

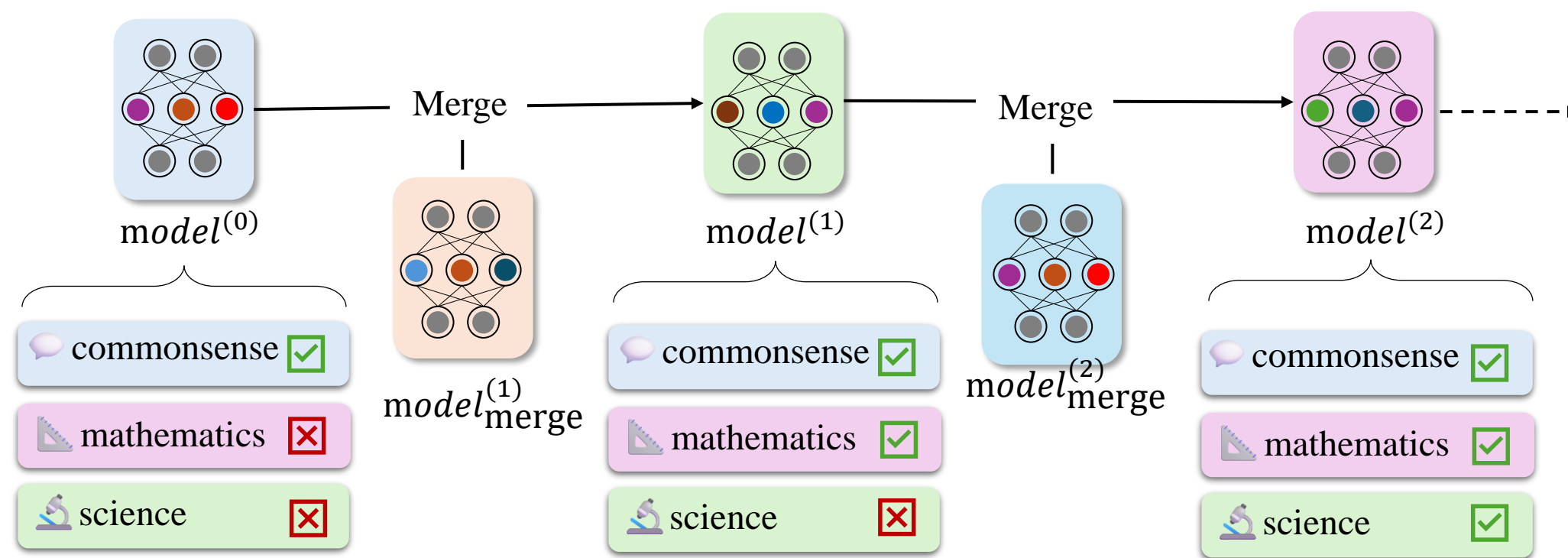
## Conceptual Motivation

### What we know:

- LLMs need require **frequent and continuous updates** to keep up with growing user **demands across diverse tasks**.
- Model Merging** has emerged as a **cost-effective** approach to combine the strengths of different models **without altering their underlying architecture**.

### Model Evolution:

- LLMs can evolve to integrate new capabilities by **iteratively merging with one another**.



$$E(\theta^{(t)} | \theta^{(t-1)}, \theta^{(t-2)}, \dots, \theta^{(0)}) = E(\theta^{(t)} | \theta^{(t-1)}, \theta_{\text{merge}}^{(t)})$$

**Question:** How can we systematically select models for merging to achieve greater performance improvements?

## Key Contributions

- Model Kinship:** Introduce a kinship metric to assess LLM similarity during merging, guiding auto-merging strategies.
- Empirical Analysis:** Evaluate iterative merging dynamics, highlighting multitask performance gains and stagnation, with insights from model kinship.
- Practical Strategies:** Propose Top-k Greedy Merging with model kinship to efficiently tackle merging optimization challenges.

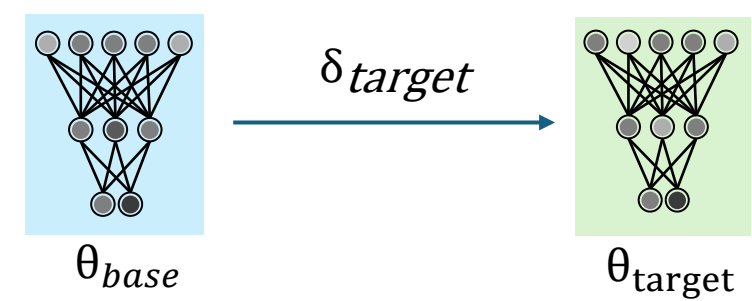
## Model Kinship

We need an **efficient metric** to evaluate the **overall capability difference** between models, without relying on a dataset for evaluation, **to estimate the outcome of future merges (high or low)**.

- Extract **delta parameter**  $\delta_{\text{target}}$  of the target models.
- Calculate the **kinship** between **delta parameters**.

$$\delta_{\text{target}} = \theta_{\text{target}} - \theta_{\text{base}}$$

$$k = \text{sim}(\delta_1, \delta_2)$$

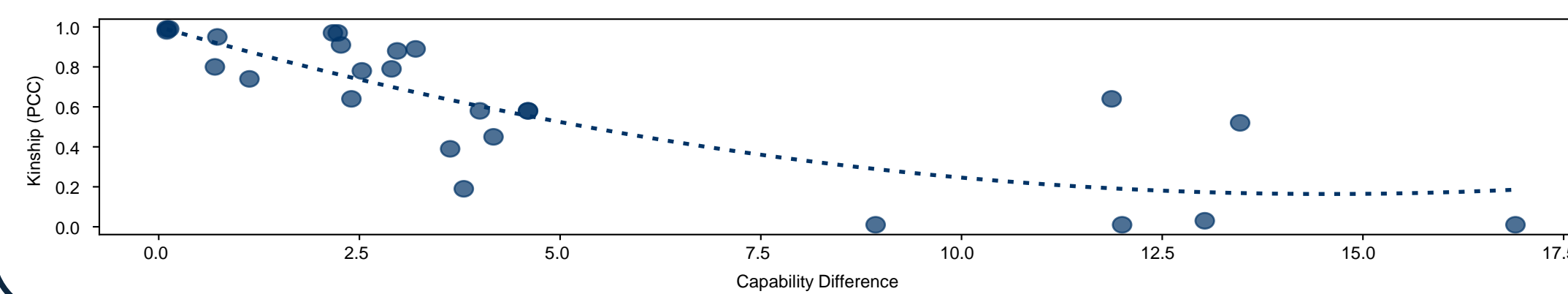


Parameter changes introduced through fine-tuning/iterative merging processes.

e.g. adopt **Pearson Correlation Coefficient** as similarity metric:

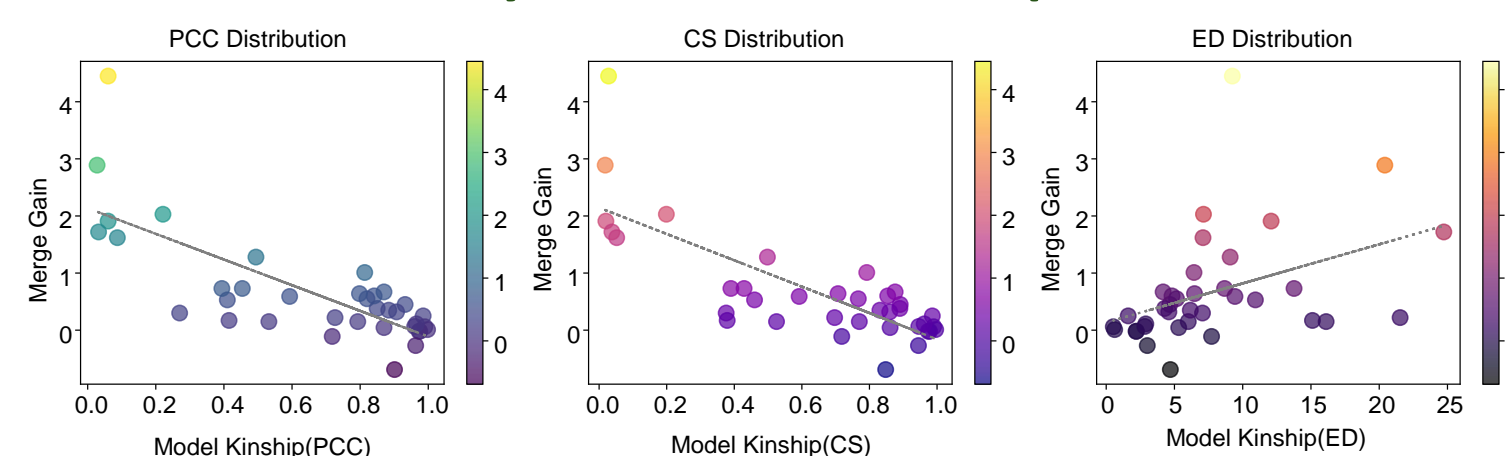
$$\text{sim}(\delta_i, \delta_j) = \frac{\text{cov}(\delta_i, \delta_j)}{\sigma_{\delta_i} \sigma_{\delta_j}} = \frac{\sum(\delta_i - \bar{\delta}_i)(\delta_j - \bar{\delta}_j)}{\sqrt{\sum(\delta_i - \bar{\delta}_i)^2} \sqrt{\sum(\delta_j - \bar{\delta}_j)^2}}$$

- Correlation between task capability difference and kinship**

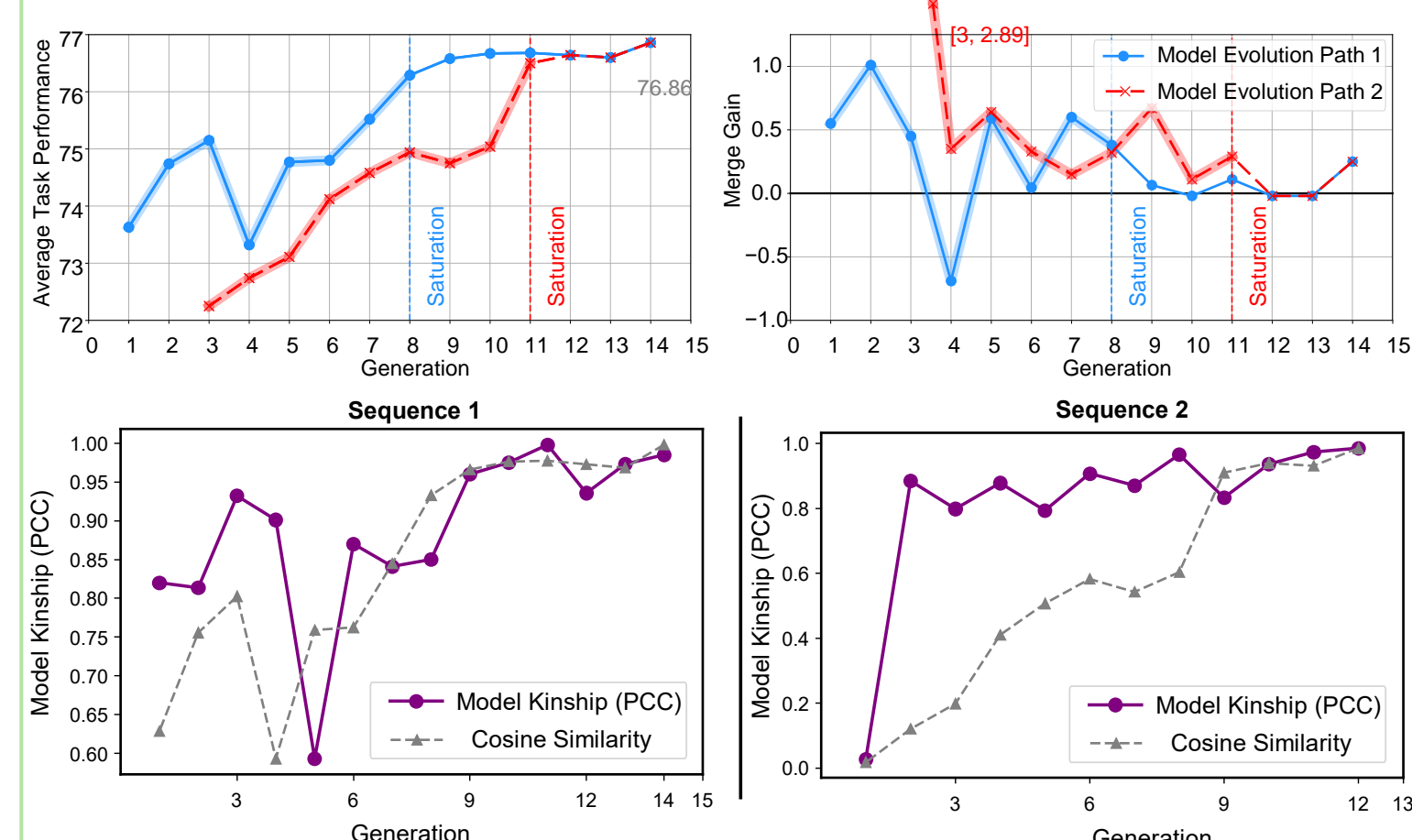


## Initial Analysis

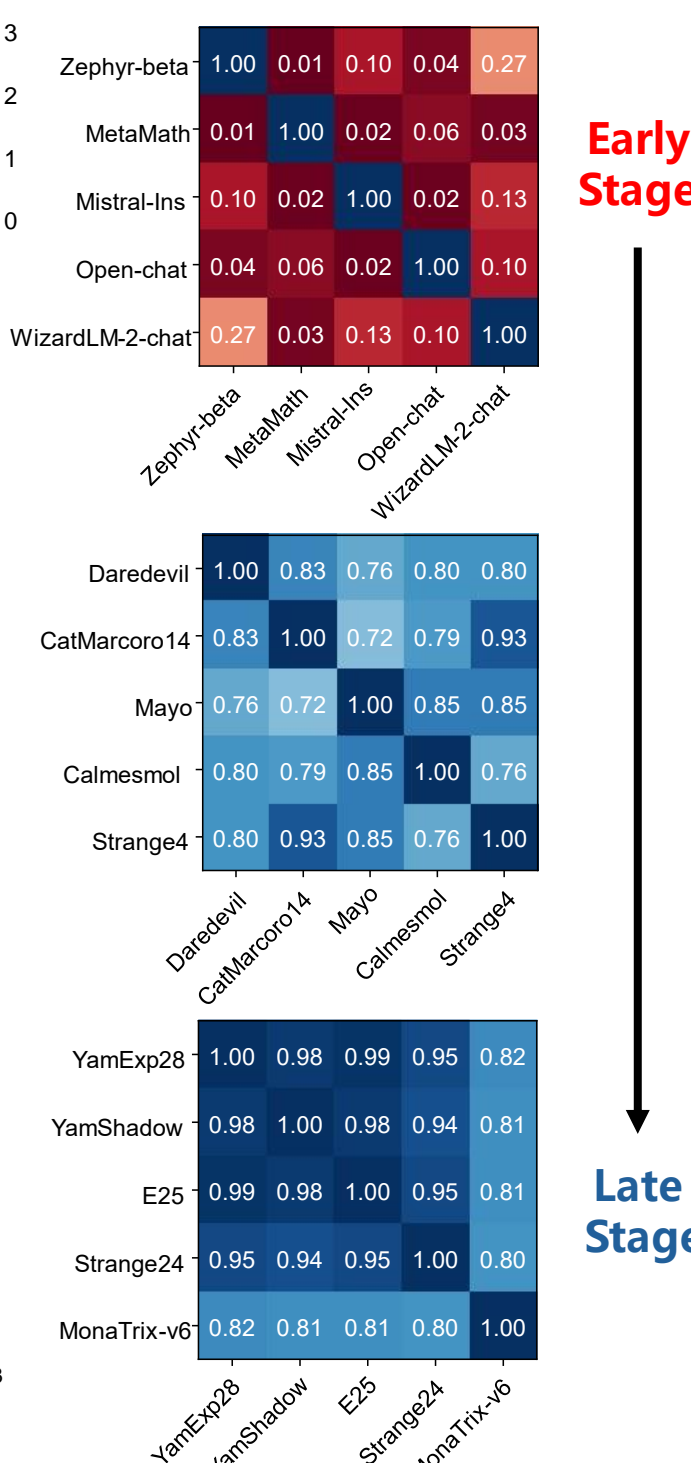
### Correlation Analysis of Model Kinship



### Kinship Change Through Model Evolution Paths



### Mutual Kinship of Candidate Models Through Evolution

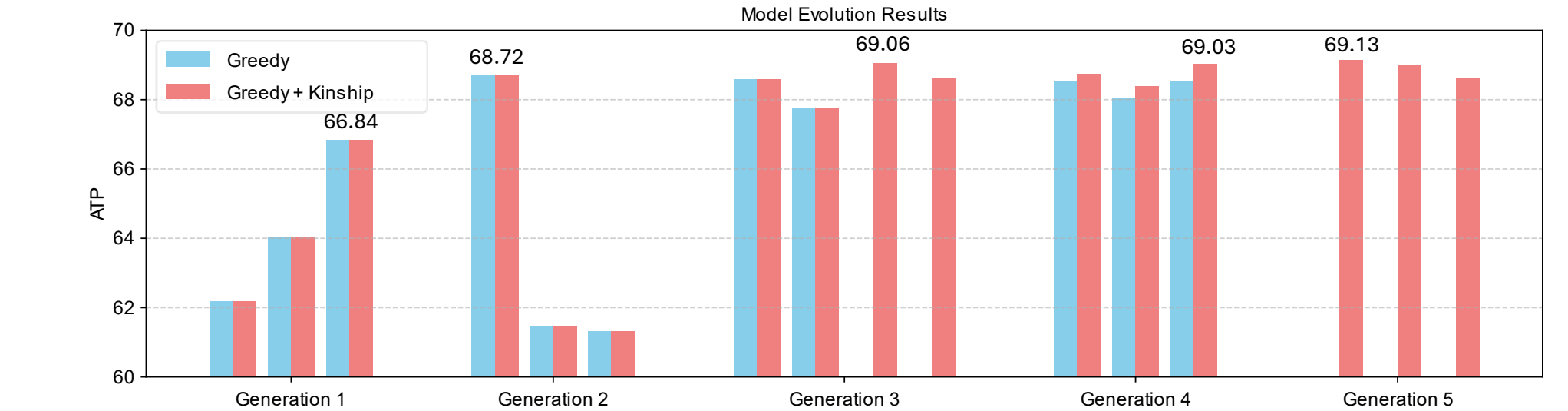


## Main Results

- Enhance the greedy merging strategy by **adding additional merges based on low model kinship**.

Table 2: Results of merging experiments comparing the vanilla greedy strategy and our proposed approach. The first three models serve as the foundation models in both experiments. **Note:** The model kinship experiment was terminated at generation 5, as it has already outperformed the greedy strategy by that point.

Greedy Strategy				+ Model Kinship			
Model	Avg.	Gain	Kinship	Model	Avg.	Gain	Kinship
MetaMath	63.72	/	/	MetaMath	63.72	/	/
Instruct	61.82	/	/	Instruct	61.82	/	/
Open-chat	66.28	/	/	Open-chat	66.28	/	/
model-1-1	62.17	-0.6	0.01	model-1-1	62.17	-0.6	0.01
model-1-2	64.02	-0.03	-0.02	model-1-2	64.02	-0.03	-0.02
model-1-3	66.84	+1.84	0.05	model-1-3	66.84	+1.84	0.05
<b>model-2-1</b>	<b>68.72</b>	<b>+2.16</b>	<b>0.93</b>	<b>model-2-1</b>	<b>68.72</b>	<b>+2.16</b>	<b>0.93</b>
model-2-2	61.47	-3.96	0.57	model-2-2	61.47	-3.96	0.57
model-2-3	61.32	-3.83	0.58	model-2-3	61.32	-3.83	0.58
model-3-1	68.59	+1.09	0.95	model-3-2	67.74	+1.09	0.93
model-3-2	67.74	-0.04	0.93	model-3-3	69.06	+0.74	0.24
-	-	-	-	model-3-4	68.61	+1.13	0.32
model-4-1	68.51	-0.14	0.98	model-4-4	68.75	-0.14	0.54
model-4-2	68.04	-0.19	0.98	model-4-5	68.39	-0.27	0.66
model-4-3	68.53	+0.37	0.94	model-4-6	69.03	+0.15	0.52
-	-	-	-	<b>model-5-1</b>	<b>69.13</b>	<b>+0.04</b>	<b>0.65</b>
-	-	-	-	model-5-2	68.98	+0.07	0.65
-	-	-	-	model-5-3	68.63	-0.37	0.98



### Findings:

- Merging low-kinship models introduces novel weight variations, enabling continued iterative merging.
- Early stopping at high kinship reduces resource consumption while maintaining performance.

### Future works

- Advance **interpretability** by designing more **informative metrics** to explain model merging behavior.
- Explore **foundational theory** for **automated, self-evolving model merging pipelines**.