Exercise 7

7.1 Problem Statement:

Use Naïve Bayes classifier to solve the credit card fraud detection problem over a skewed dataset.

7.2 Description of Machine Learning Algorithm:

A Naive Bayes classifier is a probabilistic machine learning model that's used for classification task. It is a classification technique based on Bayes' Theorem with an assumption of independence among predictors. In simple terms, a Naive Bayes classifier assumes that the presence of a particular feature in a class is unrelated to the presence of any other feature.

7.3 Description of Data Set:

Title of the data set: Credit card fraud detection

The data represents credit card transactions that occurred over two days in September 2013 by European cardholders.

Each record is classified as normal (class "0") or fraudulent (class "1") and the transactions are heavily skewed towards normal. Specifically, there are 492 fraudulent credit card transactions out of a total of 284,807 transactions, which is a total of about 0.172% of all transactions.

7.4 Data Preprocessing and Exploratory Data Analysis:

Data preprocessing is the process of transforming raw data into an understandable format. It is also an important step in data mining as we cannot work with raw data. The quality of the data should be checked before applying machine learning or data mining algorithms.

Major Tasks in Data Preprocessing:

- 1. Data cleaning
- 2. Data integration
- 3. Data reduction
- 4. Data transformation

Exploratory data analysis (EDA) is a technique that data professionals can use to understand a dataset before they start to model it. Some people refer to EDA as data exploration. The goal of conducting EDA is to determine the characteristics of the dataset. Conducting EDA can help data analysts make predictions and assumptions about data. Often, EDA involves data visualization, including creating graphs like histograms, scatter plots and box plots.

Major Tasks in EDA:

- 1. Observe your dataset
- 2. Find any missing values
- 3. Categorize your values
- 4. Find the shape of your dataset
- 5. Identify relationships in your dataset
- 6. Locate any outliers in your dataset

7.5 Machine Learning Package Used for Model building:

For classification of model we use scikit-learn

Scikit-learn is an open source Machine Learning Python package that offers functionality supporting supervised and unsupervised learning. Additionally, it provides tools for model development, selection and evaluation as well as many other utilities including data pre-processing functionality.

More specifically, scikit-learn's main functionality includes classification, regression, clustering, dimensionality reduction, model selection and pre-processing. sThe library is very simple to use and most importantly efficient as it is built on **NumPy**, **SciPy** and **matplotlib**.

Neural networks are a machine learning method inspired by how the human brain works. They are particularly good at doing pattern recognition and classification tasks, often using images as inputs. They're a well established machine learning technique that has been around since the 1950s but have gone through several iterations since that have overcome fundamental limitations of the previous one. The current state of the art neural networks are often referred to as deep learning.

7.6 Implementation:

```
from google.colab import drive
drive.mount('/content/drive')
Mounted at /content/drive
```

Data Analysis Importing the libraries

```
import numpy as np
import pandas as pd
import seaborn as sns
import matplotlib.pyplot as plt
from sklearn.preprocessing import StandardScaler
from sklearn.metrics import recall_score, precision_score, accuracy_score, f1_s
core
import scipy.stats as stats
%matplotlib inline
plt.style.use('ggplot')
```

Loading dataset

```
# Data Handling: Load CSV
df = pd.read_csv("/content/drive/MyDrive/ML Lab dataset/creditcard.csv")
# get to know list of features, data shape, stat. description.
print(df.shape)

print("First 5 lines:")
print(df.head(5))

print("describe: ")
print(df.describe())
print("info: ")
```

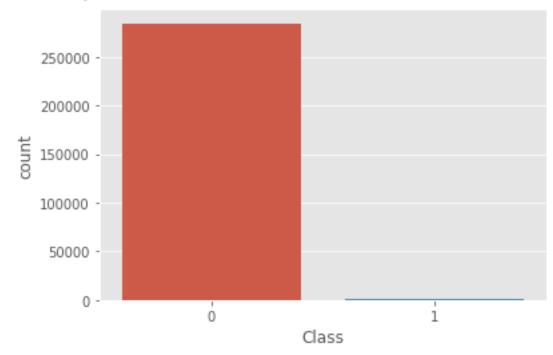
```
print(df.info())
(284807, 31)
First 5 lines:
                         V2
                                   V3
                                                       V5
   Time
               V1
                                             774
                                                                  V6
                                                                            77
0
    0.0 -1.359807 -0.072781 2.536347
                                      1.378155 -0.338321 0.462388 0.239599
1
    0.0 \quad 1.191857 \quad 0.266151 \quad 0.166480 \quad 0.448154 \quad 0.060018 \quad -0.082361 \quad -0.078803
2
    1.0 - 1.358354 - 1.340163 1.773209 0.379780 - 0.503198 1.800499 0.791461
3
    1.0 -0.966272 -0.185226
                             1.792993 -0.863291 -0.010309 1.247203 0.237609
    2.0 \;\; -1.158233 \quad 0.877737 \quad 1.548718 \quad 0.403034 \;\; -0.407193 \quad 0.095921 \quad 0.592941
                                                     V23
                   V9
                                 V21
                                           V22
                                                                V24
                                                                          V25
         V8
                       . . .
  0.098698 0.363787
                       ... -0.018307 0.277838 -0.110474 0.066928
                                                                    0.128539
  0.085102 -0.255425
                       ... -0.225775 -0.638672 0.101288 -0.339846 0.167170
1
                       ... 0.247998 0.771679 0.909412 -0.689281 -0.327642
  0.247676 -1.514654
3 0.377436 -1.387024
                       ... -0.108300 0.005274 -0.190321 -1.175575 0.647376
4 -0.270533 0.817739
                       ... -0.009431 0.798278 -0.137458 0.141267 -0.206010
                  V27
                            V28
                                Amount Class
0 -0.189115 0.133558 -0.021053
                                 149.62
                                             0
1 0.125895 -0.008983 0.014724
                                   2.69
                                             0
2 -0.139097 -0.055353 -0.059752
                                378.66
                                             0
3 -0.221929 0.062723 0.061458
                                123.50
4 0.502292 0.219422 0.215153
                                 69.99
[5 rows x 31 columns]
describe:
                Time
                                V1
                                              V2
                                                             V3
                                                                           V/4
      284807.000000
                     2.848070e+05 2.848070e+05 2.848070e+05 2.848070e+05
count
        94813.859575 3.918649e-15 5.682686e-16 -8.761736e-15 2.811118e-15
mean
std
        47488.145955 1.958696e+00 1.651309e+00 1.516255e+00 1.415869e+00
            0.000000 -5.640751e + 01 -7.271573e + 01 -4.832559e + 01 -5.683171e + 00
min
25%
        54201.500000 -9.203734e-01 -5.985499e-01 -8.903648e-01 -8.486401e-01
50%
       84692.000000 1.810880e-02 6.548556e-02 1.798463e-01 -1.984653e-02
75%
       139320.500000 1.315642e+00 8.037239e-01 1.027196e+00 7.433413e-01
       172792.000000 2.454930e+00 2.205773e+01 9.382558e+00 1.687534e+01
max
                 V5
                               V6
                                             V7
                                                           V8
                                                                          V9
count 2.848070e+05 2.848070e+05 2.848070e+05 2.848070e+05 2.848070e+05
mean -1.552103e-15 2.040130e-15 -1.698953e-15 -1.893285e-16 -3.147640e-15
       1.380247e+00 1.332271e+00 1.237094e+00 1.194353e+00 1.098632e+00
std
      -1.137433e+02 -2.616051e+01 -4.355724e+01 -7.321672e+01 -1.343407e+01
min
25%
      -6.915971e-01 -7.682956e-01 -5.540759e-01 -2.086297e-01 -6.430976e-01
      -5.433583e-02 -2.741871e-01 4.010308e-02 2.235804e-02 -5.142873e-02
50%
75%
       6.119264e-01 3.985649e-01 5.704361e-01 3.273459e-01 5.971390e-01
       3.480167e+01 7.330163e+01 1.205895e+02 2.000721e+01 1.559499e+01
max
                                   V22
                     V21
                                                 V23
       ... 2.848070e+05 2.848070e+05 2.848070e+05 2.848070e+05
count
mean
       ... 1.473120e-16 8.042109e-16 5.282512e-16 4.456271e-15
       ... 7.345240e-01 7.257016e-01 6.244603e-01 6.056471e-01
std
min
       \dots -3.483038e+01 -1.093314e+01 -4.480774e+01 -2.836627e+00
25%
       ... -2.283949e-01 -5.423504e-01 -1.618463e-01 -3.545861e-01
       ... -2.945017e-02 6.781943e-03 -1.119293e-02 4.097606e-02
50%
75%
       ... 1.863772e-01 5.285536e-01 1.476421e-01 4.395266e-01
            2.720284e+01 1.050309e+01 2.252841e+01 4.584549e+00
max
```

```
V25
                             V26
                                           V27
                                                         V28
                                                                     Amount
       2.848070e+05 2.848070e+05 2.848070e+05 2.848070e+05
                                                              284807.000000
count
       1.426896e-15 1.701640e-15 -3.662252e-16 -1.217809e-16
                                                                  88.349619
mean
      5.212781e-01 4.822270e-01 4.036325e-01 3.300833e-01
                                                                 250.120109
std
min
      -1.029540e+01 -2.604551e+00 -2.256568e+01 -1.543008e+01
                                                                   0.000000
25%
      -3.171451e-01 -3.269839e-01 -7.083953e-02 -5.295979e-02
                                                                   5.600000
      1.659350e-02 -5.213911e-02 1.342146e-03 1.124383e-02
                                                                  22.000000
50%
75%
      3.507156e-01 2.409522e-01 9.104512e-02 7.827995e-02
                                                                  77.165000
      7.519589e+00 3.517346e+00 3.161220e+01 3.384781e+01
                                                               25691.160000
max
               Class
count 284807.000000
            0.001727
mean
            0.041527
std
min
            0.000000
            0.000000
25%
50%
            0.000000
75%
            0.000000
max
            1.000000
[8 rows x 31 columns]
info:
<class 'pandas.core.frame.DataFrame'>
RangeIndex: 284807 entries, 0 to 284806
Data columns (total 31 columns):
     Column Non-Null Count
                             Dtype
    _____
            _____
             284807 non-null float64
 0
     Time
    V1
             284807 non-null float64
 1
             284807 non-null float64
 2
    V2
 3
    V3
             284807 non-null
                            float64
    V4
             284807 non-null float64
 4
 5
    V5
             284807 non-null float64
             284807 non-null float64
    V6
 6
 7
    V7
             284807 non-null float64
 8
    V8
             284807 non-null float64
 9
    V9
             284807 non-null float64
             284807 non-null float64
 10 V10
 11 V11
             284807 non-null float64
 12 V12
             284807 non-null float64
 13 V13
             284807 non-null float64
             284807 non-null float64
 14 V14
 15
    V15
             284807 non-null float64
 16 V16
             284807 non-null float64
 17 V17
             284807 non-null float64
             284807 non-null float64
 18 V18
 19
    V19
             284807 non-null float64
 20 V20
             284807 non-null float64
 21 V21
             284807 non-null float64
 22
    V22
             284807 non-null float64
 23
    V23
             284807 non-null float64
 24 V24
             284807 non-null float64
 25 V25
             284807 non-null float64
             284807 non-null float64
 26 V26
 27
    V27
             284807 non-null
                             float64
 28 V28
             284807 non-null float64
 29 Amount 284807 non-null float64
```

Exploratory Data Analysis

Analysis of Target Variable

sns.countplot(data=df, x='Class')



Number of Genuine and Fraud Transactions

```
fraud = df[df['Class']==0]
genuine = df[df['Class']==0]
perc_genuine = (len(genuine)/(len(genuine)+len(fraud)))*100
print('Number of Genuine Transactions = {} and the percentage of genuine transa ctions = {:.3f} %'.format(len(genuine),perc_genuine))
Number of Genuine Transactions = 284315 and the percentage of genuine transactions = 99.827 %

perc_fraud = (len(fraud)/(len(genuine)+len(fraud)))*100
print('Number of fraud Transactions = {} and the percentage of fraud transactions = {:.3f} %'.format(len(fraud),perc_fraud))
Number of fraud Transactions = 492 and the percentage of fraud transactions = 0.173 %
```

Data is highly imbalanced

fraud.Amount.describe()

```
492.000000
count
           122.211321
mean
std
           256.683288
             0.000000
min
25%
             1.000000
50%
             9.250000
75%
           105.890000
          2125.870000
max
Name: Amount, dtype: float64
genuine.Amount.describe()
         284315.000000
count
              88.291022
mean
std
             250.105092
               0.000000
min
25%
               5.650000
50%
              22.000000
75%
              77.050000
           25691.160000
max
Name: Amount, dtype: float64
plot, (axis1, axis2) = plt.subplots(2, 1)
axis1.hist(fraud.Amount, bins = 50)
axis1.set title('Fraud')
axis2.hist(genuine.Amount, bins = 50)
axis2.set title('Genuine')
plt.xlabel('Amount')
plt.ylabel('Number of Transactions')
plt.xlim((0, 20000))
plot.suptitle('Amount per transaction')
plt.yscale('log')
plt.show()
                    Amount per transaction
                             Fraud
   300
   200
   100
     0
Number of Transactions
                           Genuine
                                       1500
                                                 2000
                  500
   105
   10^{3}
   10<sup>1</sup>
           2500
                 5000
                        7500 10000 12500 15000 17500 20000
```

Fraud transactions are minimal

Analyzing Features

Amount

```
plt.figure(figsize=(10,8))
plt.title('Distribution of Monetary Value Feature')
```

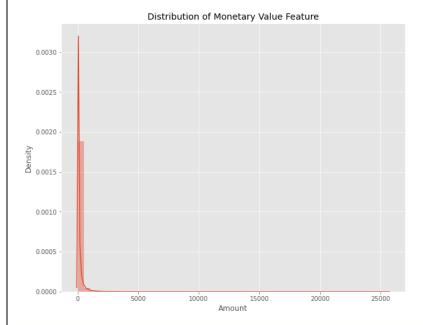
sns.distplot(df.Amount)

/usr/local/lib/python3.7/dist-packages/seaborn/distributions.py:2619:

FutureWarning: `distplot` is a deprecated function and will be removed in a future version. Please adapt your code to use either `displot` (a figure-level function with similar flexibility) or `histplot` (an axes-level function for histograms).

warnings.warn(msg, FutureWarning)

<matplotlib.axes. subplots.AxesSubplot at 0x7f715499c3d0>



plt.figure(figsize=(10,8))

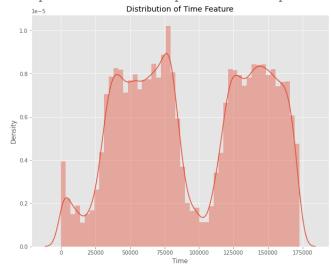
plt.title('Distribution of Time Feature')

sns.distplot(df.Time)

/usr/local/lib/python3.7/dist-packages/seaborn/distributions.py:2619:
FutureWarning: `distplot` is a deprecated function and will be removed in a future version. Please adapt your code to use either `displot` (a figure-level function with similar flexibility) or `histplot` (an axes-level function for histograms).

warnings.warn(msg, FutureWarning)

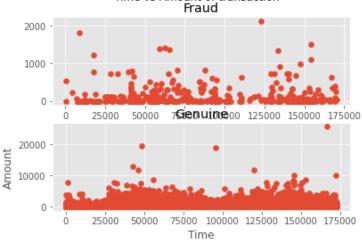
<matplotlib.axes. subplots.AxesSubplot at 0x7f7152062510>



Visualizing time with respect to class

```
plot, (axis1, axis2) = plt.subplots(2, 1)
axis1.scatter(fraud.Time, fraud.Amount)
axis1.set_title('Fraud')
axis2.scatter(genuine.Time, genuine.Amount)
axis2.set_title('Genuine')
plt.xlabel('Time')
plt.ylabel('Amount')
plot.suptitle('Time vs Amount of transaction')
#plt.show();
Text(0.5, 0.98, 'Time vs Amount of transaction')
```

Time vs Amount of transaction



Time of transaction has no effect

Correlation

Visualizing correlation of all the features

corr = df.corr()
corr

	Time	V1	V2	V3	V4	VS	V6	V7	V8	V9	 V21	V22	V23	V24	V25	V26	V27	V28	Amount	Class
Time	1.000000	1.173963e-01	-1.059333e-02	-4.196182e-01	-1.052602e-01	1.730721e-01	-6.301647e-02	8.471437e-02	-3.694943e-02	-8.660434e-03	4.473573e-02	1.440591e-01	5.114236e-02	-1.618187e-02	-2.330828e-01	-4.140710e-02	-5.134591e-03	-9.412688e-03	-0.010596	-0.012323
V1	0.117396	1.000000e+00	4.135835e-16	-1.227819e-15	-9.215150e-16	1.812612e-17	-6.506567e-16	-1.005191e-15	-2.433822e-16	-1.513678e-16	-2.457409e-16	-4.290944e-16	6.168652e-16	-4.425156e-17	-9.605737e-16	-1.581290e-17	1.198124e-16	2.083082e-15	-0.227709	-0.101347
V2	-0.010593	4.135835e-16	1.000000e+00	3.243764e-16	-1.121065e-15	5.157519e-16	2.787346e-16	2.055934e-16	-5.377041e-17	1.978488e-17	-8.480447e-17	1.526333e-16	1.634231e-16	1.247925e-17	-4.478846e-16	2.057310e-16	-4.966953e-16	-5.093836e-16	-0.531409	0.091289
V3	-0.419618	-1.227819e-15	3.243764e-16	1.000000e+00	4.711293e-16	-6.539009e-17	1.627627e-15	4.895305e-16	-1.268779e-15	5.568367e-16	5.706192e-17	-1.133902e-15	-4.983035e-16	2.686834e-19	-1.104734e-15	-1.238062e-16	1.045747e-15	9.775546e-16	-0.210880	-0.192961
V4	-0.105260	-9.215150e-16	-1.121065e-15	4.711293e-16	1.000000e+00	-1.719944e-15	-7.491959e-16	-4.104503e-16	5.697192e-16	6.923247e-16	 -1.949553e-16	-6.276051e-17	9.164206e-17	1.584638e-16	6.070716e-16	-4.247268e-16	3.977061e-17	-2.761403e-18	0.098732	0.133447
V 5	0.173072	1.812612e-17	5.157519e-16	-6.539009e-17	-1.719944e-15	1.000000e+00	2.408382e-16	2.715541e-16	7.437229e-16	7.391702e-16	-3.920976e-16	1.253751e-16	-8.428683e-18	-1.149255e-15	4.808532e-16	4.319541e-16	6.590482e-16	-5.613951e-18	-0.386356	-0.094974
V6	-0.063016	-6.506567e-16	2.787346e-16	1.627627e-15	-7.491959e-16	2.408382e-16	1.000000e+00	1.191668e-16	-1.104219e-16	4.131207e-16	 5.833316e-17	-4.705235e-19	1.046712e-16	-1.071589e-15	4.562861e-16	-1.357067e-16	-4.452461e-16	2.594754e-16	0.215981	-0.043643
V7	0.084714	-1.005191e-15	2.055934e-16	4.895305e-16	-4.104503e-16	2.715541e-16	1.191668e-16	1.000000e+00	3.344412e-16	1.122501e-15	 -2.027779e-16	-8.898922e-16	-4.387401e-16	7.434913e-18	-3.094082e-16	-9.657637e-16	-1.782106e-15	-2.776530e-16	0.397311	-0.187257
V8	-0.036949	-2.433822e-16	-5.377041e-17	-1.268779e-15	5.697192e-16	7.437229e-16	-1.104219e-16	3.344412e-16	1.000000e+00	4.356078e-16	3.892798e-16	2.026927e-16	6.377260e-17	-1.047097e-16	-4.653279e-16	-1.727276e-16	1.299943e-16	-6.200930e-16	-0.103079	0.019875
V9	-0.008660	-1.513678e-16	1.978488e-17	5.568367e-16	6.923247e-16	7.391702e-16	4.131207e-16	1.122501e-15	4.356078e-16	1.000000e+00	1.936953e-16	-7.071869e-16	-5.214137e-16	-1.430343e-16	6.757763e-16	-7.888853e-16	-6.709655e-17	1.110541e-15	-0.044246	-0.097733
V10	0.030617	7.388135e-17	-3.991394e-16	1.156587e-15	2.232685e-16	-5.202306e-16	5.932243e-17	-7.492834e-17	-2.801370e-16	-4.642274e-16	1.177547e-15	-6.418202e-16	3.214491e-16	-1.355885e-16	-2.846052e-16	-3.028119e-16	-2.197977e-16	4.864782e-17	-0.101502	-0.216883
V11	-0.247689	2.125498e-16	1.975426e-16	1.576830e-15	3.459380e-16	7.203963e-16	1.980503e-15	1.425248e-16	2.487043e-16	1.354680e-16	-5.658364e-16	7.772895e-16	-4.505332e-16	1.933267e-15	-5.600475e-16	-1.003221e-16	-2.640281e-16	-3.792314e-16	0.000104	0.154876
V12	0.124348	2.053457e-16	-9.568710e-17	6.310231e-16	-5.625518e-16	7.412552e-16	2.375468e-16	-3.536655e-18	1.839891e-16	-1.079314e-15	7.300527e-16	1.644699e-16	1.800885e-16	4.436512e-16	-5.712973e-16	-2.359969e-16	-4.672391e-16	6.415167e-16	-0.009542	-0.260593
V13	-0.065902	-2.425603e-17	6.295388e-16	2.807652e-16	1.303306e-16	5.886991e-16	-1.211182e-16	1.266462e-17	-2.921856e-16	2.251072e-15	1.008461e-16	6.747721e-17	-7.132064e-16	-1.397470e-16	-5.497612e-16	-1.769255e-16	-4.720898e-16	1.144372e-15	0.005293	-0.004570
V14	-0.098757	-5.020280e-16	-1.730566e-16	4.739859e-16	2.282280e-16	6.565143e-16	2.621312e-16	2.607772e-16	-8.599156e-16	3.784757e-15	 -3.356561e-16	3.740383e-16	3.883204e-16	2.003482e-16	-8.547932e-16	-1.660327e-16	1.044274e-16	2.289427e-15	0.033751	-0.302544
V15	-0.183453	3.547782e-16	-4.995814e-17	9.068793e-16	1.377649e-16	-8.720275e-16	-1.531188e-15	-1.690540e-16	4.127777e-16	-1.051167e-15	6.605263e-17	-4.208921e-16	-3.912243e-16	-4.478263e-16	3.206423e-16	2.817791e-16	-1.143519e-15	-1.194130e-15	-0.002986	-0.004223
V16	0.011903	7.212815e-17	1.177316e-17	8.299445e-16	-9.614528e-16	2.246261e-15	2.623672e-18	5.869302e-17	-5.254741e-16	-1.214086e-15	-4.715090e-16	-7.923387e-17	5.020770e-16	-3.005985e-16	-1.345418e-15	-7.290010e-16	6.789513e-16	7.588849e-16	-0.003910	-0.196539
V17	-0.073297	-3.879840e-16	-2.685296e-16	7.614712e-16	-2.699612e-16	1.281914e-16	2.015618e-16	2.177192e-16	-2.269549e-16	1.113695e-15	-8.230527e-16	-8.743398e-16	3.706214e-16	-2.403828e-16	2.666806e-16	6.932833e-16	6.148525e-16	-5.534540e-17	0.007309	-0.326481
V18	0.090438	3.230206e-17	3.284605e-16	1.509897e-16	-5.103644e-16	5.308590e-16	1.223814e-16	7.604126e-17	-3.667974e-16	4.993240e-16	-9.408680e-16	-4.819365e-16	-1.912006e-16	-8.986916e-17	-6.629212e-17	2.990167e-16	2.242791e-16	7.976796e-16	0.035650	-0.111485
V19	0.028975	1.502024e-16	-7.118719e-18	3.463522e-16	-3.980557e-16	-1.450421e-16	-1.865597e-16	-1.881008e-16	-3.875186e-16	-1.376135e-16	5.115885e-16	-1.163768e-15	7.032035e-16	2.587708e-17	9.577163e-16	5.898033e-16	-2.959370e-16	-1.405379e-15	-0.056151	0.034783
V20	-0.050866	4.654551e-16	2.506675e-16	-9.316409e-16	-1.857247e-16	-3.554057e-16	-1.858755e-16	9.379684e-16	2.033737e-16	-2.343720e-16	-7.614597e-16	1.009285e-15	2.712885e-16	1.277215e-16	1.410054e-16	-2.803504e-16	-1.138829e-15	-2.436795e-16	0.339403	0.020090
V21	0.044736	-2.457409e-16	-8.480447e-17	5.706192e-17	-1.949553e-16	-3.920976e-16	5.833316e-17	-2.027779e-16	3.892798e-16	1.936953e-16	1.000000e+00	3.649908e-15	8.119580e-16	1.761054e-16	-1.686082e-16	-5.557329e-16	-1.211281e-15	5.278775e-16	0.105999	0.040413
V22	0.144059	-4.290944e-16	1.526333e-16	-1.133902e-15	-6.276051e-17	1.253751e-16	-4.705235e-19	-8.898922e-16	2.026927e-16	-7.071869e-16	 3.649908e-15	1.000000e+00	-7.303916e-17	9.970809e-17	-5.018575e-16	-2.503187e-17	8.461337e-17	-6.627203e-16	-0.064801	0.000805
V23					9.164206e-17															
V24					1.584638e-16															
V25					6.070716e-16															
V26					-4.247268e-16															
V27	-0.005135				3.977061e-17															
V28	-0.009413	2.083082e-15	-5.093836e-16	9.775546e-16	-2.761403e-18	-5.613951e-18	2.594754e-16	-2.776530e-16	-6.200930e-16	1.110541e-15	5.278775e-16	-6.627203e-16	1.481903e-15	-2.819805e-16	-7.008939e-16	-2.782204e-16	-3.061287e-16	1.000000e+00	0.010258	0.009536

```
#heatmap
 corr = df.corr()
plt.figure(figsize=(20,20))
heat = sns.heatmap(data=corr,annot=True)
plt.title('Heatmap of Correlation')
                                                                                                                                                                                                                                                                                                                                                                                           Heatmap of Correlation
                                                   0.12 -0.011 -0.42 -0.11 0.17 -0.0630.0850.0370.00870.031 -0.25 0.12 -0.0660.099 -0.18 0.012-0.073 0.09 0.029-0.0510.045 0.14 0.051-0.016-0.23 -0.0410.00510.00540.0110.012
                                                                                      1e-15.2e-15.2e-16.2e-16.5e-16.e-15.4e-15.5e-15.6e-15.1e-15.1e-15.4e-1-5.e-16.5e-15.2e-15.9e-15.2e-15.5e-16.7e-15.5e-16.3e-16.2e-16.4e-15.6e-17.2e-15.1e-15.1e-15.4e-1-15.2e-15.9e-15.2e-15.9e-15.2e-15.5e-16.7e-15.5e-16.3e-16.2e-15.4e-15.6e-17.2e-15.1e-15.4e-1-15.2e-15.4e-1-15.2e-15.2e-15.2e-15.2e-15.2e-15.2e-15.2e-15.2e-15.2e-15.2e-15.2e-15.2e-15.2e-15.2e-15.2e-15.2e-15.2e-15.2e-15.2e-15.2e-15.2e-15.2e-15.2e-15.2e-15.2e-15.2e-15.2e-15.2e-15.2e-15.2e-15.2e-15.2e-15.2e-15.2e-15.2e-15.2e-15.2e-15.2e-15.2e-15.2e-15.2e-15.2e-15.2e-15.2e-15.2e-15.2e-15.2e-15.2e-15.2e-15.2e-15.2e-15.2e-15.2e-15.2e-15.2e-15.2e-15.2e-15.2e-15.2e-15.2e-15.2e-15.2e-15.2e-15.2e-15.2e-15.2e-15.2e-15.2e-15.2e-15.2e-15.2e-15.2e-15.2e-15.2e-15.2e-15.2e-15.2e-15.2e-15.2e-15.2e-15.2e-15.2e-15.2e-15.2e-15.2e-15.2e-15.2e-15.2e-15.2e-15.2e-15.2e-15.2e-15.2e-15.2e-15.2e-15.2e-15.2e-15.2e-15.2e-15.2e-15.2e-15.2e-15.2e-15.2e-15.2e-15.2e-15.2e-15.2e-15.2e-15.2e-15.2e-15.2e-15.2e-15.2e-15.2e-15.2e-15.2e-15.2e-15.2e-15.2e-15.2e-15.2e-15.2e-15.2e-15.2e-15.2e-15.2e-15.2e-15.2e-15.2e-15.2e-15.2e-15.2e-15.2e-15.2e-15.2e-15.2e-15.2e-15.2e-15.2e-15.2e-15.2e-15.2e-15.2e-15.2e-15.2e-15.2e-15.2e-15.2e-15.2e-15.2e-15.2e-15.2e-15.2e-15.2e-15.2e-15.2e-15.2e-15.2e-15.2e-15.2e-15.2e-15.2e-15.2e-15.2e-15.2e-15.2e-15.2e-15.2e-15.2e-15.2e-15.2e-15.2e-15.2e-15.2e-15.2e-15.2e-15.2e-15.2e-15.2e-15.2e-15.2e-15.2e-15.2e-15.2e-15.2e-15.2e-15.2e-15.2e-15.2e-15.2e-15.2e-15.2e-15.2e-15.2e-15.2e-15.2e-15.2e-15.2e-15.2e-15.2e-15.2e-15.2e-15.2e-15.2e-15.2e-15.2e-15.2e-15.2e-15.2e-15.2e-15.2e-15.2e-15.2e-15.2e-15.2e-15.2e-15.2e-15.2e-15.2e-15.2e-15.2e-15.2e-15.2e-15.2e-15.2e-15.2e-15.2e-15.2e-15.2e-15.2e-15.2e-15.2e-15.2e-15.2e-15.2e-15.2e-15.2e-15.2e-15.2e-15.2e-15.2e-15.2e-15.2e-15.2e-15.2e-15.2e-15.2e-15.2e-15.2e-15.2e-15.2e-15.2e-15.2e-15.2e-15.2e-15.2e-15.2e-15.2e-15.2e-15.2e-15.2e-15.2e-15.2e-15.2e-15.2e-15.2e-15.2e-15.2e-15.2e-15.2e-15.2e-15.2e-15.2e-15.2e-15.2e-15.2e-15.2e-15.2e-15.2e-15.2e-15.2e-15.2e-15.2e-15.2e-15.2e-15.2e-15.2e-15.2e-15.2e-15.2e-15.2e-15.2e-15.2e-15.2e-15.2
                                                                                                                                                                                                                                    2e-115 1e-1461e-1459e-1 72e-152 4e-1152e-1266e-1155e-1256e-142e-141.2e-1159e-1169e-1469e-147.7e-13te-142.1e-1456e-1154e-1455e-1266e-16022 -0.04
                                 . 1085-1e-12 1e-1459e-14 1e-1257e-1252e-1 🔭 1 2.3e-1251e-1355e-1274e-135.5e-128e-1276e-1257e-1259e-1272e-1356e-1279e-1254e-142e-1464e-1464e-1254e-1254e-1254e-1254e-1254e-1254e-1254e-1254e-1254e-1254e-1254e-1254e-1254e-1254e-1254e-1254e-1254e-1254e-1254e-1254e-1254e-1254e-1254e-1254e-1254e-1254e-1254e-1254e-1254e-1254e-1254e-1254e-1254e-1254e-1254e-1254e-1254e-1254e-1254e-1254e-1254e-1254e-1254e-1254e-1254e-1254e-1254e-1254e-1254e-1254e-1254e-1254e-1254e-1254e-1254e-1254e-1254e-1254e-1254e-1254e-1254e-1254e-1254e-1254e-1254e-1254e-1254e-1254e-1254e-1254e-1254e-1254e-1254e-1254e-1254e-1254e-1254e-1254e-1254e-1254e-1254e-1254e-1254e-1254e-1254e-1254e-1254e-1254e-1254e-1254e-1254e-1254e-1254e-1254e-1254e-1254e-1254e-1254e-1254e-1254e-1254e-1254e-1254e-1254e-1254e-1254e-1254e-1254e-1254e-1254e-1254e-1254e-1254e-1254e-1254e-1254e-1254e-1254e-1254e-1254e-1254e-1254e-1254e-1254e-1254e-1254e-1254e-1254e-1254e-1254e-1254e-1254e-1254e-1254e-1254e-1254e-1254e-1254e-1254e-1254e-1254e-1254e-1254e-1254e-1254e-1254e-1254e-1254e-1254e-1254e-1254e-1254e-1254e-1254e-1254e-1254e-1254e-1254e-1254e-1254e-1254e-1254e-1254e-1254e-1254e-1254e-1254e-1254e-1254e-1254e-1254e-1254e-1254e-1254e-1254e-1254e-1254e-1254e-1254e-1254e-1254e-1254e-1254e-1254e-1254e-1254e-1254e-1254e-1254e-1254e-1254e-1254e-1254e-1254e-1254e-1254e-1254e-1254e-1254e-1254e-1254e-1254e-1254e-1254e-1254e-1254e-1254e-1254e-1254e-1254e-1254e-1254e-1254e-1254e-1254e-1254e-1254e-1254e-1254e-1254e-1254e-1254e-1254e-1254e-1254e-1254e-1254e-1254e-1254e-1254e-1254e-1254e-1254e-1254e-1254e-1254e-1254e-1254e-1254e-1254e-1254e-1254e-1254e-1254e-1254e-1254e-1254e-1254e-1254e-1254e-1254e-1254e-1254e-1254e-1254e-1254e-1254e-1254e-1254e-1254e-1254e-1254e-1254e-1254e-1254e-1254e-1254e-1254e-1254e-1254e-1254e-1254e-1254e-1254e-1254e-1254e-1254e-1254e-1254e-1254e-1254e-1254e-1254e-1254e-1254e-1254e-1254e-1254e-1254e-1254e-1254e-1254e-1254e-1254e-1254e-1254e-1254e-1254e-1254e-1254e-1254e-1254e-1254e-1254e-1254e-1254e-1254e-1254e-1254e-1254e-1254e-1254e-1254e-1254e-1254e-1254e-1254e-125
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                      - 0.6
                               ) 032/4e-1554e-1773e-1574e-1514e-151e-1653e-1 1 1 4e-1758e-1255e-1258e-1259e-1558e-1551e-1553e-1563e-1567e-1569e-162e-1664e-177.e-1674e-1764e-1764e-1767e-1167e-1167e-1167e-1167e-1167e-1167e-1167e-1167e-1167e-1167e-1167e-1167e-1167e-1167e-1167e-1167e-1167e-1167e-1167e-1167e-1167e-1167e-1167e-1167e-1167e-1167e-1167e-1167e-1167e-1167e-1167e-1167e-1167e-1167e-1167e-1167e-1167e-1167e-1167e-1167e-1167e-1167e-1167e-1167e-1167e-1167e-1167e-1167e-1167e-1167e-1167e-1167e-1167e-1167e-1167e-1167e-1167e-1167e-1167e-1167e-1167e-1167e-1167e-1167e-1167e-1167e-1167e-1167e-1167e-1167e-1167e-1167e-1167e-1167e-1167e-1167e-1167e-1167e-1167e-1167e-1167e-1167e-1167e-1167e-1167e-1167e-1167e-1167e-1167e-1167e-1167e-1167e-1167e-1167e-1167e-1167e-1167e-1167e-1167e-1167e-1167e-1167e-1167e-1167e-1167e-1167e-1167e-1167e-1167e-1167e-1167e-1167e-1167e-1167e-1167e-1167e-1167e-1167e-1167e-1167e-1167e-1167e-1167e-1167e-1167e-1167e-1167e-1167e-1167e-1167e-1167e-1167e-1167e-1167e-1167e-1167e-1167e-1167e-1167e-1167e-1167e-1167e-1167e-1167e-1167e-1167e-1167e-1167e-1167e-1167e-1167e-1167e-1167e-1167e-1167e-1167e-1167e-1167e-1167e-1167e-1167e-1167e-1167e-1167e-1167e-1167e-1167e-1167e-1167e-1167e-1167e-1167e-1167e-1167e-1167e-1167e-1167e-1167e-1167e-1167e-1167e-1167e-1167e-1167e-1167e-1167e-1167e-1167e-1167e-1167e-1167e-1167e-1167e-1167e-1167e-1167e-1167e-1167e-1167e-1167e-1167e-1167e
                       -0.252.1e-162e-16.6e-15.5e-1762e-162e-15.4e-18.5e-1864e-146.6e-1 1 5
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                      - 0.4
                             0122 le-1566e-1573e-1566e-1574e-1554e-1554e-1554e-1564e-1564e-1564e-1564e-1564e-1564e-1564e-1564e-1564e-1564e-1564e-1564e-1564e-1564e-1564e-1564e-1564e-1564e-1564e-1564e-1564e-1564e-1564e-1564e-1564e-1564e-1564e-1564e-1564e-1564e-1564e-1564e-1564e-1564e-1564e-1564e-1564e-1564e-1564e-1564e-1564e-1564e-1564e-1564e-1564e-1564e-1564e-1564e-1564e-1564e-1564e-1564e-1564e-1564e-1564e-1564e-1564e-1564e-1564e-1564e-1564e-1564e-1564e-1564e-1564e-1564e-1564e-1564e-1564e-1564e-1564e-1564e-1564e-1564e-1564e-1564e-1564e-1564e-1564e-1564e-1564e-1564e-1564e-1564e-1564e-1564e-1564e-1564e-1564e-1564e-1564e-1564e-1564e-1564e-1564e-1564e-1564e-1564e-1564e-1564e-1564e-1564e-1564e-1564e-1564e-1564e-1564e-1564e-1564e-1564e-1564e-1564e-1564e-1564e-1564e-1564e-1564e-1564e-1564e-1564e-1564e-1564e-1564e-1564e-1564e-1564e-1564e-1564e-1564e-1564e-1564e-1564e-1564e-1564e-1564e-1564e-1564e-1564e-1564e-1564e-1564e-1564e-1564e-1564e-1564e-1564e-1564e-1564e-1564e-1564e-1564e-1564e-1564e-1564e-1564e-1564e-1564e-1564e-1564e-1564e-1564e-1564e-1564e-1564e-1564e-1564e-1564e-1564e-1564e-1564e-1564e-1564e-1564e-1564e-1564e-1564e-1564e-1564e-1564e-1564e-1564e-1564e-1564e-1564e-1564e-1564e-1564e-1564e-1564e-1564e-1564e-1564e-1564e-1564e-1564e-1564e-1564e-1564e-1564e-1564e-1564e-1564e-1564e-1564e-1564e-1564e-1564e-1564e-1564e-1564e-1564e-1564e-1564e-1564e-1564e-1564e-1564e-1564e-1564e-1564e-1564e-1564e-1564e-1564e-1564e-1564e-1564e-1564e-1564e-1564e-1564e-1564e-1564e-1564e-1564e-1564e-1564e-1564e-1564e-1564e-1564e-1564e-1564e-1564e-1564e-1564e-1564e-1564e-1564e-1564e-1564e-1564e-1564e-1564e-1564e-1564e-1564e-1564e-1564e-1564e-1564e-1564e-1564e-1564e-1564e-1564e-1564e-1564e-1564e-1564e-1564e-1564e-1564e-1564e-1564e-1564e-1564e-1564e-1564e-1564e-1564e-1564e-1564e-1564e-1564e-1564e-1564e-1564e-1564e-1564e-1564e-1564e-1564e-1564e-1564e-1564e-1564e-1564e-1564e-1564e-1564e-1564e-1564e-1564e-1564e-1564e-1564e-1564e-1564e-1564e-1564e-1564e-1564e-1564e-1564e-1564e-1564e-1564e-1564e-1564e-1564e-1564e-1564e-1564e-1564e-1564e-1564e-1564e-1564e-1564e-1564e-1564e-1564
                         0.0662 4e-1673e-1658e-1659e-1659e-1659e-1659e-1759e-163e-154e-162e-1523e-1-1122e-154e-166e-1766e-1779e-166e-181e-1667e-1771e-164e-1655e-1668e-1467e-1601e-16000530.004
                               ).0995c-141.7c-1367c-1363c-1366c-1366c-1366c-1366c-1366c-1366c-1366c-1366c-1366c-1368c-1372c-1368c-1372c-1366c-1372c-1366c-1372c-1366c-1366c-1366c-1366c-1368c-1366c-1368c-1366c-1368c-1372c-1378c-1378c-1378c-1378c-1378c-1378c-1378c-1378c-1378c-1378c-1378c-1378c-1378c-1378c-1378c-1378c-1378c-1378c-1378c-1378c-1378c-1378c-1378c-1378c-1378c-1378c-1378c-1378c-1378c-1378c-1378c-1378c-1378c-1378c-1378c-1378c-1378c-1378c-1378c-1378c-1378c-1378c-1378c-1378c-1378c-1378c-1378c-1378c-1378c-1378c-1378c-1378c-1378c-1378c-1378c-1378c-1378c-1378c-1378c-1378c-1378c-1378c-1378c-1378c-1378c-1378c-1378c-1378c-1378c-1378c-1378c-1378c-1378c-1378c-1378c-1378c-1378c-1378c-1378c-1378c-1378c-1378c-1378c-1378c-1378c-1378c-1378c-1378c-1378c-1378c-1378c-1378c-1378c-1378c-1378c-1378c-1378c-1378c-1378c-1378c-1378c-1378c-1378c-1378c-1378c-1378c-1378c-1378c-1378c-1378c-1378c-1378c-1378c-1378c-1378c-1378c-1378c-1378c-1378c-1378c-1378c-1378c-1378c-1378c-1378c-1378c-1378c-1378c-1378c-1378c-1378c-1378c-1378c-1378c-1378c-1378c-1378c-1378c-1378c-1378c-1378c-1378c-1378c-1378c-1378c-1378c-1378c-1378c-1378c-1378c-1378c-1378c-1378c-1378c-1378c-1378c-1378c-1378c-1378c-1378c-1378c-1378c-1378c-1378c-1378c-1378c-1378c-1378c-1378c-1378c-1378c-1378c-1378c-1378c-1378c-1378c-1378c-1378c-1378c-1378c-1378c-1378c-1378c-1378c-1378c-1378c-1378c-1378c-1378c-1378c-1378c-1378c-1378c-1378c-1378c-1378c-1378c-1378c-1378c-1378c-1378c-1378c-1378c-1378c-1378c-1378c-1378c-1378c-1378c-1378c-1378c-1378c-1378c-1378c-1378c-1378c-1378c-1378c-1378c-1378c-1378c-1378c-1378c-1378c-1378c-1378c-1378c-1378c-1378c-1378c-1378c-1378c-1378c-1378c-1378c-1378c-1378c-1378c-1378c-1378c-1378c-1378c-1378c-1378c-1378c-1378c-1378c-1378c-1378c-1378c-1378c-1378c-1378c-1378c-1378c-1378c-1378c-1378c-1378c-1378c-1378c-1378c-1378c-1378c-1378c-1378c-1378c-1378c-1378c-1378c-1378c-1378c-1378c-1378c-1378c-1378c-1378c-1378c-1378c-1378c-1378c-1378c-1378c-1378c-1378c-1378c-1378c-1378c-1378c-1378c-1378c-1378c-1378c-1378c-1378c-1378c-1378c-1378c-1378c-1378c-1378c-1378c-1378c-1378c-1378c-1378c-1378c-1378c-1378c-137
                         -0.183 5e-165e-179.1e-1154e-185.7e-1155e-1157e-1861e-1851e-1858e-1153e-1354e-1354e-1354e-1358e-171 _ .3e-1656e-1355e-1355e-1358e-1366e-147.2e-2559e-1455e-1352e-1358e-1351e-1352e-135
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                               ).017/2e-1172e-1973e-1866e-1862e-1866e-1969e-1973e-1862e-1868e-1868e-186e-196.4e-1853e-15 1 25e-184e-1853e-1852e-146.7e-1859e-196-163e-161.3e-1853e-1868e-1860039-0.2
      20.073.9e-1257e-1256e-1257e-1256e-1257e-1254e-1254e-1254e-1254e-1254e-1254e-1254e-1254e-1254e-1254e-1254e-1254e-1254e-1254e-1254e-1254e-1254e-1254e-1254e-1254e-1254e-1254e-1254e-1254e-1254e-1254e-1254e-1254e-1254e-1254e-1254e-1254e-1254e-1254e-1254e-1254e-1254e-1254e-1254e-1254e-1254e-1254e-1254e-1254e-1254e-1254e-1254e-1254e-1254e-1254e-1254e-1254e-1254e-1254e-1254e-1254e-1254e-1254e-1254e-1254e-1254e-1254e-1254e-1254e-1254e-1254e-1254e-1254e-1254e-1254e-1254e-1254e-1254e-1254e-1254e-1254e-1254e-1254e-1254e-1254e-1254e-1254e-1254e-1254e-1254e-1254e-1254e-1254e-1254e-1254e-1254e-1254e-1254e-1254e-1254e-1254e-1254e-1254e-1254e-1254e-1254e-1254e-1254e-1254e-1254e-1254e-1254e-1254e-1254e-1254e-1254e-1254e-1254e-1254e-1254e-1254e-1254e-1254e-1254e-1254e-1254e-1254e-1254e-1254e-1254e-1254e-1254e-1254e-1254e-1254e-1254e-1254e-1254e-1254e-1254e-1254e-1254e-1254e-1254e-1254e-1254e-1254e-1254e-1254e-1254e-1254e-1254e-1254e-1254e-1254e-1254e-1254e-1254e-1254e-1254e-1254e-1254e-1254e-1254e-1254e-1254e-1254e-1254e-1254e-1254e-1254e-1254e-1254e-1254e-1254e-1254e-1254e-1254e-1254e-1254e-1254e-1254e-1254e-1254e-1254e-1254e-1254e-1254e-1254e-1254e-1254e-1254e-1254e-1254e-1254e-1254e-1254e-1254e-1254e-1254e-1254e-1254e-1254e-1254e-1254e-1254e-1254e-1254e-1254e-1254e-1254e-1254e-1254e-1254e-1254e-1254e-1254e-1254e-1254e-1254e-1254e-1254e-1254e-1254e-1254e-1254e-1254e-1254e-1254e-1254e-1254e-1254e-1254e-1254e-1254e-1254e-1254e-1254e-1254e-1254e-1254e-1254e-1254e-1254e-1254e-1254e-1254e-1254e-1254e-1254e-1254e-1254e-1254e-1254e-1254e-1254e-1254e-1254e-1254e-1254e-1254e-1254e-1254e-1254e-1254e-1254e-1254e-1254e-1254e-1254e-1254e-1254e-1254e-1254e-1254e-1254e-1254e-1254e-1254e-1254e-1254e-1254e-1254e-1254e-1254e-1254e-1254e-1254e-1254e-1254e-1254e-1254e-1254e-1254e-1254e-1254e-1254e-1254e-1254e-1254e-1254e-1254e-1254e-1254e-1254e-1254e-1254e-1254e-1254e-1254e-1254e-1254e-1254e-1254e-1254e-1254e-1254e-1254e-1254e-1254e-1254e-1254e-1254e-1254e-1254e-1254e-1254e-1254e-1254e-1254e-1254e-1254e-1254e-1254e-1254e-1254e-1254e-1254e-1254e-12
                               0.093.2e-1373e-1355e-1351e-1363e-1352e-1352e-1356e-1373e-146e-1363e-1364e-1468e-137.2e-156e-1355e-1354e-1459e-1.1 2.5e-1354e-1458e-1369e-139e-1356e-136-142
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                                 .04⊊.5e-1855e-187e-1179e-1859e-1869e-186e-112e-169e-1162e-15.7e-175e-16e-16e-169e-186e-147.7e-1862e-1864e-169e-169e-1159e-186e-1113.6e-1851e-1159e-186e-1157e-1866e-1162e-1863e-1169e-1169e-1169e-1169e-1169e-1169e-1169e-1169e-1169e-1169e-1169e-1169e-1169e-1169e-1169e-1169e-1169e-1169e-1169e-1169e-1169e-1169e-1169e-1169e-1169e-1169e-1169e-1169e-1169e-1169e-1169e-1169e-1169e-1169e-1169e-1169e-1169e-1169e-1169e-1169e-1169e-1169e-1169e-1169e-1169e-1169e-1169e-1169e-1169e-1169e-1169e-1169e-1169e-1169e-1169e-1169e-1169e-1169e-1169e-1169e-1169e-1169e-1169e-1169e-1169e-1169e-1169e-1169e-1169e-1169e-1169e-1169e-1169e-1169e-1169e-1169e-1169e-1169e-1169e-1169e-1169e-1169e-1169e-1169e-1169e-1169e-1169e-1169e-1169e-1169e-1169e-1169e-1169e-1169e-1169e-1169e-1169e-1169e-1169e-1169e-1169e-1169e-1169e-1169e-1169e-1169e-1169e-1169e-1169e-1169e-1169e-1169e-1169e-1169e-1169e-1169e-1169e-1169e-1169e-1169e-1169e-1169e-1169e-1169e-1169e-1169e-1169e-1169e-1169e-1169e-1169e-1169e-1169e-1169e-1169e-1169e-1169e-1169e-1169e-1169e-1169e-1169e-1169e-1169e-1169e-1169e-1169e-1169e-1169e-1169e-1169e-1169e-1169e-1169e-1169e-1169e-1169e-1169e-1169e-1169e-1169e-1169e-1169e-1169e-1169e-1169e-1169e-1169e-1169e-1169e-1169e-1169e-1169e-1169e-1169e-1169e-1169e-1169e-1169e-1169e-1169e-1169e-1169e-1169e-1169e-1169e-1169e-1169e-1169e-1169e-1169e-1169e-1169e-1169e-1169e-1169e-1169e-1169e-1169e-1169e-1169e-1169e-1169e-1169e-1169e-1169e-1169e-1169e-1169e-1169e-1169e-1169e-1169e-1169e-1169e-1169e-1169e-1169e-1169e-1169e-1169e-1169e-1169e-1169e-1169e-1169e-1169e-1169e-1169e-1169e-1169e-1169e-1169e-1169e-1169e-1169e-1169e-1169e-1169e-1169e-1169e-1169e-1169e-1169e-1169e-1169e-1169e-1169e-1169e-1169e-1169e-1169e-1169e-1169e-1169e-1169e-1169e-1169e-1169e-1169e-1169e-1169e-1169e-1169e-1169e-1169e-1169e-1169e-1169e-1169e-1169e-1169e-1169e-1169e-1169e-1169e-1169e-1169e-1169e-1169e-1169e-1169e-1169e-1169e-1169e-1169e-1169e-1169e-1169e-1169e-1169e-1169e-1169e-1169e-1169e-1169e-1169e-1169e-1169e-1169e-1169e-1169e-1169e-1169e-1169e-1169e-1169e-1169e-1169e-1169e-1169e-116
                               0.144.3e-165e-115.1e-165e-175e-146.7e-1899e-18e-167.1e-165e-166e-166e-167e-177e-146.2e-1759e-187e-1468e-162e-159e-156e-1 7.3e-17e-16-5e-192.5e-175e-1876e-140.060.0008
                                  05 ib. 2e- 1156e- 165e- 16- 2e- 137. 4e- 13e- 164. 4e- 1542e- 1542e- 1562e- 156. 2e- 1161e- 1569e- 1569e- 1569e- 167. 9e- 1569e- 169- 167. 9e- 1569e- 1569e-
                                 ) 014-4e-172e-172e-173e-175e-1751e-1751e-1751e-1754e-1764e-1764e-1764e-1764e-1764e-1764e-1764e-1764e-1764e-1764e-1764e-1764e-1764e-1764e-1764e-1764e-1764e-1764e-1764e-1764e-1764e-1764e-1764e-1764e-1764e-1764e-1764e-1764e-1764e-1764e-1764e-1764e-1764e-1764e-1764e-1764e-1764e-1764e-1764e-1764e-1764e-1764e-1764e-1764e-1764e-1764e-1764e-1764e-1764e-1764e-1764e-1764e-1764e-1764e-1764e-1764e-1764e-1764e-1764e-1764e-1764e-1764e-1764e-1764e-1764e-1764e-1764e-1764e-1764e-1764e-1764e-1764e-1764e-1764e-1764e-1764e-1764e-1764e-1764e-1764e-1764e-1764e-1764e-1764e-1764e-1764e-1764e-1764e-1764e-1764e-1764e-1764e-1764e-1764e-1764e-1764e-1764e-1764e-1764e-1764e-1764e-1764e-1764e-1764e-1764e-1764e-1764e-1764e-1764e-1764e-1764e-1764e-1764e-1764e-1764e-1764e-1764e-1764e-1764e-1764e-1764e-1764e-1764e-1764e-1764e-1764e-1764e-1764e-1764e-1764e-1764e-1764e-1764e-1764e-1764e-1764e-1764e-1764e-1764e-1764e-1764e-1764e-1764e-1764e-1764e-1764e-1764e-1764e-1764e-1764e-1764e-1764e-1764e-1764e-1764e-1764e-1764e-1764e-1764e-1764e-1764e-1764e-1764e-1764e-1764e-1764e-1764e-1764e-1764e-1764e-1764e-1764e-1764e-1764e-1764e-1764e-1764e-1764e-1764e-1764e-1764e-1764e-1764e-1764e-1764e-1764e-1764e-1764e-1764e-1764e
                          .0.239.6e-1455e-1161e-1151e-1468e-1466e-145.1e-1467e-1658e-125.8e-1256e-1655e-1655e-1652e-115.8e-1257e-1456e-1976e-1154e-115.7e-1.5e-1.6.2e-1.7e-1.5
                               ) 0.411. 6e-1271.e-1362e-1463e-145.4e-1367e-1367e-1367e-1369e-161e-142. 4e-1368e-1367e-1268e-136.9e-1369e-1369e-136.8e-1366e-1255e-1371e-1358e-1366e-125
                                  009241e-15.1e-1938e-1258e-1258e-1258e-1258e-1258e-1258e-1258e-1258e-1258e-1258e-1258e-1258e-1254e-1258e-1254e-1258e-1258e-1258e-1258e-1258e-1258e-1258e-1258e-1258e-1258e-1258e-1258e-1258e-1258e-1258e-1258e-1258e-1258e-1258e-1258e-1258e-1258e-1258e-1258e-1258e-1258e-1258e-1258e-1258e-1258e-1258e-1258e-1258e-1258e-1258e-1258e-1258e-1258e-1258e-1258e-1258e-1258e-1258e-1258e-1258e-1258e-1258e-1258e-1258e-1258e-1258e-1258e-1258e-1258e-1258e-1258e-1258e-1258e-1258e-1258e-1258e-1258e-1258e-1258e-1258e-1258e-1258e-1258e-1258e-1258e-1258e-1258e-1258e-1258e-1258e-1258e-1258e-1258e-1258e-1258e-1258e-1258e-1258e-1258e-1258e-1258e-1258e-1258e-1258e-1258e-1258e-1258e-1258e-1258e-1258e-1258e-1258e-1258e-1258e-1258e-1258e-1258e-1258e-1258e-1258e-1258e-1258e-1258e-1258e-1258e-1258e-1258e-1258e-1258e-1258e-1258e-1258e-1258e-1258e-1258e-1258e-1258e-1258e-1258e-1258e-1258e-1258e-1258e-1258e-1258e-1258e-1258e-1258e-1258e-1258e-1258e-1258e-1258e-1258e-1258e-1258e-1258e-1258e-1258e-1258e-1258e-1258e-1258e-1258e-1258e-1258e-1258e-1258e-1258e-1258e-1258e-1258e-1258e-1258e-1258e-1258e-1258e-1258e-1258e-1258e-1258e-1258e-1258e-1258e-1258e-1258e-1258e-1258e-1258e-1258e-1258e-1258e-1258e-1258e-1258e-1258e-1258e-1258e-1258e-1258e-1258e-1258e-1258e-1258e-1258e-1258e-1258e-1258e-1258e-1258e-1258e-1258e-1258e-1258e-1258e-1258e-1258e-1258e-1258e-1258e-1258e-1258e-1258e-1258e-1258e-1258e-1258e-1258e-1258e-1258e-1258e-1258e-1258e-1258e-1258e-1258e-1258e-1258e-1258e-1258e-1258e-1258e-1258e-1258e-1258e-1258e-1258e-1258e-1258e-1258e-1258e-1258e-1258e-1258e-1258e-1258e-1258e-1258e-1258e-1258e-1258e-1258e-1258e-1258e-1258e-1258e-1258e-1258e-1258e-1258e-1258e-1258e-1258e-1258e-1258e-1258e-1258e-1258e-1258e-1258e-1258e-1258e-1258e-1258e-1258e-1258e-1258e-1258e-1258e-1258e-1258e-1258e-1258e-1258e-1258e-1258e-1258e-1258e-1258e-1258e-1258e-1258e-1258e-1258e-1258e-1258e-1258e-1258e-1258e-1258e-1258e-1258e-1258e-1258e-1258e-1258e-1258e-1258e-1258e-1258e-1258e-1258e-1258e-1258e-1258e-1258e-1258e-1258e-1258e-1258e-1258e-1258e-1258e-1258e-1258e-1258e-1258e-1258
                          0011-0.23 -0.53 -0.21 0.099 -0.39 0.22 0.4 -0.1 -0.044 -0.1 0.0000.0096.00530 034-0.0030.0036-0.056 0.34 0.11 -0.065-0.110.00510.0480 00320 029 0.01 1
                       0.012 0.1 0.091 0.19 0.13 0.0950 044 0.19 0.02 0.098 0.22 0.15 0.260 0046 0.3 0.0042 0.2 0.33 0.11 0.035 0.02 0.040 00000 0020 0.070 0030 00450 0.180 0095 0.056
                                                                                                                                                                                                                                  Data Preprocessing
```

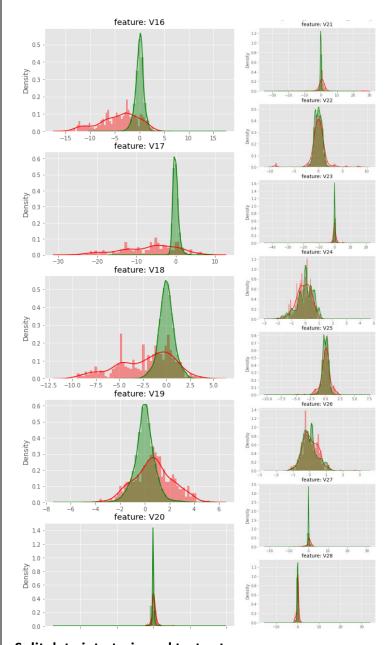
Missing data
df.isnull().values.any()

```
False
Feature Scaling
scaler = StandardScaler()
scaler2 = StandardScaler()
#scaling time
scaled time = scaler.fit transform(df[['Time']])
flat list1 = [item for sublist in scaled time.tolist() for item in sublist]
scaled time = pd.Series(flat list1)
#scaling the amount column
scaled amount = scaler2.fit transform(df[['Amount']])
flat list2 = [item for sublist in scaled amount.tolist() for item in sublist]
scaled amount = pd.Series(flat list2)
#concatenating newly created columns w original df
df = pd.concat([df, scaled_amount.rename('scaled_amount'), scaled_time.rename('
scaled time')], axis=1)
df.sample(5)
       Time
                                                               V23
                                                                                         V28 Amount Class scaled_amount scaled_time
 98975 66903.0 1.289482 -1.582951 0.348539 -1.520838 -1.581663 0.005741 -1.281381 0.079842 -1.673657 .... -0.206424 -0.524138 0.347005 -0.078579 0.019208 0.026865 128.00 0 0.158526 -0.587745
 153407 9893.0 -0.632977 -0.486623 1.385542 -0.970855 -0.044483 0.426488 0.734698 -0.521861 0.497694 .... -0.686892 -0.419792 1.055355 0.507998 -0.41932 -0.406969 139.00
                                                                                                      0.202505
                                                                                                             0.086846
 89025 6239.0 0.784985 -0.690212 0.894514 1.299230 -0.74628 -0.60667 0.396667 0.396667 0.633693 ... -0.242930 -0.315704 0.346549 -0.223209 0.041405 0.045083 170.00
 135501 81282.0 1,192938 0,119649 0,035486 1,212958 0,221914 0,292477 0,057719 0,044891 0,379221 .... -0,177587 -0,763538 0,761675 -0,261159 0,034483 0,009699 24.19
                                                                                                      -0.256516
                                                                                                            -0.284953
 168808 119393.0 2.090275 -0.455652 -1.876569 -1.454087 -0.174865 -1.854779 0.400016 -0.505552 1.495054 .... 0.002438 0.033655 0.278185 -0.108404 -0.041460 -0.066570 30.00 0
5 rows × 33 columns
plot, (axis1, axis2) = plt.subplots(2, 1)
axis1.scatter(fraud.Time, fraud.Amount)
axis1.set title('Fraud')
axis2.scatter(genuine.Time, genuine.Amount)
axis2.set title('Genuine')
plt.xlabel('Time')
plt.ylabel('Amount')
plot.suptitle('Time vs Amount of transaction')
#plt.show();
Text(0.5, 0.98, 'Time vs Amount of transaction')
                    Time vs Amount of transaction
                                Fraud
     2000
     1000
                       50000 76enuine00 125000 150000 175000
                25000
    20000
   10000
                25000 50000 75000 100000 125000 150000 175000
                                 Time
```

10

By seeing the graph we can say that they have nothing much information to prove that transaction is fraud. So it is not having any prediction power coz of it we can simply drop the time variable from dataset.

```
#dropping old amount and time columns
df.drop(['Amount', 'Time'], axis=1, inplace=True)
#let us check correlations and shapes of those 25 principal components.
# Features V1, V2, ... V28 are the principal components obtained with PCA.
import seaborn as sns
import matplotlib.gridspec as gridspec
gs = gridspec.GridSpec(28, 1)
plt.figure(figsize=(6,28*4))
for i, col in enumerate(df[df.iloc[:,0:28].columns]):
      ax5 = plt.subplot(gs[i])
      sns.distplot(df[col][df.Class == 1], bins=50, color='r')
      sns.distplot(df[col][df.Class == 0], bins=50, color='g')
      ax5.set xlabel('')
      ax5.set title('feature: ' + str(col))
plt.show()
                feature: V1
  0.40
                                                                                     reature: VII
                                          -100
                                                  -60 -40 -20
feature: V6
                                                                       0.35
  0.35
  0.30
                                                                       0.30
  0.25
                                                                       0.25
  0.20
                                                                       0.20
  0.15
                                                                      ē 0.15
  0.10
                                     ā 0.2
                                                                       0.10
  0.05
                                                                       0.05
                                      0.1
                feature: V2
                                                                       0.00
                                                                                                   12.5 15.0
                                                                              -2.5
                                                                                     2.5 5.0 7.5
feature: V12
                                      0.0
  0.40
                                                   feature: V7
  0.35
  0.30
  0.25
                                                                        0.4
  0.20
                                                                       0.3
                                     A 0.3
  0.15
  0.10
  0.05
                                                                        0.1
  0.00
                feature: V3
                                      0.0
                                                                                     -10 -5
feature: V13
                                                  feature: V8
  0.30
  0.25
  0.20
                                      0.8
                                                                        0.3
  0.15
                                     S 0.6
  0.10
  0.05
                                                                        0.1
                                      0.2
  0.00
                feature: V4
                                                   feature: V9
                                                                                     feature: V14
  0.35
                                                                        0.6
  0.30
                                                                        0.5
  0.25
£ 0.20
O 0.15
                                                                        0.3
                                     G 0.2
                                      0.1
  0.05
                                                                        0.1
                                      0.0
                                                                        0.0
                feature: V5
                                                  feature: V10
                                                                                     feature: V15
  0.40
  0.35
                                                                        0.5
                                      0.5
  0.30
                                                                        0.4
 0.25
                                                                       0.3
  0.20
  0.15
  0.10
  0.05
                                                  feature: V11
                feature: V6
```

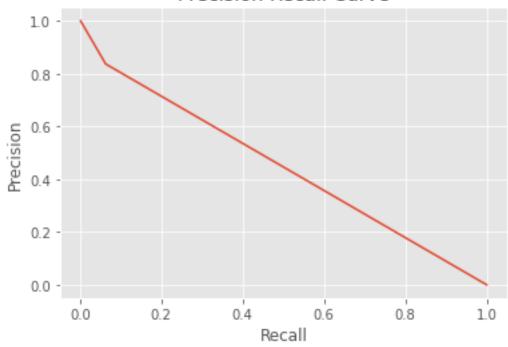


Split data into train and test set

```
fraud cases in test-set:
# splitting dataset to train & test dataset
from sklearn.model selection import train test split
X train, X test, y train, y test = train test split(X, y, test size=0.3, random
state=0)
print(X train.shape)
print(X test.shape)
print(y train.shape)
print(y test.shape)
(199364, 30)
(85443, 30)
(199364,)
(85443,)
Model Building using Naive Bayes
from sklearn.naive bayes import GaussianNB
from sklearn.metrics import confusion matrix
from sklearn.metrics import classification report
from sklearn.metrics import roc curve, auc, precision recall curve, roc curve
NBclf=GaussianNB()
NBclf.fit(X train, y train)
NB pred, NB pred prob=NBclf.predict(X test), NBclf.predict proba(X test)
acc score = NBclf.score(X test, y test)
print(f'Accuracy of model on test dataset :- {acc score}')
# predict result using test dataset
y pred = NBclf.predict(X test)
# confusion matrix
print(f"Confusion Matrix :- \n {confusion matrix(y test, y pred)}")
# classification report for f1-score
print(f"Classification Report :- \n {classification report(y test, y pred)}")
precision, recall, thresholds = precision recall curve(y test, y pred)
# Plot ROC curve
plt.plot(precision, recall)
plt.xlabel('Recall')
plt.ylabel('Precision')
plt.title('Precision Recall Curve')
plt.show()
Accuracy of model on test dataset :- 0.9784651756141521
Confusion Matrix :-
 [[83480 1816]
 [ 24
         12311
Classification Report :-
               precision recall f1-score
                                                support
                                                 85296
           0
                   1.00
                             0.98
                                        0.99
           1
                   0.06
                             0.84
                                        0.12
                                                   147
    accuracy
                                        0.98
                                                 85443
```

macro avg 0.53 0.91 0.55 85443 weighted avg 1.00 0.98 0.99 85443

Precision Recall Curve



7.7 Results and Discussion:

Naïve Bayes classifier is used to solve the credit card fraud detection problem over a skewed dataset. The model is 98% accurate.