Liang Ding, Han Hu, and Li Shen. Deep model fusion: A survey. *CoRR*, abs/2309.15698, 2023a. doi: 10.48550/ARXIV.2309.15698. URL https://doi.org/10.48550/arXiv.2309.15698.

Weishi Li, Yong Peng, Miao Zhang, Liang Ding, Han Hu, and Li Shen. Deep model fusion: A survey. *arXiv preprint arXiv:2309.15698*, 2023b.

Xuechen Li, Tianyi Zhang, Yann Dubois, Rohan Taori, Ishaan Gulrajani, Carlos Guestrin, Percy Liang, and Tatsunori B. Hashimoto. Alpacaeval: An automatic evaluator of instruction-following models. https://github.com/tatsu-lab/alpaca_eval, 5 2023c.

Cong Liu, Xiaojun Quan, Yan Pan, Liang Li, Weigang Wu, and Xu Chen. Cool-fusion: Fuse large language models without training. *CoRR*, abs/2407.19807, 2024. doi: 10.48550/ARXIV.2407.19807. URL https://doi.org/10.48550/arXiv.2407.19807.

Jinliang Lu, Ziliang Pang, Min Xiao, Yaochen Zhu, Rui Xia, and Jiajun Zhang. Merge, ensemble, and cooperate! A survey on collaborative strategies in the era of large language models. *CoRR*, abs/2407.06089, 2024. doi: 10.48550/ARXIV.2407.06089. URL https://doi.org/10.48550/arXiv.2407.06089.

Michael Matena and Colin Raffel. Merging models with fisher-weighted averaging. In Sanmi Koyejo, S. Mohamed, A. Agarwal, Danielle Belgrave, K. Cho, and A. Oh (eds.), *Advances in Neural Information Processing Systems 35: Annual Conference on Neural Information Processing Systems 2022, NeurIPS 2022, New Orleans, LA, USA, November 28 - December 9, 2022*, 2022. URL http://papers.nips.cc/paper_files/paper/2022/hash/70c26937fbf3d4600b69a129031b66ec-Abstract-Conference.html.

Maxime Labonne . Yamshadowexperiment28-7b, 2024. URL https://huggingface.co/automerger/YamshadowExperiment28-7B.

Vaishnavh Nagarajan and J. Zico Kolter. Uniform convergence may be unable to explain generalization in deep learning. In Hanna M. Wallach, Hugo Larochelle, Alina Beygelzimer, Florence d'Alché-Buc, Emily B. Fox, and Roman Garnett (eds.), *Advances in Neural Information Processing Systems 32: Annual Conference on Neural Information Processing Systems 2019, NeurIPS 2019, December 8-14, 2019, Vancouver, BC, Canada*,

pp. 11611–11622, 2019. URL https://proceedings.neurips.cc/paper/2019/hash/05e97c207235d63ceb1db43c60db7bbb-Abstract.html.

Aviv Navon, Aviv Shamsian, Ethan Fetaya, Gal Chechik, Nadav Dym, and Haggai Maron. Equivariant deep weight space alignment. In *Forty-first International Conference on Machine Learning, ICML 2024, Vienna, Austria, July 21-27, 2024*. OpenReview.net, 2024. URL https://openreview.net/forum?id=nBPnmk6EeO.

Behnam Neyshabur, Hanie Sedghi, and Chiyuan Zhang. What is being transferred in transfer learning? In Hugo Larochelle, Marc'Aurelio Ranzato, Raia Hadsell, Maria-Florina Balcan, and Hsuan-Tien Lin (eds.), *Advances in Neural Information Processing Systems 33: Annual Conference on Neural Information Processing Systems 2020, NeurIPS 2020, December 6-12, 2020, virtual*, 2020. URL https://proceedings.neurips.cc/paper/2020/hash/0607f4c705595b911a4f3e7a127b44e0-Abstract.html.

Long Ouyang, Jeffrey Wu, Xu Jiang, Diogo Almeida, Carroll L. Wainwright, Pamela Mishkin, Chong Zhang, Sandhini Agarwal, Katarina Slama, Alex Ray, John Schulman, Jacob Hilton, Fraser Kelton, Luke Miller, Maddie Simens, Amanda Askell, Peter Welinder, Paul F. Christiano, Jan Leike, and Ryan Lowe. Training language models to follow instructions with human feedback. In Sanmi Koyejo, S. Mohamed, A. Agarwal, Danielle Belgrave, K. Cho, and A. Oh (eds.), *Advances in Neural Information Processing Systems 35: Annual Conference on Neural Information Processing Systems 2022, NeurIPS 2022, New Orleans, LA, USA, November 28 - December 9, 2022*, 2022. URL http://papers.nips.cc/paper_files/paper/2022/hash/b1efde53be364a73914f58805a001731-Abstract-Conference.html.

Arthi Padmanabhan, Neil Agarwal, Anand Iyer, Ganesh Ananthanarayanan, Yuanchao Shu, Nikolaos Karianakis, Guoqing Harry Xu, and Ravi Netravali. Gemel: Model merging for {Memory-Efficient},{Real-Time} video analytics at the edge. In *20th USENIX Symposium on Networked Systems Design and Implementation (NSDI 23)*, pp. 973–994, 2023.

Xipeng Qiu, Tianxiang Sun, Yige Xu, Yunfan Shao, Ning Dai, and Xuanjing Huang. Pre-trained models for natural language processing: A survey. *CoRR*, abs/2003.08271, 2020. URL https://arxiv.org/abs/2003.08271.

Marshall Sahlins. *What kinship is-and is not*. University of Chicago Press, 2013.

Ken Shoemake. Animating rotation with quaternion curves. In Pat Cole, Robert Heilman, and Brian A. Barsky (eds.), *Proceedings of the 12th Annual Conference on Computer Graphics and Interactive Techniques, SIGGRAPH 1985, San Francisco, California, USA, July 22-26, 1985*, pp. 245–254. ACM, 1985. doi: 10.1145/325334.325242. URL https://doi.org/10.1145/325334.325242.

David Silver, Satinder Singh, Doina Precup, and Richard S Sutton. Reward is enough. *Artificial Intelligence*, 299:103535, 2021.

Sidak Pal Singh and Martin Jaggi. Model fusion via optimal transport. In Hugo Larochelle, Marc'Aurelio Ranzato, Raia Hadsell, Maria-Florina Balcan, and Hsuan-Tien Lin (eds.), *Advances in Neural Information Processing Systems 33: Annual Conference on Neural Information Processing Systems 2020, NeurIPS 2020, December 6-12, 2020, virtual*, 2020. URL https://proceedings.neurips.cc/paper/2020/hash/fb2697869f56484404c8ceee2985b01d-Abstract.html.

Joshua Smith and Michael Gashler. An investigation of how neural networks learn from the experiences of peers through periodic weight averaging. In Xuewen Chen, Bo Luo, Feng Luo, Vasile Palade, and M. Arif Wani (eds.), *16th IEEE International Conference on Machine Learning and Applications, ICMLA 2017, Cancun, Mexico, December 18-21, 2017*, pp. 731–736. IEEE, 2017. doi: 10.1109/ICMLA.2017.00-72. URL https://doi.org/10.1109/ICMLA.2017.00-72.

George Stoica, Daniel Bolya, Jakob Bjorner, Pratik Ramesh, Taylor Hearn, and Judy Hoffman. Zipit! merging models from different tasks without training. *arXiv preprint arXiv:2305.03053*, 2023.

Yi-Lin Sung, Linjie Li, Kevin Lin, Zhe Gan, Mohit Bansal, and Lijuan Wang. An empirical study of multimodal model merging. In Houda Bouamor, Juan Pino, and Kalika Bali (eds.), *Findings of the Association for Computational Linguistics: EMNLP 2023, Singapore, December 6-10, 2023*, pp. 1563–1575. Association for Computational Linguistics, 2023. doi: 10.18653/V1/2023.FINDINGS-EMNLP.105. URL https://doi.org/10.18653/v1/2023.findings-emnlp.105.

Derek Tam, Mohit Bansal, and Colin Raffel. Merging by matching models in task parameter subspaces. *Trans. Mach. Learn. Res.*, 2024, 2024. URL https://openreview.net/forum?id=qNGo6ghWFB.

Anke Tang, Li Shen, Yong Luo, Han Hu, Bo Du, and Dacheng Tao. Fusionbench: A comprehensive benchmark of deep model fusion. *CoRR*, abs/2406.03280, 2024. doi: 10.48550/ARXIV.2406.03280. URL https://doi.org/10.48550/arXiv.2406.03280.

Antti Tarvainen and Harri Valpola. Mean teachers are better role models: Weight-averaged consistency targets improve semi-supervised deep learning results. In *5th International Conference on Learning Representations, ICLR 2017, Toulon, France, April 24-26, 2017, Workshop Track Proceedings*. OpenReview.net, 2017. URL https://openreview.net/forum?id=ry8u21rtl.

N. Joseph Tatro, Pin-Yu Chen, Payel Das, Igor Melnyk, Prasanna Sattigeri, and Rongjie Lai. Optimizing mode connectivity via neuron alignment. In Hugo Larochelle, Marc'Aurelio Ranzato, Raia Hadsell, Maria-Florina Balcan, and Hsuan-Tien Lin (eds.), *Advances in Neural Information Processing Systems 33: Annual Conference on Neural Information Processing Systems 2020, NeurIPS 2020, December 6-12, 2020, virtual*, 2020. URL https://proceedings.neurips.cc/paper/2020/hash/aecad42329922dfc97eee948606e1f8e-Abstract.html.

Mani Kumar Tellamekala, Shahin Amiriparian, Björn W. Schuller, Elisabeth André, Timo Giesbrecht, and Michel F. Valstar. COLD fusion: Calibrated and ordinal latent distribution fusion for uncertainty-aware multimodal emotion recognition. *IEEE Trans. Pattern Anal. Mach. Intell.*, 46(2):805–822, 2024. doi: 10.1109/TPAMI.2023.3325770. URL https://doi.org/10.1109/TPAMI.2023.3325770.

Professor Elizabeth A. Thompson. *Pedigree Analysis in Human Genetics*. Johns Hopkins University Press, Baltimore, 1985.

Joachim Utans. Weight averaging for neural networks and local resampling schemes. In *Proc. AAAI-96 Workshop on Integrating Multiple Learned Models*, pp. AAAI Press. Citeseer, 1996.

Fanqi Wan, Xinting Huang, Deng Cai, Xiaojun Quan, Wei Bi, and Shuming Shi. Knowledge fusion of large language models. In *The Twelfth International Conference on Learning Representations, ICLR 2024, Vienna, Austria, May 7-11, 2024*. OpenReview.net, 2024a. URL https://openreview.net/forum?id=jiDsk12qcz.

Fanqi Wan, Ziyi Yang, Longguang Zhong, Xiaojun Quan, Xinting Huang, and Wei Bi. Fusechat: Knowledge fusion of chat models. *CoRR*, abs/2402.16107, 2024b. doi: 10.48550/ARXIV.2402.16107. URL https://doi.org/10.48550/arXiv.2402.16107.

Mitchell Wortsman, Gabriel Ilharco, Samir Yitzhak Gadre, Rebecca Roelofs, Raphael Gontijo Lopes, Ari S. Morcos, Hongseok Namkoong, Ali Farhadi, Yair Carmon, Simon Kornblith, and Ludwig Schmidt. Model soups: averaging weights of multiple fine-tuned models improves accuracy without increasing inference time. In Kamalika Chaudhuri, Stefanie Jegelka, Le Song, Csaba Szepesvári, Gang Niu, and Sivan Sabato (eds.), *International Conference on Machine Learning, ICML 2022, 17-23 July 2022, Baltimore, Maryland, USA*, volume 162 of *Proceedings of Machine Learning Research*, pp. 23965–23998. PMLR, 2022. URL https://proceedings.mlr.press/v162/wortsman22a.html.

Zhengqi Xu, Ke Yuan, Huiqiong Wang, Yong Wang, Mingli Song, and Jie Song. Training-free pretrained model merging. *CoRR*, abs/2403.01753, 2024. doi: 10.48550/ARXIV.2403.01753. URL https://doi.org/10.48550/arXiv.2403.01753.

Prateek Yadav, Derek Tam, Leshem Choshen, Colin A. Raffel, and Mohit Bansal. Ties-merging: Resolving interference when merging models. In Alice Oh, Tristan Naumann, Amir Globerson, Kate Saenko, Moritz Hardt, and Sergey Levine (eds.), *Advances in Neural Information Processing Systems 36: Annual Conference on Neural Information Processing Systems 2023, NeurIPS 2023, New Orleans, LA, USA, December 10 - 16, 2023*, 2023. URL http://papers.nips.cc/paper_files/paper/2023/hash/1644c9af28ab7916874f6fd6228a9bcf-Abstract-Conference.html.

Enneng Yang, Li Shen, Guibing Guo, Xingwei Wang, Xiaochun Cao, Jie Zhang, and Dacheng Tao. Model merging in llms, mllms, and beyond: Methods, theories, applications and opportunities. *CoRR*, abs/2408.07666, 2024a. doi: 10.48550/ARXIV.2408.07666. URL https://doi.org/10.48550/arXiv.2408.07666.

Enneng Yang, Zhenyi Wang, Li Shen, Shiwei Liu, Guibing Guo, Xingwei Wang, and Dacheng Tao. Adamerging: Adaptive model merging for multi-task learning. In *The Twelfth International Conference on Learning Representations, ICLR 2024, Vienna, Austria, May 7-11, 2024*. OpenReview.net, 2024b. URL https://openreview.net/forum?id=nZP6NgD3QY.

Le Yu, Bowen Yu, Haiyang Yu, Fei Huang, and Yongbin Li. Language models are super mario: Absorbing abilities from homologous models as a free lunch. In *Forty-first International Conference on Machine Learning, ICML 2024, Vienna, Austria, July 21-27, 2024*. OpenReview.net, 2024. URL https://openreview.net/forum?id=fq0NaiU8Ex.

Yu Zhang and Qiang Yang. A survey on multi-task learning. *IEEE Trans. Knowl. Data Eng.*, 34 (12):5586–5609, 2022. doi: 10.1109/TKDE.2021.3070203. URL https://doi.org/10.1109/TKDE.2021.3070203.

Wayne Xin Zhao, Kun Zhou, Junyi Li, Tianyi Tang, Xiaolei Wang, Yupeng Hou, Yingqian Min, Beichen Zhang, Junjie Zhang, Zican Dong, Yifan Du, Chen Yang, Yushuo Chen, Zhipeng Chen, Jinhao Jiang, Ruiyang Ren, Yifan Li, Xinyu Tang, Zikang Liu, Peiyu Liu, Jian-Yun Nie, and Ji-Rong Wen. A survey of large language models. *CoRR*, abs/2303.18223, 2023. URL https://doi.org/10.48550/arXiv.2303.18223.

A LIMITATIONS

However, there are several limitations to consider: *a)* The experiments in this study are conducted on models with two architecture, leaving uncertainty about the transferability of our metric and method to other architectures, such as *Mamba* (Gu & Dao, 2023). Furthermore, scaling of tasks and candidate models requires further experimentation to understand the computational cost across various scenarios. *b)* The analysis is based on open source data from the Open Leaderboard, which is community-generated and may contain noise due to user bias. *c)* Correlation metrics for model kinship have not been fully explored. Other metrics may perform better than those discussed in this paper. *d)* The effectiveness of model kinship is demonstrated through empirical evidence. However, a theoretical framework (such as the assumptions in Appendix G) is needed to explain model evolution and model kinship more rigorously. *e)* Model kinship currently guides merging and enhances performance, but does not support sustained evolution. Future progress may require environmental feedback, reward models (Silver et al., 2021), as well as new architectures.

B DETAILS OF EXPERIMENTS IN MAIN SECTIONS

This section provides comprehensive details on the models used in the analysis of community experiments. The open merged models from these experiments are accessible through the Hugging Face Hub[3]. The evaluation results can be accessed in the Openleaderboard[4] The following tables cover two primary aspects:

- **(1)** Information on the selected model family trees for two distinct evolution paths, along with detailed analysis results for each merge.
- **(2)** A summary of the merge experiments conducted for distribution analysis.

B.1 SELECTING THE EVOLUTION PATH

The evolution paths are selected using a structured process, focusing on identifying key sequences within the model family trees. The steps were as follows:

- **Model Family Tree Construction**: The complete model family tree is constructed by referencing model card details for each model involved.
- **Branch Identification**: We identified the two longest branches within each tree, representing significant sequences of model merging.
- **Performance and Kinship Evaluation**: These branches were analyzed for changes in merging performance, particularly focusing on shifts in multitask capabilities and model kinship metrics.

Table 3 and 4 present detailed information on the sequential merging process. The second and third columns record the foundational models involved in each merge, while the final column lists the resulting merged models.

B.2 ADDITIONAL RESULTS IN ANALYSIS

Table 5 and Table 6 present detailed analysis results that are not reported in the main paper. These include Average Task Performance (ATP), merge gains, and model kinship values, which are computed using Pearson Correlation coefficient, Cosine Similarity, and Euclidean Distance for each merge.

Table 7 presents all merge experiments contributing to the distribution analysis. The selection of sample experiments adheres to two rules: **(1)** Samples are evenly chosen across average task performance values ranging from *0.7* to *0.7686* (the average task performance of the best 7B merged model) to accurately reflect the full scope of model evolution. **(2)** The experiments involve merges of two foundation models, as including multiple models introduces excessive noise.

[3] https://huggingface.co/datasets

[4] https://huggingface.co/spaces/open-llm-leaderboard-old/open_llm_leaderboards

Table 3: Model Family tree of evolution Path 1.

Gen	Model-1	Model-2	Model-Merged
1	Marcoroni-7B-v3	Mistral-7B-Merge-14-v0.1	distilabeled-Marcoro14-7B-slerp
2	distilabeled-Marcoro14-7B	UNA-TheBeagle-7b-v1	Beagle14-7B
3	NeuralBeagle14-7B	Turdus	TurdusBeagle-7B
4	TurdusBeagle-7B	FernandoGPT-v1	StrangeMerges_9-7B-dare_ties
5	StrangeMerges_9-7B-dare_ties	MBX-7B-v3	StrangeMerges_10-7B-slerp
6	StrangeMerges_10-7B-slerp	NeuralBeagle14-7B	StrangeMerges_11-7B-slerp
7	StrangeMerges_11-7B-slerp	MBX-7B-v3	StrangeMerges_20-7B-slerp
8	StrangeMerges_20-7B-slerp	NeuTrixOmniBe-7B-model	StrangeMerges_21-7B-slerp
9	StrangeMerges_21-7B-slerp	Experiment26	StrangeMerges_30-7B-slerp
10	StrangeMerges_30-7B-slerp	Experiment24	StrangeMerges_31-7B-slerp
11	StrangeMerges_31-7B-slerp	Experiment28	StrangeMerges_32-7B-slerp
12	StrangeMerges_32-7B-slerp	...	shadow-clown-7B-slerp
13	shadow-clown-7B-slerp	yam-jom-7B	YamShadow-7B
14	YamShadow-7B	Experiment28	YamshadowExperiment28-7B

Table 4: Model Family tree of evolution Path 2.

Gen	Model-1	Model-2	Model-Merged
1	neural-chat-7b-v3-3	openchat-3.5-1210	CatPPT-base
2	Marcoroni-7B-v3	CatPPT-base	CatMacaroni-Slerp
3	LeoScorpius-7B	CatMacaroni-Slerp	SamirGPT-v1
4	SamirGPT-v1	...	Daredevil-7B
5	NeuralBeagle14-7B	NeuralDaredevil-7B	DareBeagle-7B
6	Turdus	DareBeagle-7B	TurdusDareBeagle-7B
7	MarcMistral-7B	TurdusDareBeagle-7B	MarcDareBeagle-7B
8	MarcBeagle-7B	MarcDareBeagle-7B	MBX-7B
9	MBX-7B	...	pastiche-crown-clown-7b-dare
10	pastiche-crown-clown-7b-dare	...	shadow-clown-7B-slerp
11	yam-jom-7B	shadow-clown-7B-slerp	YamShadow-7B
12	Experiment28-7B	YamShadow-7B	YamshadowExperiment28-7B

B.3 Details of Datasets Selection

In the main experiments, we utilize three task-specific benchmark datasets—Winogrande, GSM8k, and TruthfulQA—to evaluate the distinct strengths of the models. These datasets assess the following capabilities:

- **Winogrande**: Evaluates the model's commonsense reasoning.
- **GSM8k**: Measures the model's mathematical reasoning.
- **TruthfulQA**: Assesses the model's ability to identify and address human falsehoods.

Table 5: Summary of Path 1 Results.

Gen	Model-Merged	ATP	Gain	PCC	CS	ED
1	distilabeled-Marcoro14-7B-slerp	73.63	0.55	0.82	0.76	5.15
2	Beagle14-7B	74.74	1.01	0.81	0.79	6.43
3	StrangeMerges_9-7B-dare_ties	75.15	0.45	0.93	0.89	4.66
4	StrangeMerges_9-7B-dare_ties	73.32	-0.69	0.90	0.84	4.70
5	StrangeMerges_10-7B-slerp	74.77	0.59	0.59	0.59	9.43
6	StrangeMerges_11-7B-slerp	74.8	0.045	0.87	0.86	5.31
7	StrangeMerges_20-7B-slerp	75.52	0.6	0.84	0.85	4.82
8	StrangeMerges_21-7B-slerp	76.29	0.38	0.85	0.89	4.28
9	StrangeMerges_30-7B-slerp	76.58	0.065	0.96	0.94	2.83
10	StrangeMerges_31-7B-slerp	76.67	-0.02	0.97	0.97	2.21
11	StrangeMerges_32-7B-slerp	76.68	0.11	0.99	0.99	0.62
12	shadow-clown-7B-slerp	76.64	-0.02	0.93	0.94	2.49
13	YamShadow-7B	76.6	-0.02	0.97	0.97	2.19
14	YamshadowExperiment28-7B	76.86	0.25	0.98	0.98	1.61

Table 6: Summary of Path 2 Results.

Gen	Model-Merged	ATP	Gain	PCC	CS	ED
1	CatPPT-base	72.25	2.89	0.02	0.01	20.41
2	CatMacaroni-Slerp	72.74	0.35	0.88	0.83	6.16
3	SamirGPT-v1	73.11	0.64	0.79	0.70	6.47
4	Daredevil-7B	74.12	0.33	0.87	0.83	4.81
5	DareBeagle-7B	74.58	0.15	0.79	0.77	6.01
6	TurdusDareBeagle-7B	74.94	0.32	0.90	0.86	4.59
7	MarcDareBeagle-7B	74.75	0.67	0.87	0.87	4.17
8	MBX-7B	75.04	0.11	0.96	0.96	2.90
9	pastiche-crown-clown-7b-dare	76.50	0.29	0.83	0.84	5.38
10	shadow-clown-7B-slerp	76.64	-0.02	0.93	0.94	2.49
11	YamShadow-7B	76.60	-0.02	0.97	0.97	2.19
12	YamshadowExperiment28-7B	76.86	0.25	0.98	0.98	1.61

Table 7: **All Sample Experiments** used in distribution analysis.

Model 1	Model 2	Merge Gain
Multi_verse_model-7B	Experiment26-7B	0.06
M7-7b	StrangeMerges_32-7B-slerp	-0.03
Ognoexperiment27	Multi_verse_model-7B	0.03
YamShadow-7B	Experiment28	0.25
shadow-clown-7B-slerp	yam-jom-7B	-0.02
StrangeMerges_21-7B-slerp	Experiment26	0.06
StrangeMerges_31-7B-slerp	Experiment28	0.11
NeuralBeagle14-7B	Turdus	0.45
DareBeagle-7B	Turdus	0.32
TurdusBeagle-7B	FernandoGPT-v1	-0.69
StrangeMerges_10-7B-slerp	NeuralBeagle14-7B	0.04
TurdusDareBeagle-7B	MarcMistral-7B	0.67
StrangeMerges_20-7B-slerp	NeuTrixOmniBe-7B-model-remix	0.38
StrangeMerges_11-7B-slerp	MBX-7B-v3	0.6
Marcoroni-7B-v3	Mistral-7B-Merge-14-v0.1	0.55
distilabeled-Marcoro14-7B-slerp	UNA-TheBeagle-7b-v1	1.01
UNA-TheBeagle-7b-v1	distilabeled-Marcoro14-7B-slerp	0.89
CatPPT-base	Marcoroni-7B-v3	0.35
CatMacaroni-Slerp	LeoScorpius-7B	0.64
NeuralDaredevil-7B	NeuralBeagle14-7B	0.15
StrangeMerges_9-7B-dare_ties	MBX-7B-v3	0.59
mistral-ft-optimized-1218	NeuralHerems-Mistral-2.5-7B	-0.85
neural-chat-7b-v3-2	OpenHermes-2.5-Mistral-7B	1.91
StrangeMerges_30-7B-slerp	Experiment24	-0.02
openchat-3.5-1210	neural-chat-7b-v3-3	2.89
MultiverseEx26-7B-slerp	CalmExperiment-7B-slerp	-0.09
CapybaraMarcoroni-7B	DistilHermes-2.5-Mistral-7B	0.47
Multi_verse_model-7B	Calme-7B-Instruct-v0.9	0.04
StrangeMerges_16-7B-slerp	coven_7b_128k_orpo_alpha	-0.35
Kunoichi-DPO-v2-7B	AlphaMonarch-7B	-1.05
StrangeMerges_15-7B-slerp	Kunoichi-7B	0.39
Mistral-T5-7B-v1	Marcoroni-neural-chat-7B-v2	-0.18
Marcoro14-7B-slerp	mistral-ft-optimized-1218	-0.61
mistral-ft-optimized-1218	NeuralHermes-2.5-Mistral-7B	-0.85
MarcDareBeagle-7B	MarcBeagle-7B	-0.07
MetaMath-Mistral-7B	Tulpar-7b-v2	-0.29
YugoGPT	AlphaMonarch-7B	-5.96

C Ablation Study of Greedy Strategy

The ablation study on the Greedy Strategy is conducted using the Mistral-7B architecture, following the same experimental settings outlined in the main experiments. For comparison, we employ the **random-merge strategy**, where models in each generation are merged with randomly selected models (excluding themselves) from the repository, as illustrated in Algorithm 2.

Algorithm 2 Random Merge Algorithm.

Require: A set M of n foundation models $\{m_1, m_2, \ldots, m_n\}$, Evaluation function f.

1: Generate the first generation of merged models G_1 by randomly merging pairs in set M, and set generation i = 1.
2: Combine the set G_1 into set M.
3: Evaluate each model m in set M.
4: Initialize a variable $S_{\text{prev}} = \emptyset$ to store the top k models from the previous iteration.
5: **while** $S \neq S_{\text{prev}}$ **do**
6: i++
7: Set $S_{\text{prev}} = S$.
8: Randomly select pairs of models from M. Denote this set as $P = \{p_1, p_2, \ldots, p_j\}$.
9: Merge each selected pair in set P to form the merged model set $G_i = \{m_1, m_2, \ldots, m_j\}$ for generation i, and add each merged model into set M.
10: Evaluate each new model $m \in G_i$ using f and update S.
11: **end while**

The following table presents the evaluation results. Each column represents:

- **Model:** The name of each model. Note that the first three entries are fine-tuned foundation models used in our experiments.
- **TruthfulQA_mc2, Winogrande, GSM8K:** The benchmark results for each dataset, indicating the model's task-specific capabilities.
- **Average:** The average score across all benchmarks, reflecting the model's overall generalization performance.
- **Model Kinship:** The kinship score (Here, we use cosine similarity to measure model kinship) of the parent models involved in the merge, indicating their relatedness.
- **Parent-1 and Parent-2:** The names of the parent models used in the merging process.

Model	TruthfulQA_mc2	Winogrande	GSM8K	Average	Model Kinship	Parent-1	Parent-2
MetaMath-mistral-7B	44.89	75.77	70.51	63.72	/	/	/
Mistral-7B-Instruct-v0.2	68.26	77.19	40.03	61.82	/	/	/
Open-chat-3.5-1210	52.15	80.74	65.96	66.28	/	/	/
child1-1	52.51	76.16	57.85	62.17	0.01	Instruct	MetaMath
child1-2	58.04	76.32	57.72	64.02	0.01	Instruct	Openchat
child1-3	48.96	78.69	72.86	66.84	0.03	Openchat	MetaMath
child2-1	44.68	74.00	50.80	56.40	0.29	child1-1	MetaMath
child2-2	49.78	78.93	55.72	61.47	0.41	child1-2	child1-3
child2-3	61.01	79.56	63.76	68.11	0.01	child1-3	Instruct
child3-1	51.52	78.23	56.71	62.15	0.84	child2-1	child1-2
child3-2	43.52	75.22	47.43	55.39	0.59	child2-2	MetaMath
child3-3	54.32	78.53	72.81	**68.55**	0.28	child2-3	child1-3
child4-1	55.32	78.41	56.23	63.32	0.54	child3-1	child2-3
child4-2	50.53	78.42	57.65	62.20	0.86	child3-2	child1-2
child4-3	53.45	79.31	72.65	68.47	0.67	child3-3	Openchat

Table 8: Evaluation results using the random-merge strategy.

In the **random-merge strategy**, the average performance in each generation fluctuates. The highest average performance achieved is 68.55, slightly lower than the 68.72 observed in the **greedy experiment**. While the random-merge strategy avoids convergence to local optima, it demonstrates an unstable improvement process, which can lead to unpredictable results.

D Analysis of Model Kinship Change across Merging Stages

To determine whether the discovery of increasing model kinship in model evolution paths can be generalized to the entire model evolution process, we perform an analysis of the merging stages. Given the community's predominant use of the performance-prior strategy, we calculate model kinship among models with similar performance, simulating the selection of models at each stage. For this analysis, we randomly select 5 models from each merging stage, as delineated by boundaries identified in prior analysis - Saturation Stage ($\geq$ 0.75), Learning Stage ($<$0.75 and $\geq$0.73), and Initial Merges (fine-tuned models) to form three foundation model groups, representing potential merges at different stages of model evolution.

D.1 Details of Model Group Selection

This section presents the exact models included in each model group, as shown in Table 9. The selection process is conducted across three distinct groups: **(1)** the top 5 models on the leaderboard, with a performance difference of 0.2, **(2)** 5 models with performance scores around 73 and a performance difference of 0.2, and **(3)** 5 fine-tuned models. It is important to note that the fine-tuned models are not selected based on performance, and may exhibit significant differences in results.

Table 9: Model Group in Kinship Matrix Analysis.

Group	Models
Top Model Group	YamshadowExperiment28-7B Yamshadow-7B Experiment25-7B StrangeMerges_24-7B-slerp MonaTrix-v6
Mid Stage Model Group	Daredevil-7B CatMarcoro14-7B Mayo Calmesmol-7B-slerp StrangeMerges_4-7B-slerp
Fine-tuned Model Group	Zephyr-beta MetaMath-Mistral-7B Mistral-7B-Instruct-v0.2 openchat-3.5-1210 WizardLM-2

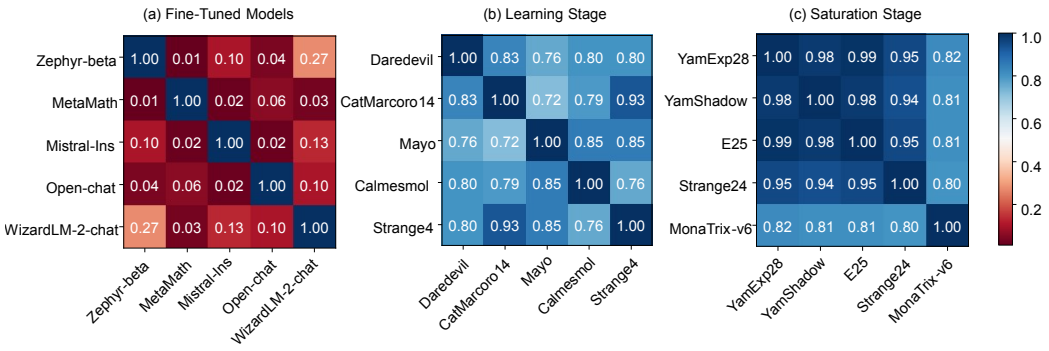

Figure 7: **The Model Kinship Matrices for the three model groups**. Each element represents the model kinship value between the corresponding models. In Group B and C, the merged models are arranged by average task performance, ordered from **high to low** (left to right).

Figure 7 illustrates the model kinship between models within each group. We observe that model kinship increases with the average task performance across models that follow different evolution paths. Additionally, during the saturation stage, all potential merges display a strong affinity, with model kinship values nearing 1.

E Analysis between Task Relatedness and Model Kinship

In the formulation of model kinship, we use the placeholder $\sim(\cdot,\cdot)$ as a similarity metric function to explore options that can effectively capture task-related differences. One such metric is cosine similarity, derived from the analysis in the task vector, which has been validated as effective for representing differences in single-task models through the cosine similarity of delta parameters (task vectors). In addition to cosine similarity, we also investigate the Pearson correlation coefficient and Euclidean distance.

However, we have not thoroughly evaluated the applicability of these metrics in the context of model evolution, particularly for merged models with multitask capabilities. To address this, we examine the relationship between the similarity metrics and task information in subsequent sections.

Our analysis focuses on the LLaMA-2 architecture, as we can find the necessary open-source fine-tuned checkpoints on various datasets. To measure differences between models, we currently use a preliminary evaluation method: the **Average Task Performance Difference** (ATPD), which aims to represent task capability differences based on evaluation performance.

The Average Task Performance Difference (ATPD) between two models, M_1 and M_2, is calculated by averaging the absolute differences in performance across all tasks. Let T denote the set of tasks, and $P_i^{(j)}$ represent the performance of model M_j on task i. Then, the ATPD is defined as:

$$\text{ATPD}(M_1, M_2) = \frac{1}{|T|} \sum_{i \in T} \left| P_i^{(1)} - P_i^{(2)} \right|$$

- $|T|$: the total number of tasks.
- $P_i^{(1)}$ and $P_i^{(2)}$: performances of models M_1 and M_2 on task i.
- $\left| P_i^{(1)} - P_i^{(2)} \right|$: absolute difference in performance for task i.

Table 10: Correlation values between ATPD and model kinship.

Method	**Correlation(cs)**	**Correlation(pcc)**	**Correlation(ed)**
Value	-0.77	-0.74	0.80

For this study, we utilize models from additional **LLaMA-2** experiments (Appendix.I). These models are merged from three fine-tuned models, allowing us to control the generated models to focus solely on the corresponding task capabilities. The following table presents the results, with Winogrande, TruthfulQA, and GSM8K representing the performance differences across each task.

The results in Table.10 demonstrate strong correlations: Cosine Similarity (-0.77) and Pearson Correlation Coefficient (-0.74) exhibit negative correlations, while Euclidean Distance (0.80) shows a positive correlation. This supports that model kinship is related to task differences. As mentioned in the limitations, the current metrics are viable but not optimal. Combining them with task information studies could further enhance the value of our work.

Table 11: Summary of Model Merging Results.

Model 1	Model 2	Winogrande	TruthfulQA	GSM8K	ATPD	Kinship(cs)	Kinship(pcc)	Kinship(ed)
child-4-1-greedy	child-5-3-greedy	0.10	0.00	0.20	0.10	0.99	0.99	2.17
child-2-1-greedy	child-4-1-greedy	0.20	0.10	0.00	0.10	0.98	0.99	4.22
child-2-1-greedy	child-5-3-greedy	0.10	0.10	0.20	0.13	0.99	0.99	2.19
child-4-exp	child-2-1-greedy	1.10	0.90	0.10	0.70	0.80	0.75	25.53
child-2-1-greedy	child-3-1-greedy	0.20	1.30	0.70	0.73	0.95	0.98	6.74
child-4-1-greedy	child-6-exp	0.10	1.90	1.40	1.13	0.74	0.71	25.54
child-4-1-greedy	child-4-2-greedy	0.30	3.00	3.20	2.17	0.97	0.98	6.57
child-2-2-greedy	child-3-1-greedy	0.50	3.10	3.10	2.23	0.97	0.98	6.57
child-2-1-greedy	child-4-2-greedy	0.50	3.10	3.20	2.27	0.91	0.96	9.29
child-3-exp	child-2-1-greedy	0.70	0.20	6.30	2.40	0.64	0.52	35.52
child-4-exp	child-2-1-greedy	1.10	2.50	4.00	2.53	0.78	0.75	25.53
child-2-1-greedy	child1-2-greedy	2.30	4.00	2.40	2.90	0.79	0.89	15.75
child-2-1-greedy	child-2-2-greedy	0.70	4.40	3.80	2.97	0.88	0.95	12.43
child-2-2-greedy	child1-2-greedy	3.00	0.40	6.20	3.20	0.89	0.92	11.68
child1-1-greedy	GSM8K	1.20	5.90	3.80	3.63	0.39	0.46	36.39
child1-1-greedy	child1-2-greedy	6.50	4.90	0.00	3.80	0.19	0.16	38.07
child-2-exp	child-2-1-greedy	1.10	2.80	8.10	4.00	0.58	0.77	28.33
child1-2-greedy	GSM8K	7.70	1.00	3.80	4.17	0.45	0.38	26.32
child-2-1-greedy	child1-3-greedy	7.80	3.10	2.90	4.60	0.58	0.51	45.24
child-3-1-greedy	child-2-exp	0.90	4.10	8.80	4.60	0.58	0.63	32.45
winogrande	TruthfulQA	14.70	9.00	3.10	8.93	0.01	0.01	74.49
child1-2-greedy	child1-3-greedy	0.60	2.70	32.30	11.87	0.64	0.52	46.06
child1-2-greedy	winogrande	4.70	3.50	27.80	12.00	0.01	0.02	55.89
winogrande	GSM8K	3.00	4.50	31.60	13.03	0.03	0.11	54.01
child1-1-greedy	child1-3-greedy	5.90	2.20	32.30	13.47	0.52	0.64	44.16
GSM8K	TruthfulQA	17.70	4.50	28.50	16.90	0.01	0.01	61.56

F Optimization Assumption of Model Evolution

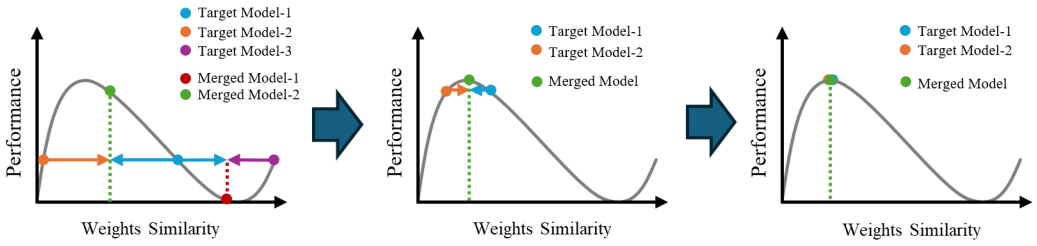

Figure 9: An intuitive illustration of **the optimization process assumption** in model evolution, where models progressively converge towards the optimal model.

Our findings using new strategy offer a new perspective on model evolution through multiple merging. If the merging process can be improved using a common optimization strategy, it raises the question of *whether the underlying mechanism mirrors this optimization problem*. Thus, we hypothesize the following:

> ***Hypothesis:*** *The evolution process may be simplified to a binary search process for most weight-averaging-based model merging methods.*

Figure 9 illustrates the ideal scenario in our assumption where multiple merges produce a highly generalized model. For the generalization task t, the y-axis represents the model performance for task t and the x-axis represents the model's weight space. In early merging stages, models fine-tuned with different tasks exhibit significant weight space dissimilarity. The merging process averages these weight spaces, and the experiment conductor selects the better-merged models while discarding the inferior ones. In stage 2, the search area narrows and the improvements become stable, eventually leading to an optimized state in stage 3 when "saturation stage" occurs.

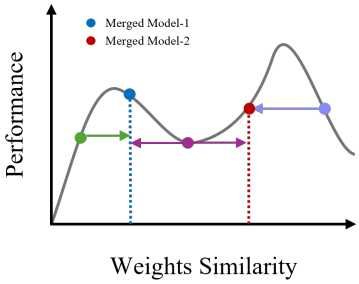

Figure 8: An intuitive illustration of **how model evolution can fall into local optima** due to a performance-prior strategy. It shows that Merged Model 2 may be overlooked, despite its potential for better multitask performance.

In this context, Model Kinship serves as a metric to quantify the weight space distance between two models, with a higher model kinship indicating a lower weight space distance. Following this assumption, our findings of the optimization problem in model evolution can be elucidated in Figure 8.

However, we currently lack sufficient evidence to validate this hypothesis. Future work is needed to explore this further.

G Additional Results: Analysis of Model Kinship and Average Task Performance

This section provides supplementary analysis on the relationship between model kinship and average task performance. Figure 10 illustrates a comparison between average task performance and model kinship using two additional metrics not included in the main paper. From an intuitive observation, model kinship based on the three metrics exhibits a similar correlation with average task performance.

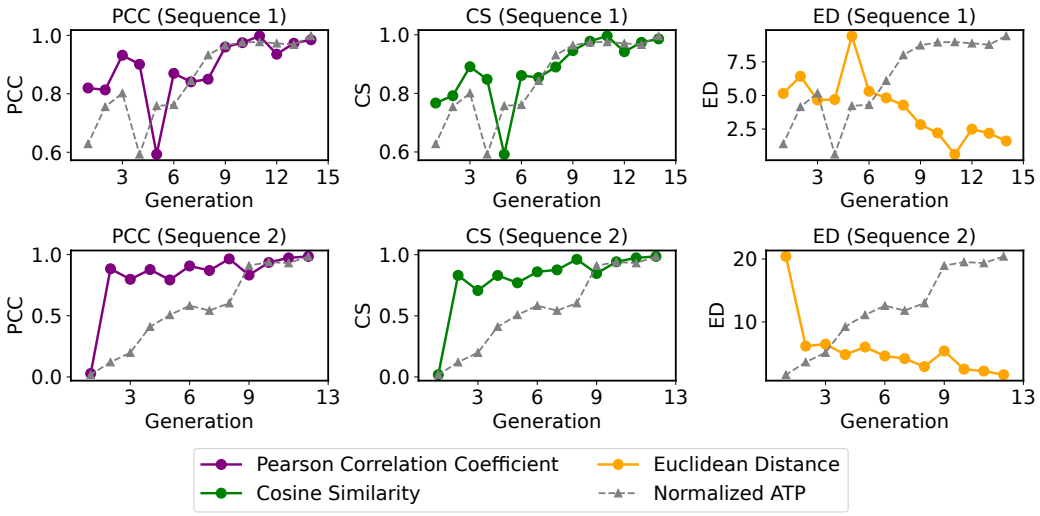

Figure 10: Illustration of comparison between the correlation of Pearson Correlation Coefficient (PCC), Cosine Similarity (CS), and Euclidean Distance (ED) with average task performance (Normalized to the same value scale).

H REFERENCED CONCEPTS IN EVOLUTIONARY BIOLOGY

In this section, we detail the conceptual parallels between biological processes and model merging, highlighting our motivation for employing model kinship.

H.1 ITERATIVE MERGING VS. ARTIFICIAL SELECTION

We draw inspiration for model evolution from biological evolution, specifically focusing on the correlation between biological evolution through artificial selection and model evolution via model merging. Artificial selection involves retaining desirable traits by manually selecting breeding pairs in each generation, typically those exhibiting the most significant features. Similarly, model evolution, as explored in this paper through Iterative Model Merging, adopts a comparable approach: users preserve desired task capabilities by strategically selecting merging pairs. Through iterative merging, they can develop a model that is proficient in all tasks in a given task set. To illustrate this comparison more effectively, Figure 11 shows an example of combining two features/task capabilities in evolution.

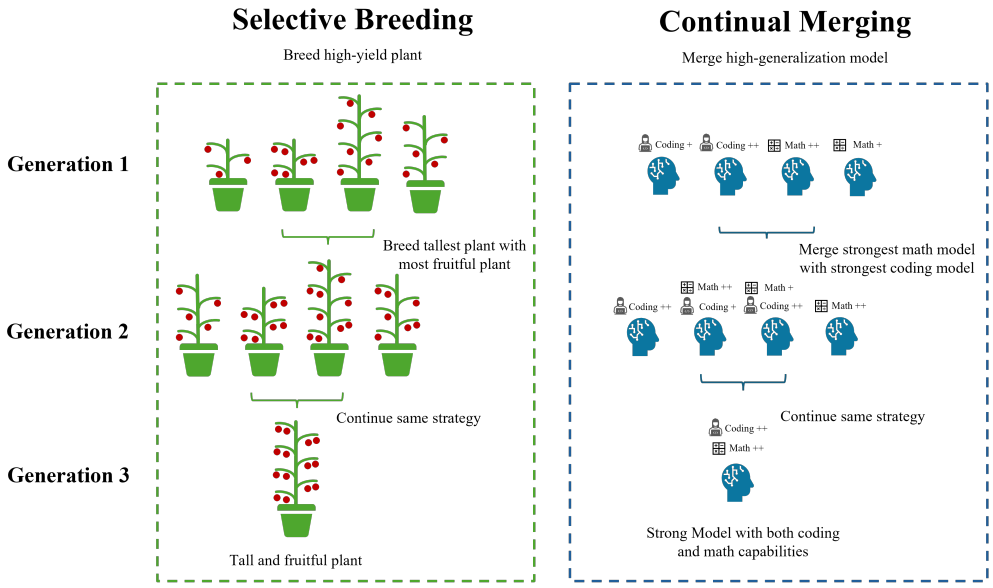

Figure 11: An intuitive **comparison between selective breeding and continual model merging**. The **left** process demonstrates breeding a tall and frutful plant by selecting parents with the desired traits in an biological scenario. The **right** process shows developing a model with capabilities of coding and math through model evolution.

H.2 INBREEDING DEPRESSION VS. SATURATION STAGE

As highlighted in the main paper, one of our key findings is that the late stage of model evolution often enters a saturation stage, during which models exhibit minimal differences from one another. This phenomenon parallels ”inbreeding depression” in artificial selection, where breeding closely related individuals reduces genetic diversity and fitness. Although genetic inheritance and model weights operate differently, merging closely related models leads to new models with minimal variation, thereby reducing the effectiveness of merging, particularly in weight averaging. To address this issue, we propose quantifying the differences between models, a concept we term model kinship, to guide the merging process and mitigate the challenges associated with the saturation stage in model evolution.

I Full Evaluation Results of Main Experiments and Additional Experiments

Table 12 provides a detailed evaluation of the main experiments, including results for exploration models and their performance on specific tasks.

I.1 Llama2 Experiments

To validate the generalization of our strategy, we conduct additional experiments on Llama-2-8B architecture. Table 13 provides information on additional experiments conducted using Llama-2. Consistent with the results observed for Mistral-7B, model evolution guided by model kinship produces better generalized models compared to the vanilla greedy strategy in Llama-2.

Table 12: Evaluation Results of Main Experiments of Mistral-7B.

Model	TruthfulQA	Winogrande	GSM8K	Avg.	Model Kinship
MetaMath	44.89	75.77	70.51	63.72	/
Instruct	68.26	77.19	40.03	61.82	/
Open-chat	52.15	80.74	65.96	66.28	/
model-1-1-greedy	52.51	76.16	57.85	62.17	0.01
model-1-2-greedy	58.04	76.32	57.72	64.02	-0.02
model-1-3-greedy	48.96	78.69	72.86	66.84	0.05
model-2-1-greedy	50.94	80.11	75.13	68.72	0.93
model-2-2-greedy	49.78	78.93	55.72	61.47	0.57
model-2-3-greedy	52.36	78.61	52.99	61.32	0.58
model-2-exp	61.01	79.56	63.76	68.11	-0.02
model-3-1-greedy	51.95	80.51	73.31	68.59	0.95
model-3-2-greedy	49.96	79.72	73.54	67.74	0.93
model-3-3	56.95	80.25	70.00	69.06	0.24
model-3-4	54.38	78.45	73.01	68.61	0.32
model-3-exp	54.13	78.69	71.65	68.15	0.03
model-4-1-greedy	50.82	80.11	74.60	68.51	0.98
model-4-2-greedy	50.36	79.47	74.31	68.04	0.98
model-4-3-greedy	51.04	79.72	74.83	68.53	0.94
model-4-4	53.31	79.40	73.54	68.75	0.54
model-4-5	52.48	79.01	73.68	68.39	0.66
model-4-6	53.69	79.72	73.69	69.03	0.52
model-4-exp	55.16	78.53	71.80	68.49	0.48
model-5-1	54.85	79.37	73.31	**69.13**	0.65
model-5-2	54.78	79.40	72.86	68.98	0.65
model-5-3	53.49	79.24	73.16	68.63	0.98
model-5-exp	52.98	79.32	72.78	68.36	0.59

Table 13: Evaluation Results of addtional experiments of Llama-2.

Model	TruthfulQA	Winogrande	GSM8K	Avg.	Model Kinship
winogrande	42.0	77.9	6.4	42.1	/
GSM8K	39.0	73.4	38.0	50.1	/
TruthfulQA	56.7	68.9	9.5	45.0	/
child1-1-greedy	40.2	79.3	34.2	51.2	0.03
child1-2-greedy	46.7	74.4	34.2	51.7	0.01
child1-3-greedy	46.1	77.1	1.9	41.7	0.01
child-2-1-greedy	44.6	78.6	36.8	53.3	0.19
child-2-2-greedy	43.7	74.0	40.4	52.7	0.45
child-2-3-greedy	38.9	77.5	37.1	51.1	0.39
child-2-exp	43.3	81.2	28.5	51.0	0.01
child-3-1-greedy	44.2	77.1	37.3	52.8	0.88
child-3-2-greedy	45.4	77.5	34.5	52.4	0.79
child-3-3-greedy	45.0	73.8	36.6	51.8	0.89
child-3-exp	45.1	78.6	30.3	51.3	0.58
child-4-1-greedy	44.4	78.5	36.8	53.2	0.95
child-4-2-greedy	44.1	75.5	40.0	53.1	0.97
child-4-exp	43.3	80.9	32.6	52.2	0.81
child-5-1-greedy	44.2	77.1	37.2	52.8	0.97
child-5-2-greedy	44.3	77.4	36.7	52.8	0.91
child-5-3-greedy	44.3	78.3	36.8	53.1	0.98
child-5-exp	44.5	78.1	32.0	51.5	0.64
child-6-1-greedy	44.5	78.5	36.8	53.2	0.99
child-6-2-greedy	44.4	78.3	36.8	53.2	0.99
child-6-3-greedy	44.3	78.3	36.8	53.1	0.99
child-6-exp	44.3	80.4	35.3	**53.4**	0.80