

# Résolution de niveaux du Sokoban

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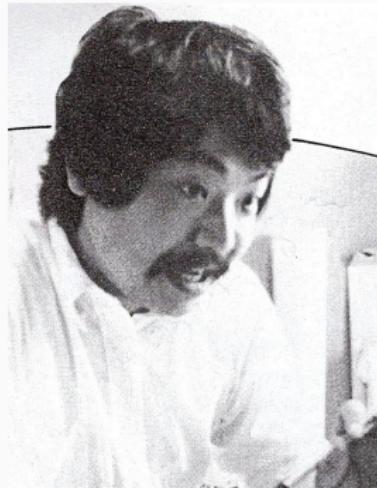
Nom Prénom

Candidat n°01234

# Introduction

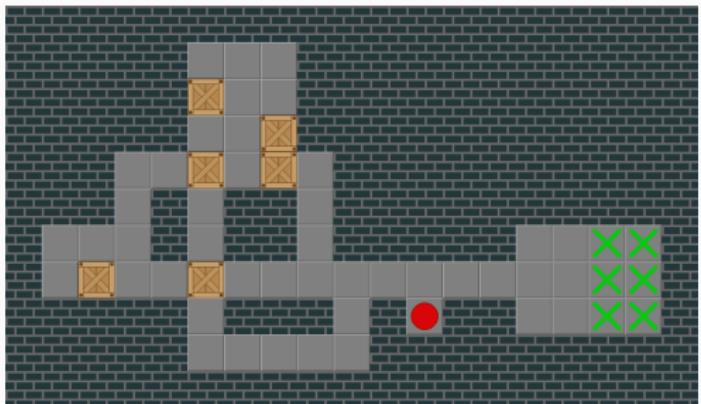
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# Le jeu du Sokoban



<https://shmuulations.com/wp-content/uploads/2022/03/thinkingrabbit04.jpg>

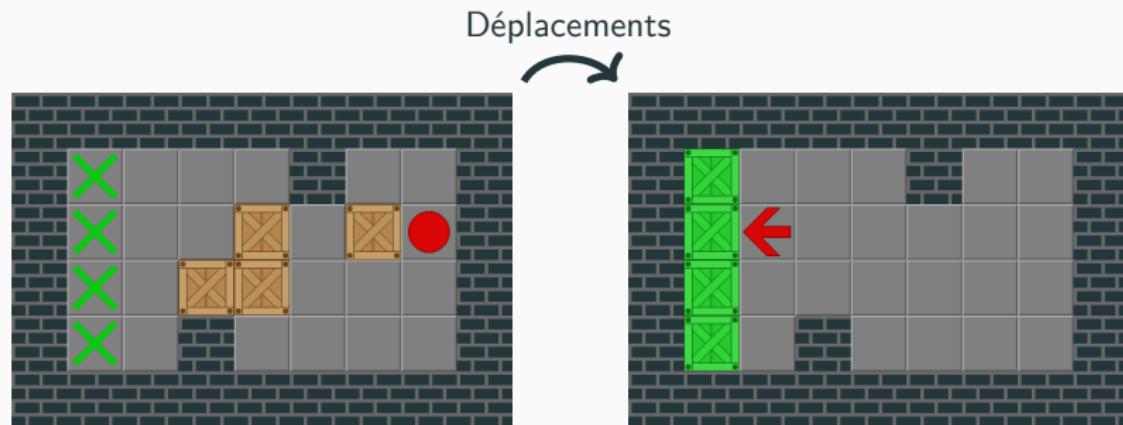
Hiroyuki Imabayashi



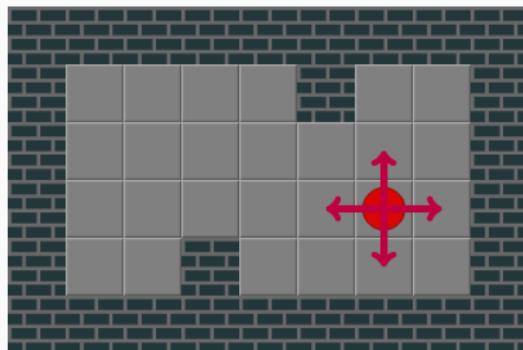
*X*Sokoban

Problème **PSPACE-complet**

# But du jeu

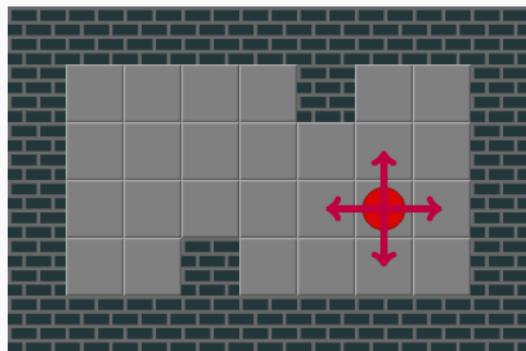


# Règles

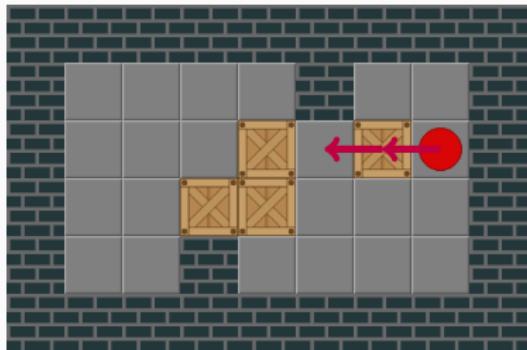


Déplacements autorisés

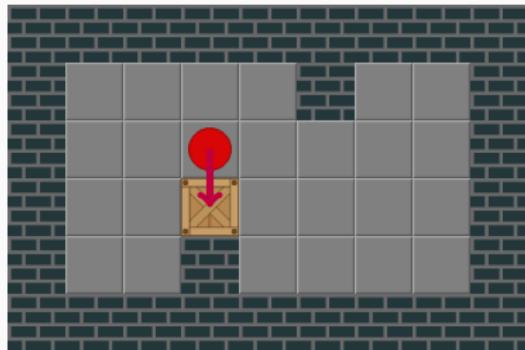
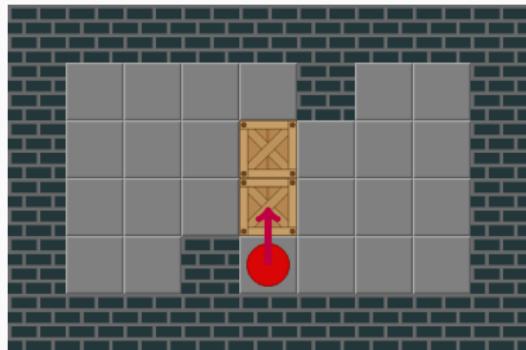
# Règles



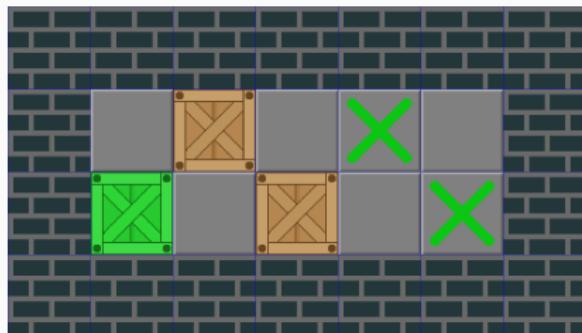
Déplacements autorisés



# Règles



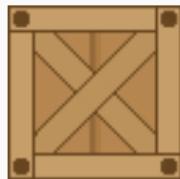
# Tuiles



Mur



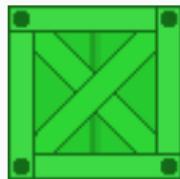
Sol



Caisse



Cible



Caisse sur une cible

# Quelles stratégies adopter pour trouver une solution le plus rapidement possible à un niveau de Sokoban ?

```
Welcome to sokoshell - Version 1.0
Type 'help' to show help. More help for a command with 'help command'
sokoshell> █
```

# Plan

Introduction

Principe de résolution

Réduction de l'espace de recherche

Analyse statique

Analyse dynamique

Recherche dirigée par une heuristique

Optimisations

Résultats

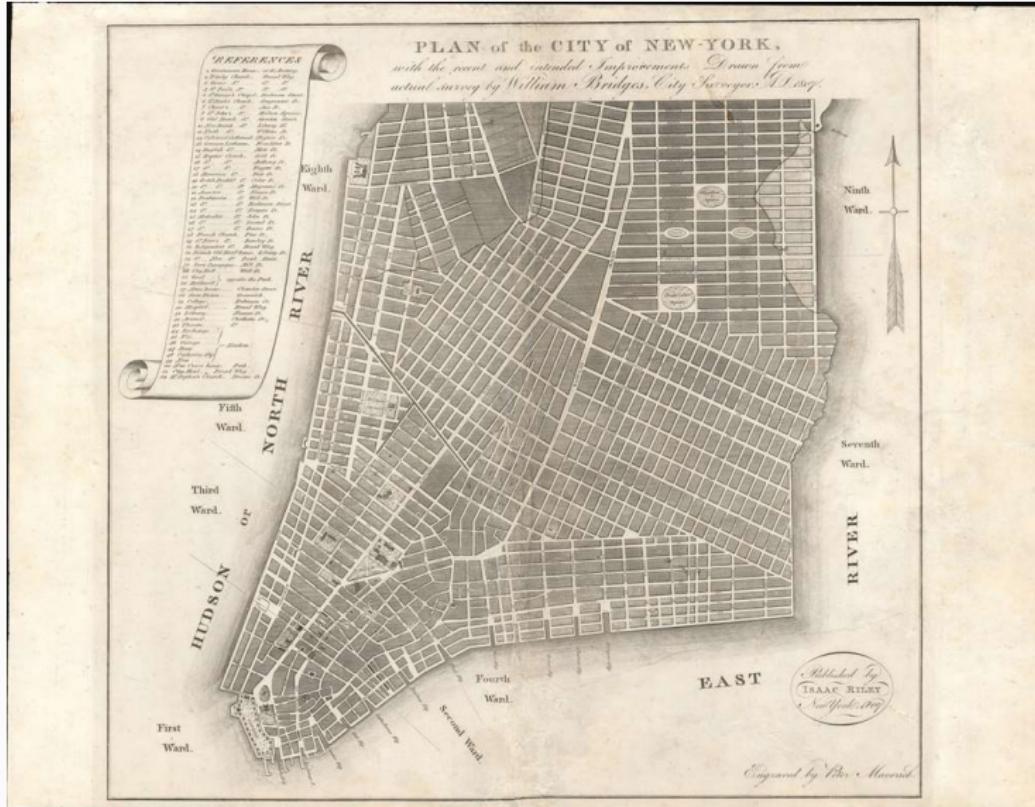
Annexe

## Lien avec le thème de l'année



Source : *Indiana Jones et les Aventuriers de l'arche perdue* (scène de fin), Steven Spielberg, 1981  
<https://pbs.twimg.com/media/EyjVShEVEAAQZjK.jpg>

# Lien avec le thème de l'année

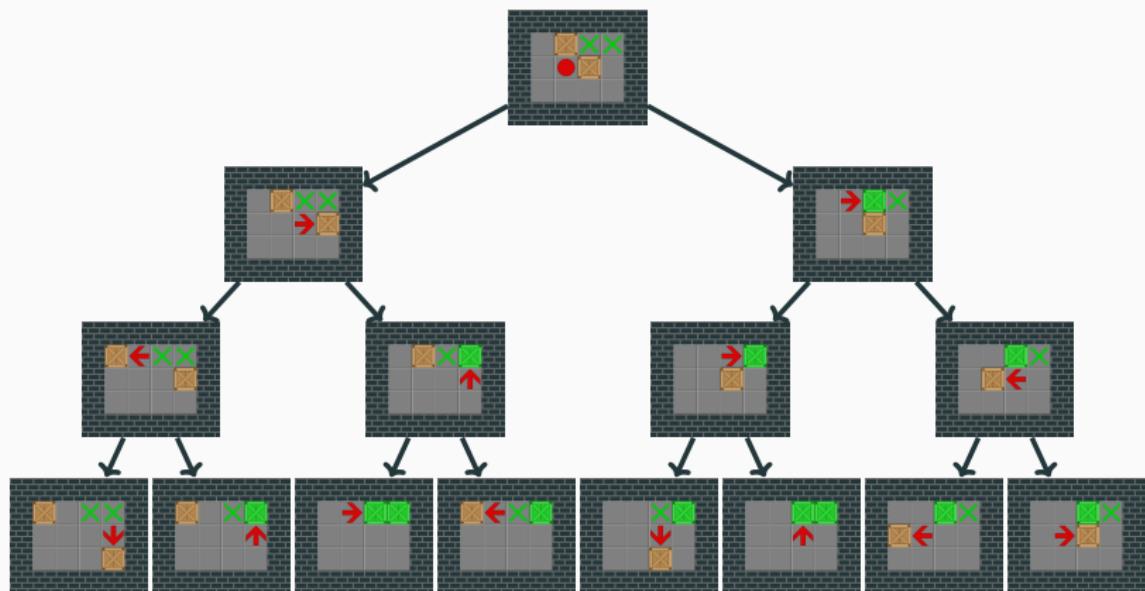


Source : <https://www.geographicus.com/mm5/graphics/00000001/L/NewYork-bridgesmaverick-1807.jpg>

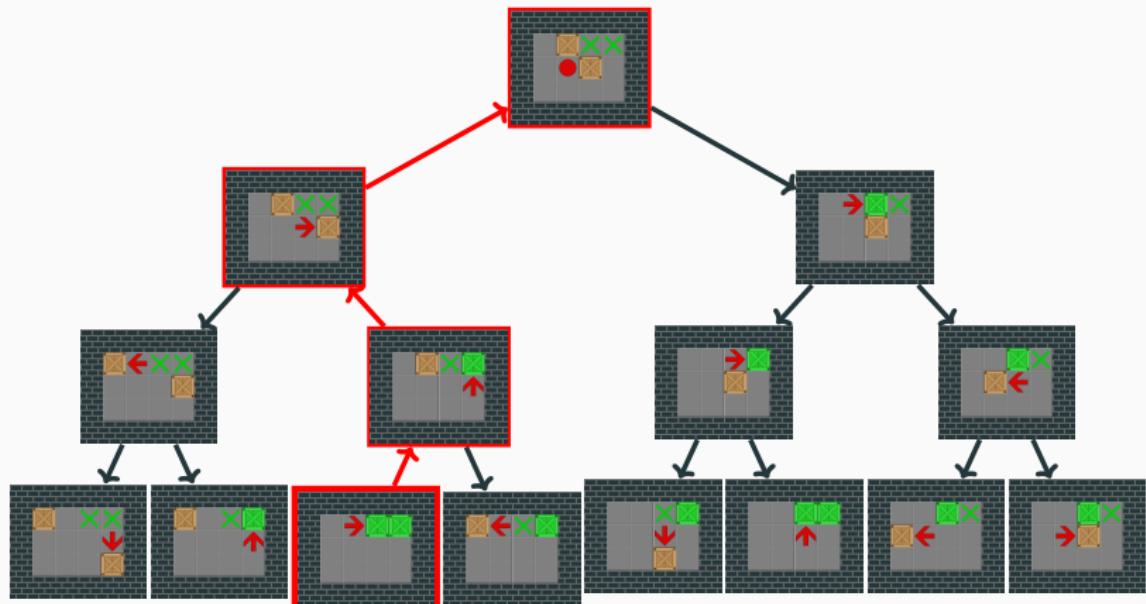
## Principe de résolution

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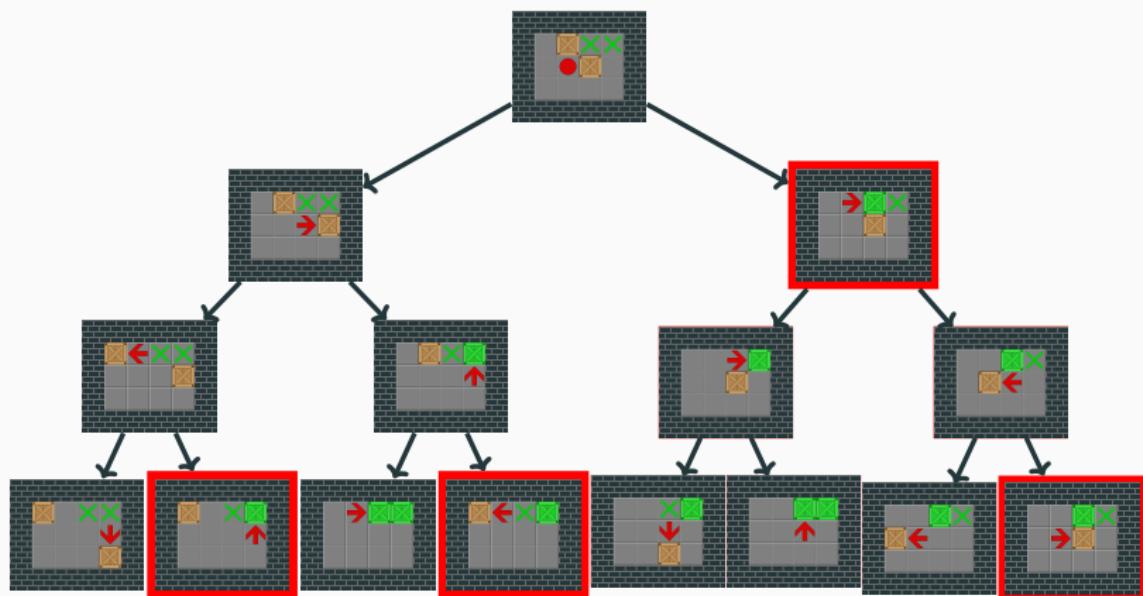
# Arbre des états



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## Calcul du *hash* d'un état - Hash de Zobrist

Propriétés du **XOR** :

1.  $a \text{XOR } a = 0$
2. **XOR** commutatif, associatif
3. **XOR** préserve l'aléatoire

Initialisation :

$$T = \begin{pmatrix} \text{caisse} & \text{joueur} & \text{case} \\ 6357 & 01234 & 0 \\ -1378 & 42 & 1 \\ \vdots & \vdots & \vdots \\ 93268 & -278 & wh - 1 \end{pmatrix}$$

## Calcul du *hash* d'un état - Hash de Zobrist

- $(c_1, \dots, c_n)$   $n$  caisses et  $p$  position du joueur :

$$h = \bigoplus_{i=0}^n T[c_i][0] \text{ XOR } T[p][1]$$

en  $\mathcal{O}(n)$

- **Connaissant le hash de l'état parent** :  $c_i \rightarrow c'_i, p \rightarrow p'$

$$h' = h \text{ XOR } T[c_i][0] \text{ XOR } T[c'_i][0] \text{ XOR } T[p][1] \text{ XOR } T[p'][1]$$

en  $\mathcal{O}(1)$

## Réduction de l'espace de recherche

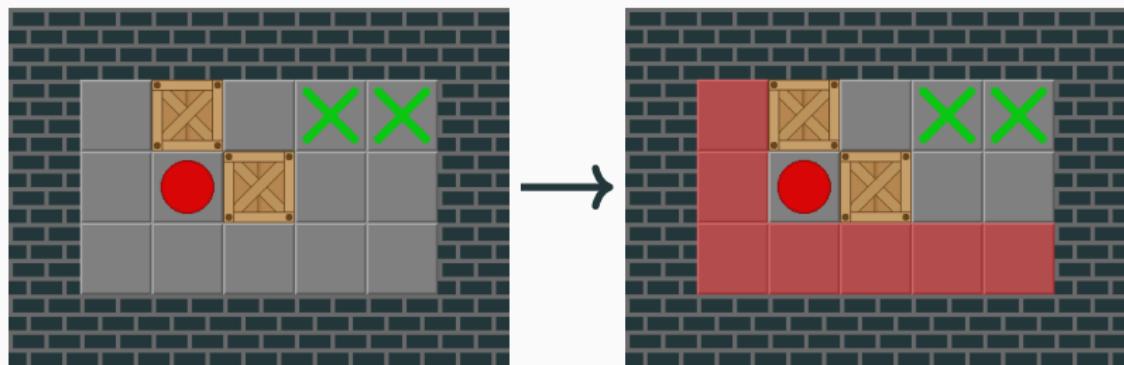
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# Réduction de l'espace de recherche

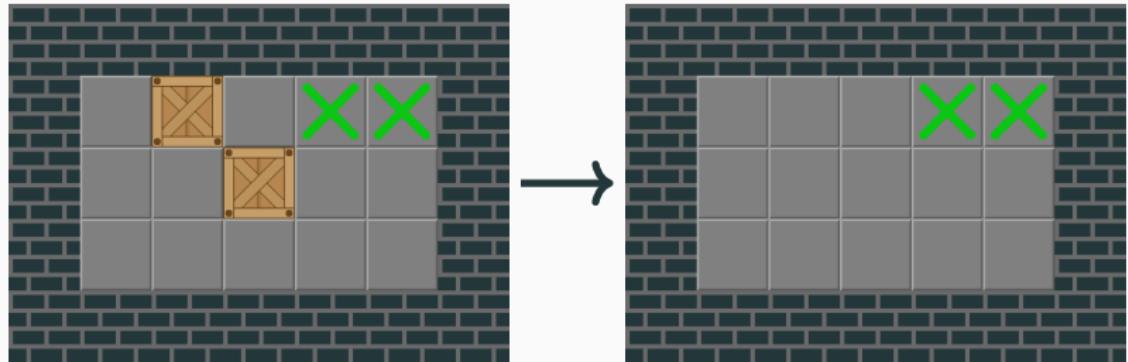
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Analyse statique

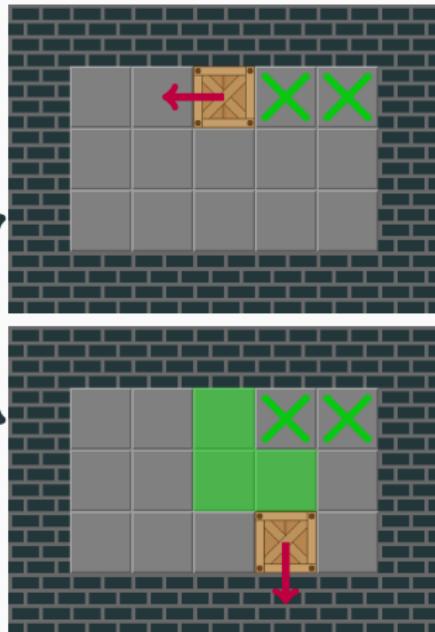
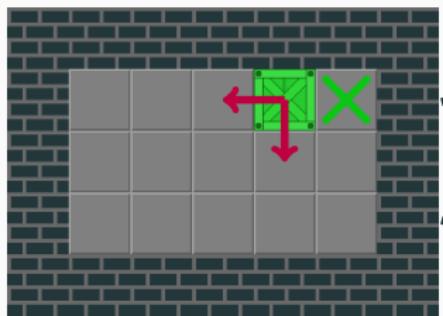
## Détection des positions mortes (*dead positions*)



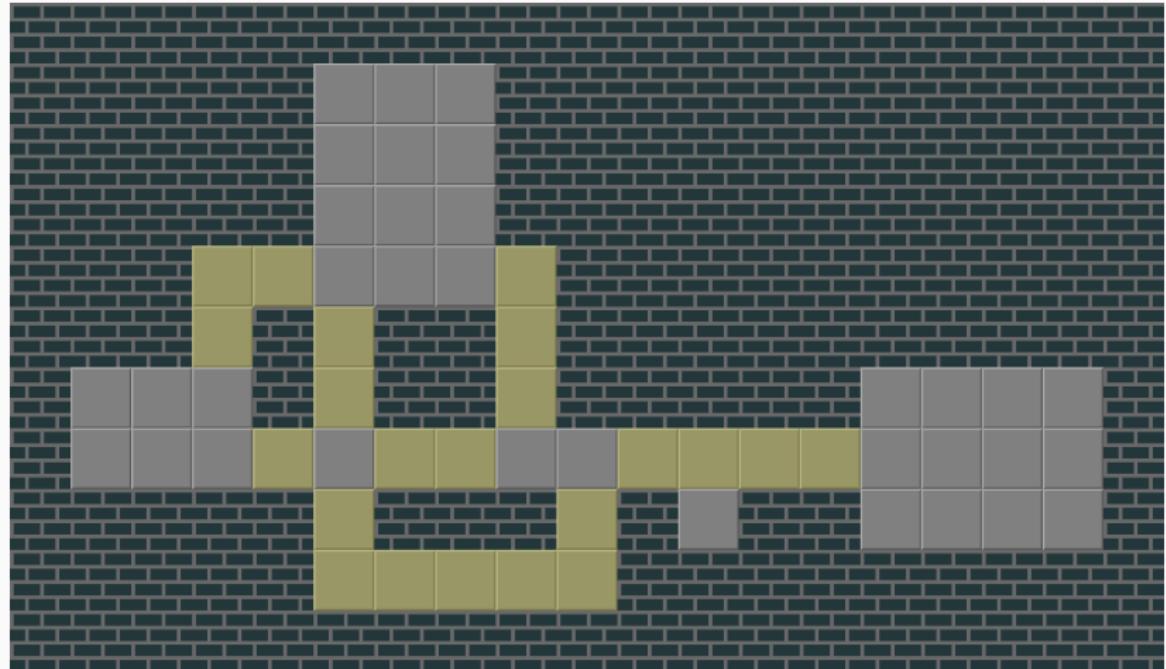
## Détection des positions mortes (*dead positions*)



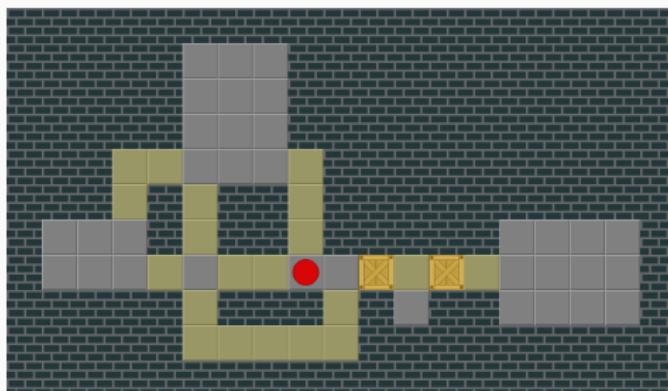
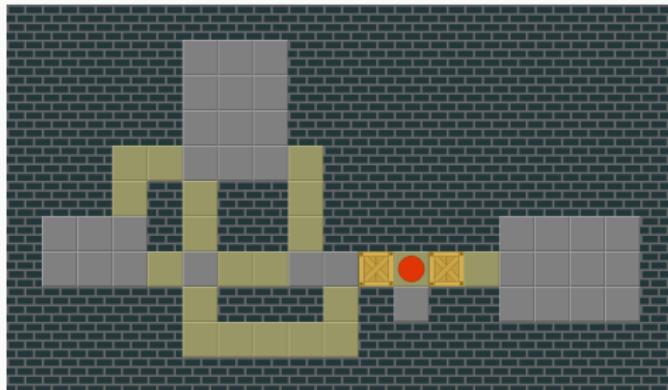
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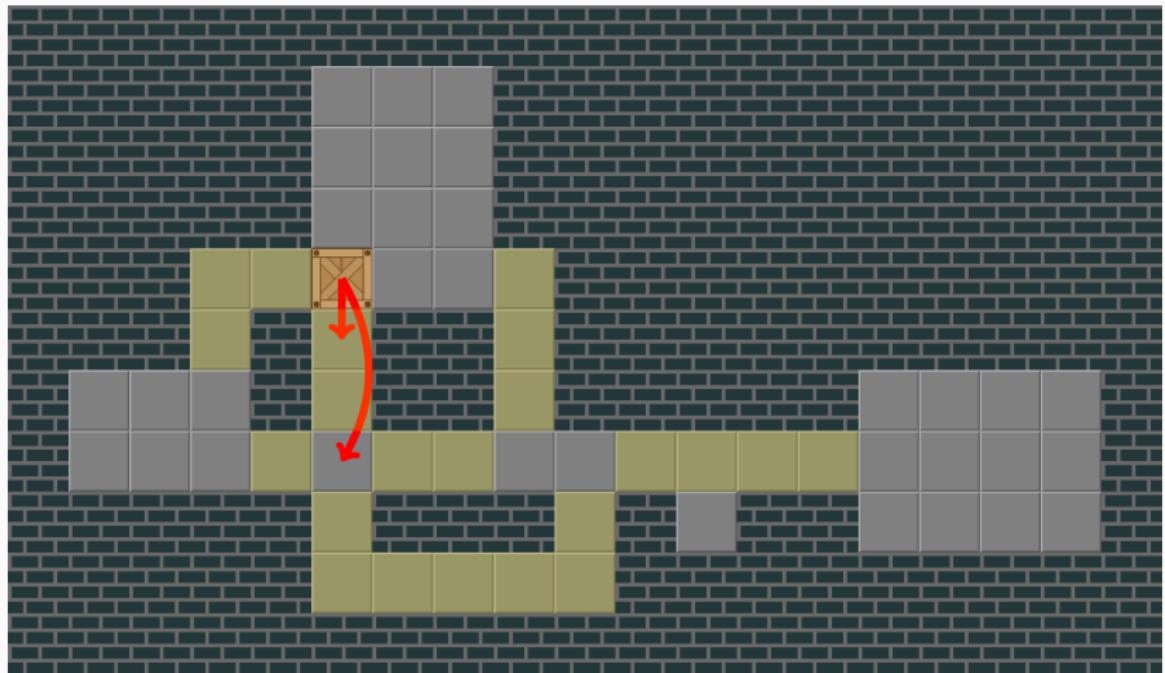
# Détection de tunnels



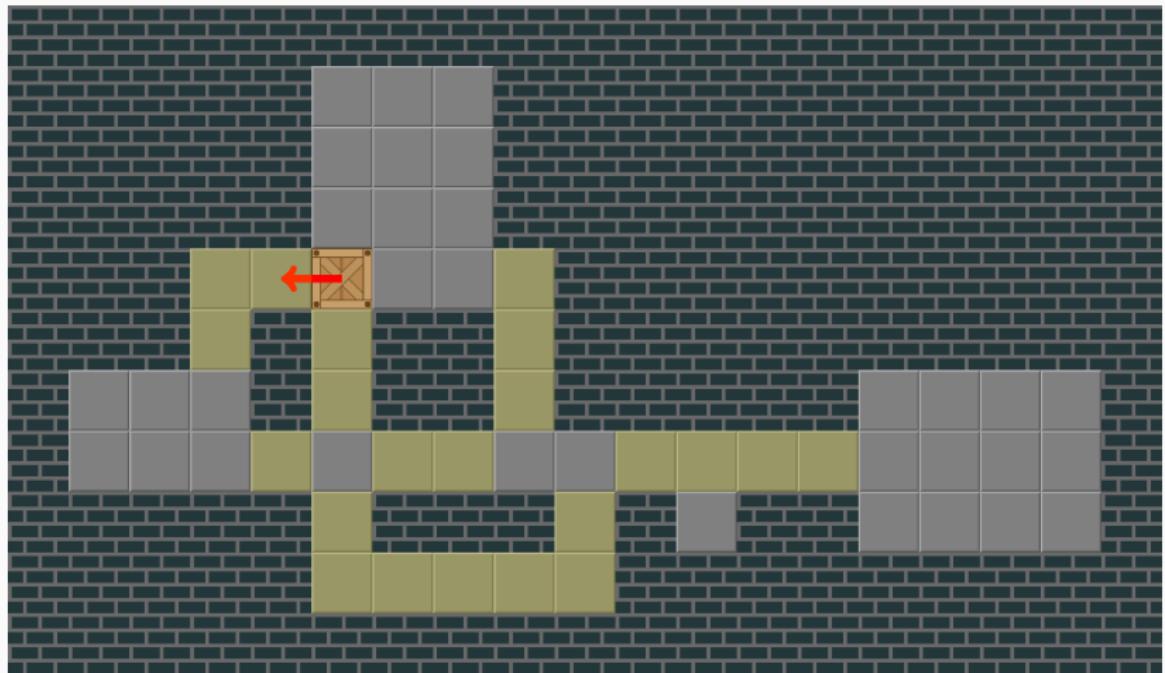
## Détection de tunnels



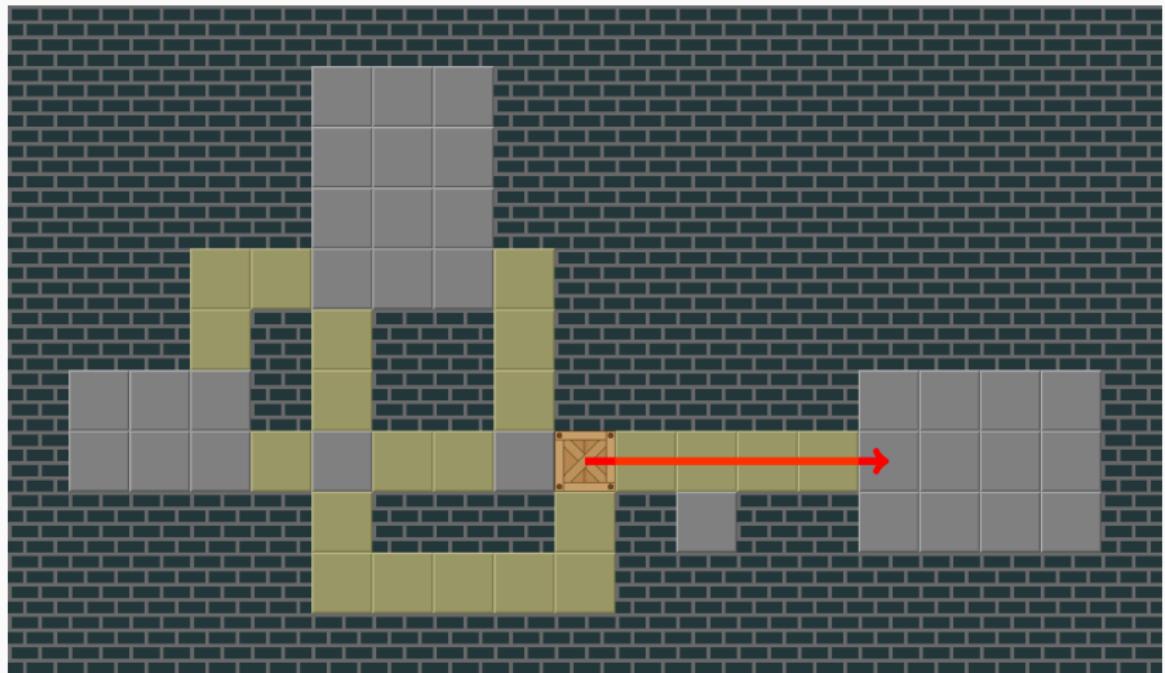
# Détection de tunnels



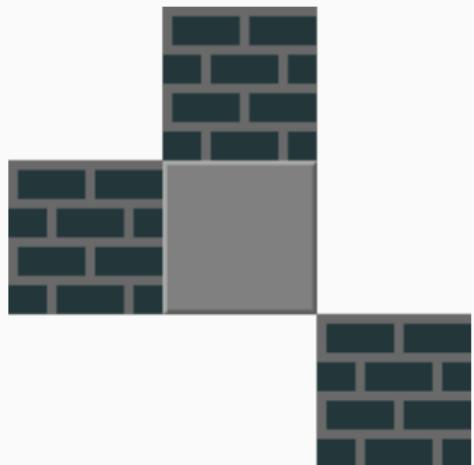
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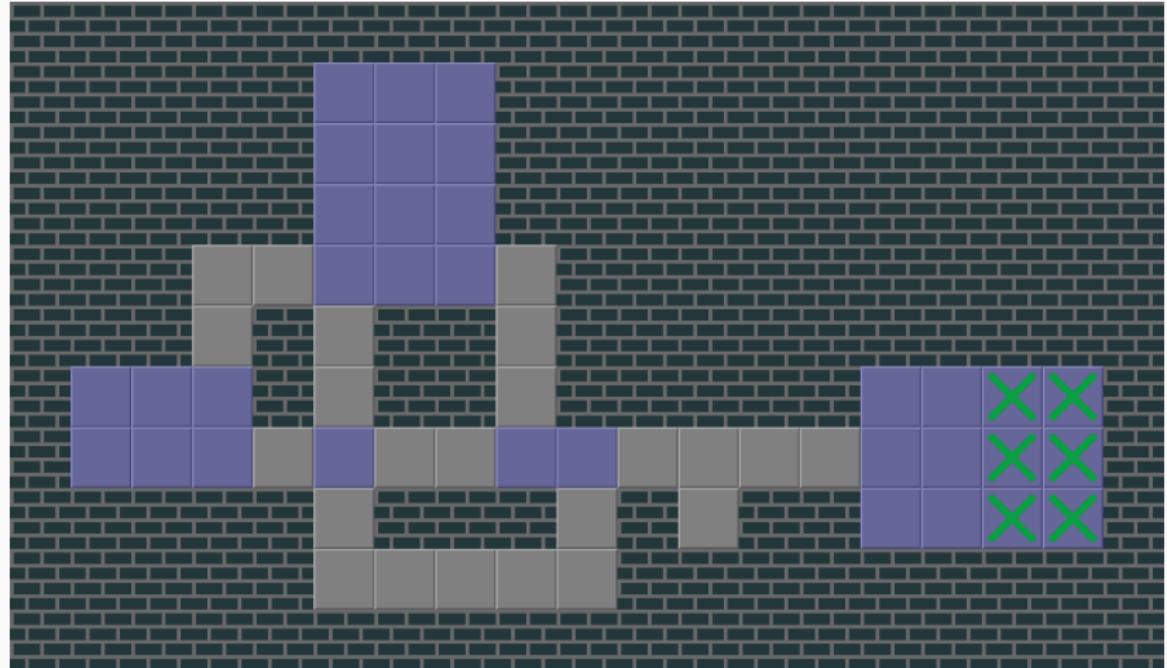


# Détection de tunnels

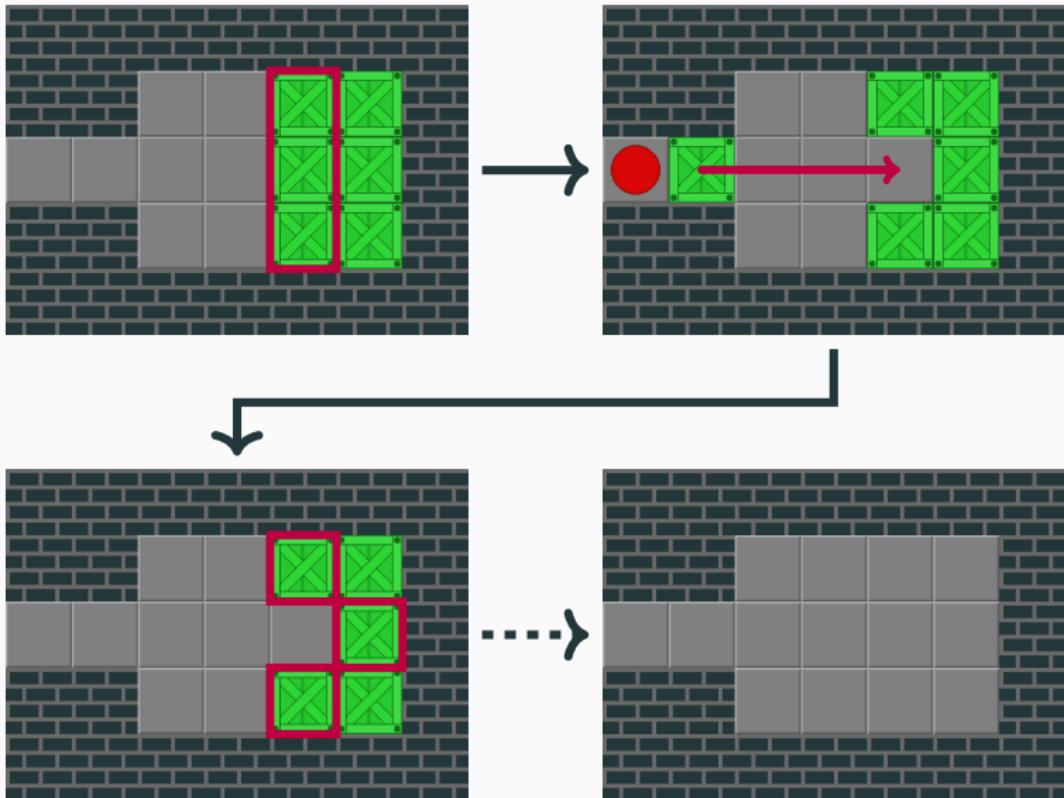


Composition d'un tunnel

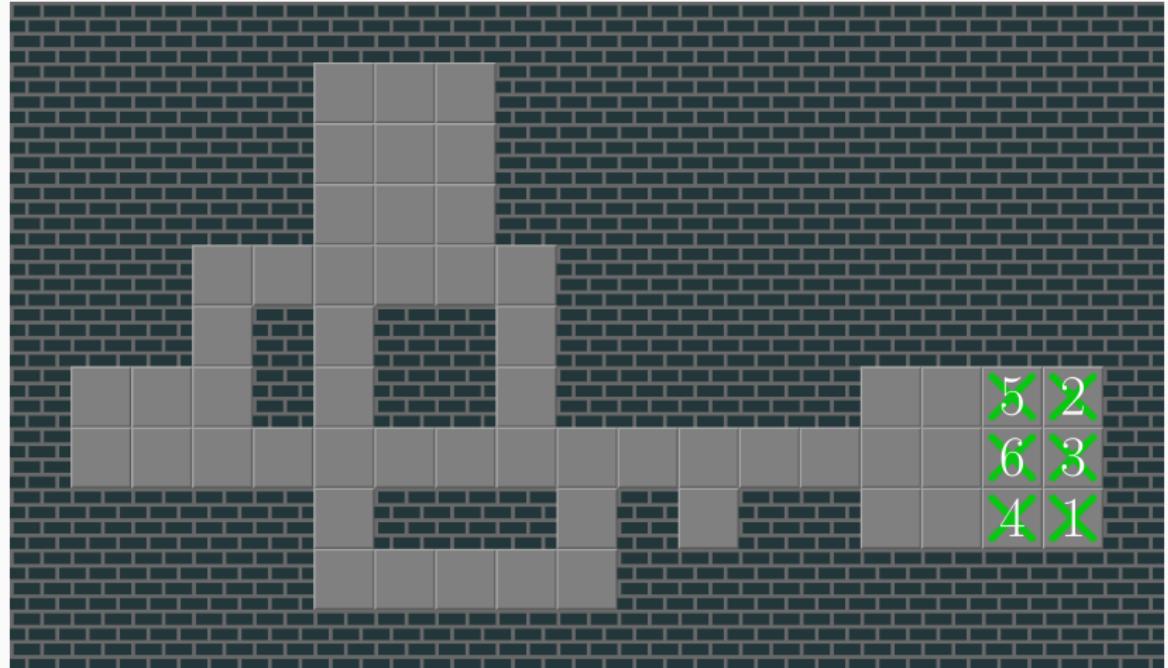
## Salles et ordre de rangement (*packing order*)



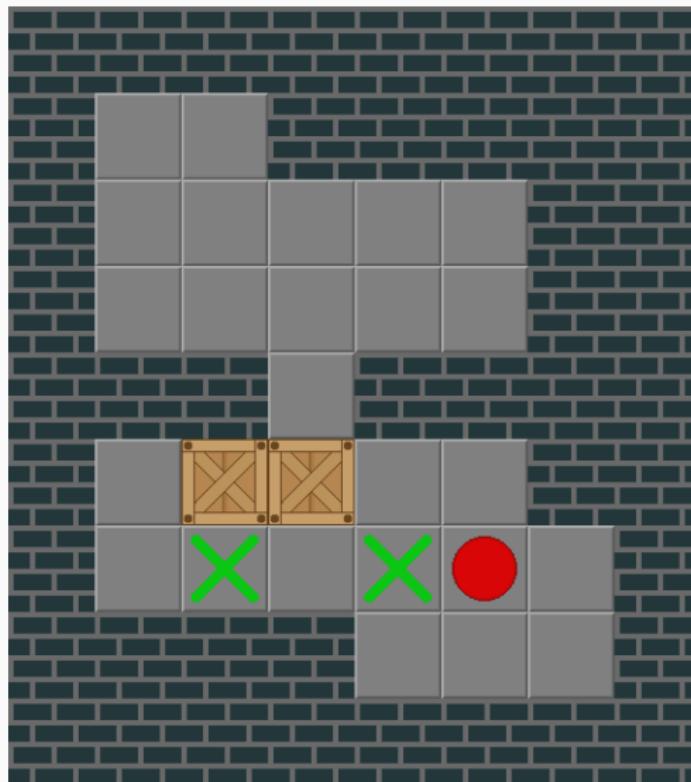
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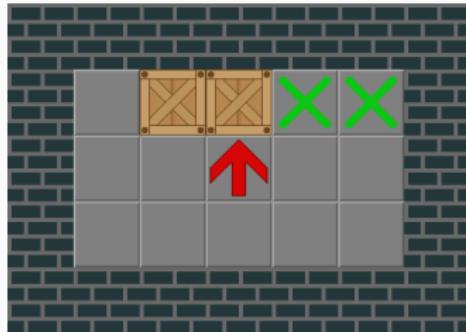


## Réduction de l'espace de recherche

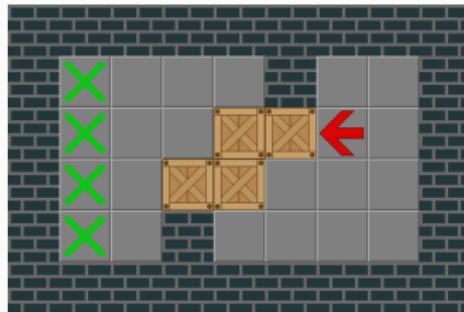
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Analyse dynamique

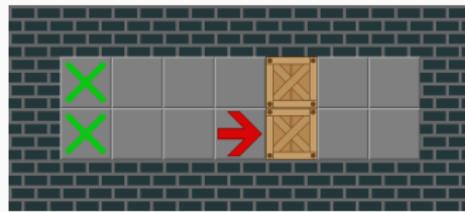
# Détection d'impasses (*deadlocks*)



(a) *Freeze deadlock n°1*



(b) *Freeze deadlock n°2*

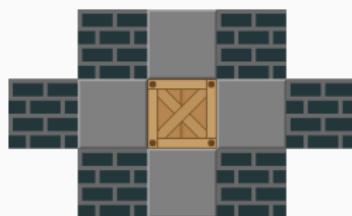


(c) *PI Corral deadlock*

# Détection de *freeze deadlock*



(a) Règle n°1

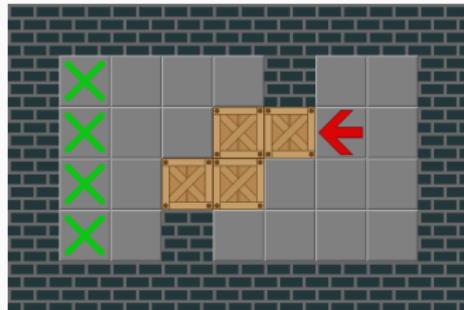


(b) Règle n°2

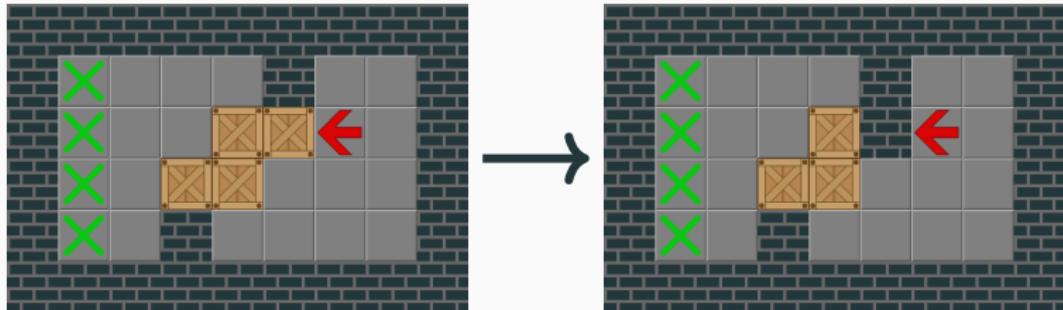


(c) Règle n°3

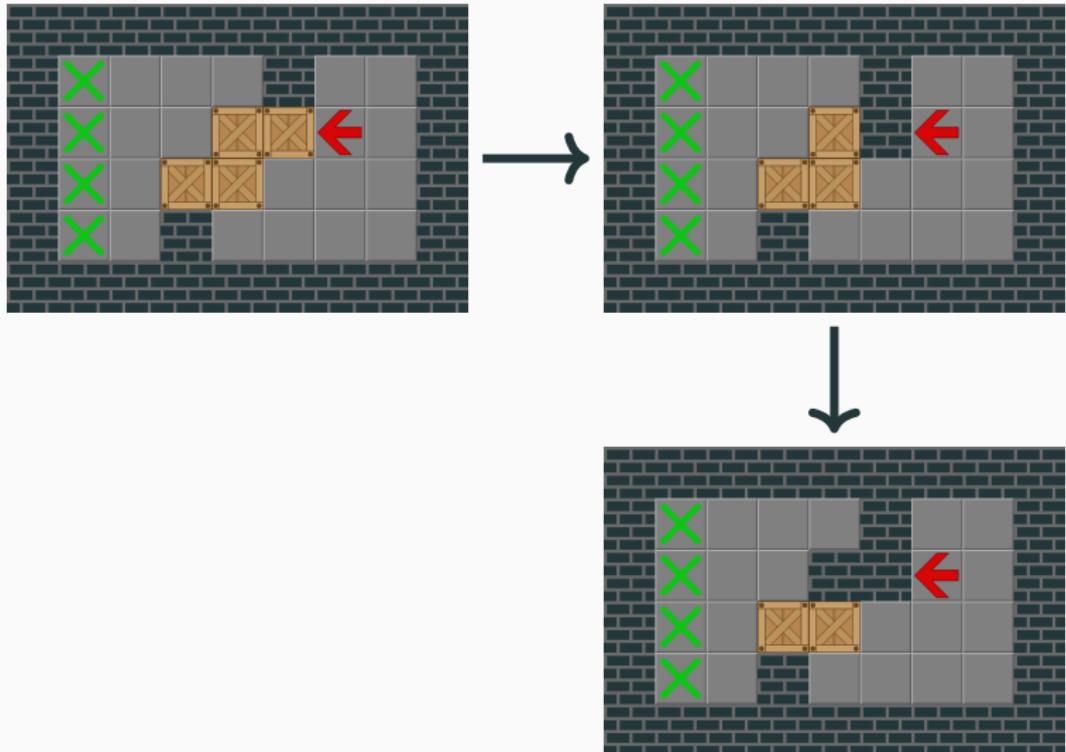
## Détection de *freeze deadlocks*



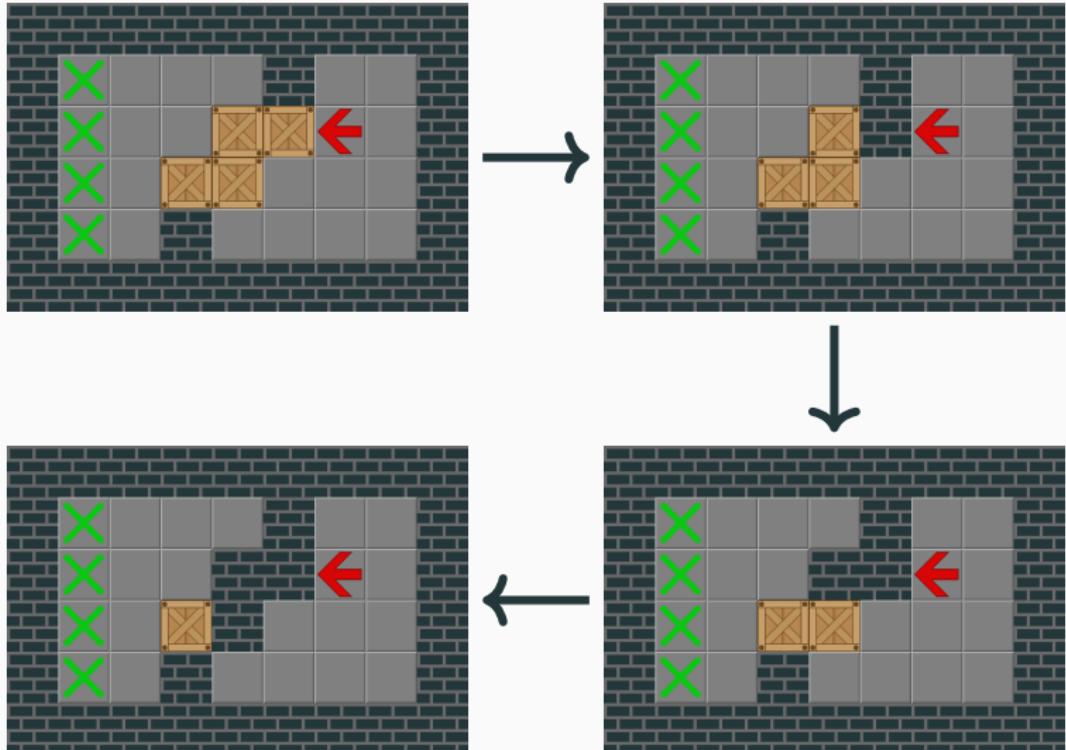
## Détection de *freeze deadlocks*



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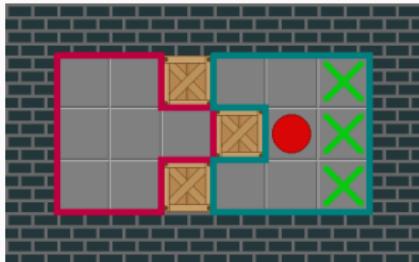


# Détection de *freeze deadlocks*

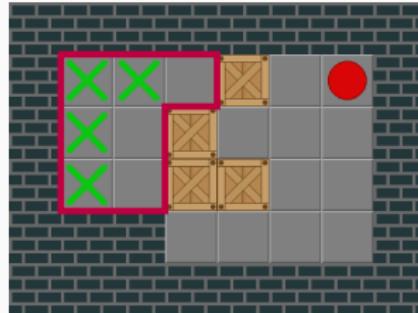


Gelée!

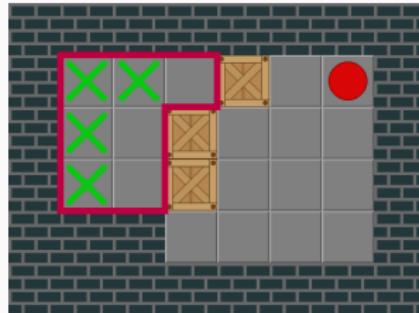
# Détection de *PI Corral deadlocks*



(a) *Corral*

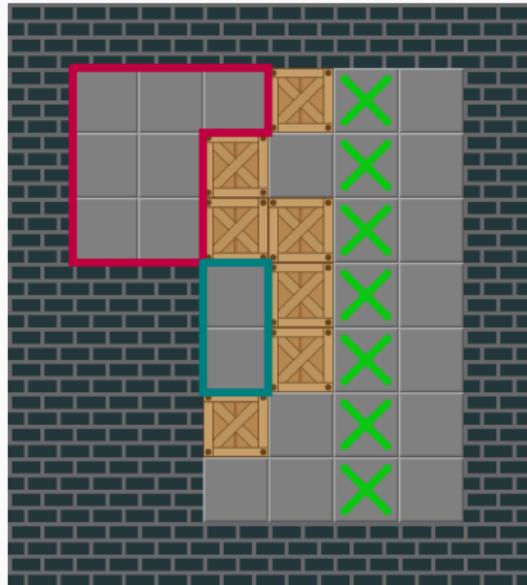


(b) *I Corral*

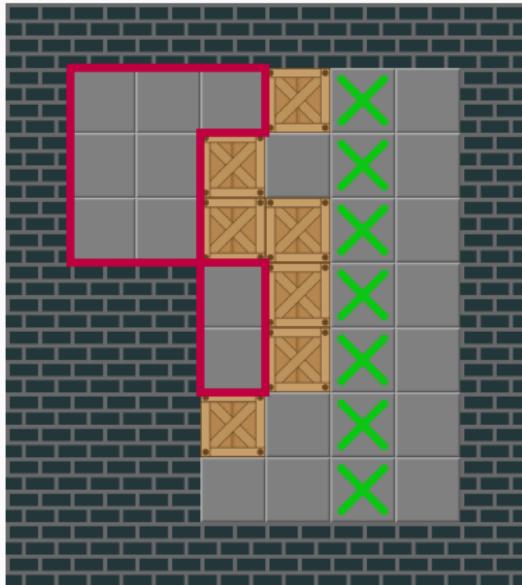


(c) *PI Corral*

## Détection de *PI Corral deadlocks*



Deux *I-Corrals*

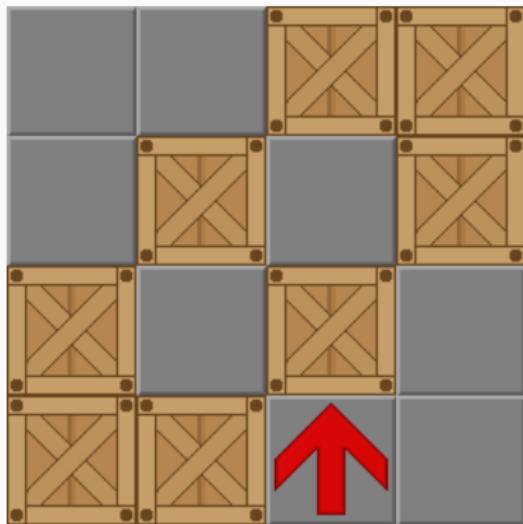
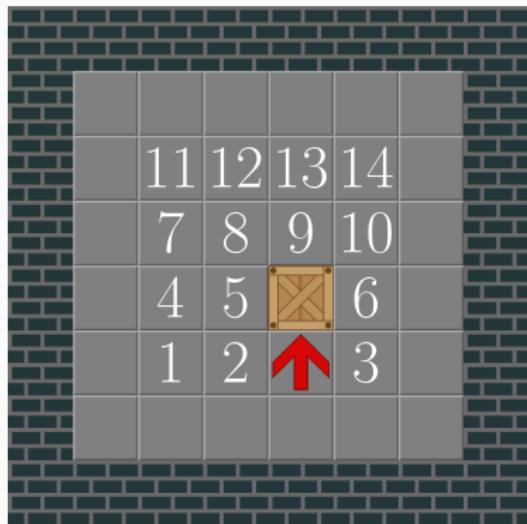


Un multi *PI-Corral*

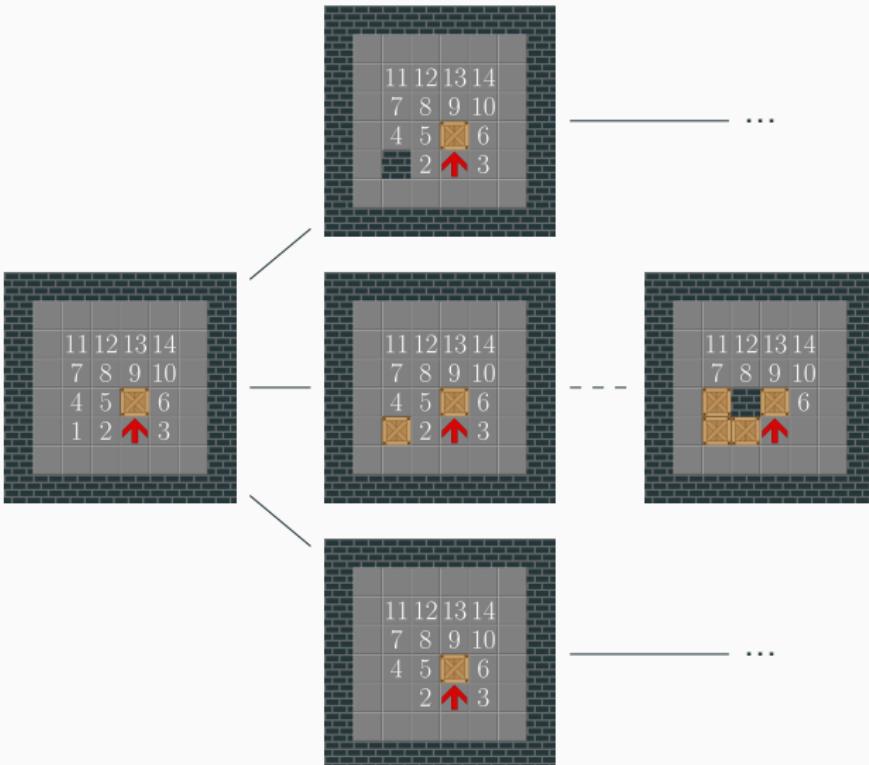
## Détection de *PI Corral deadlocks*

Brian Damgaard : émonde l'arbre de recherche d'au moins **20%** !

## Table de deadlocks



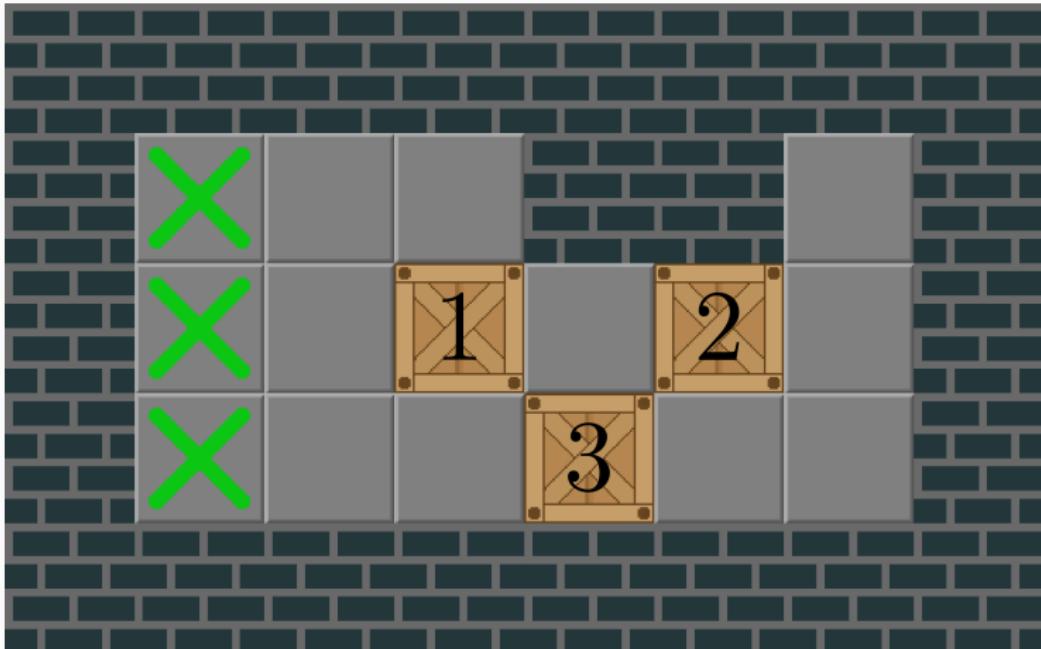
# Table de deadlocks



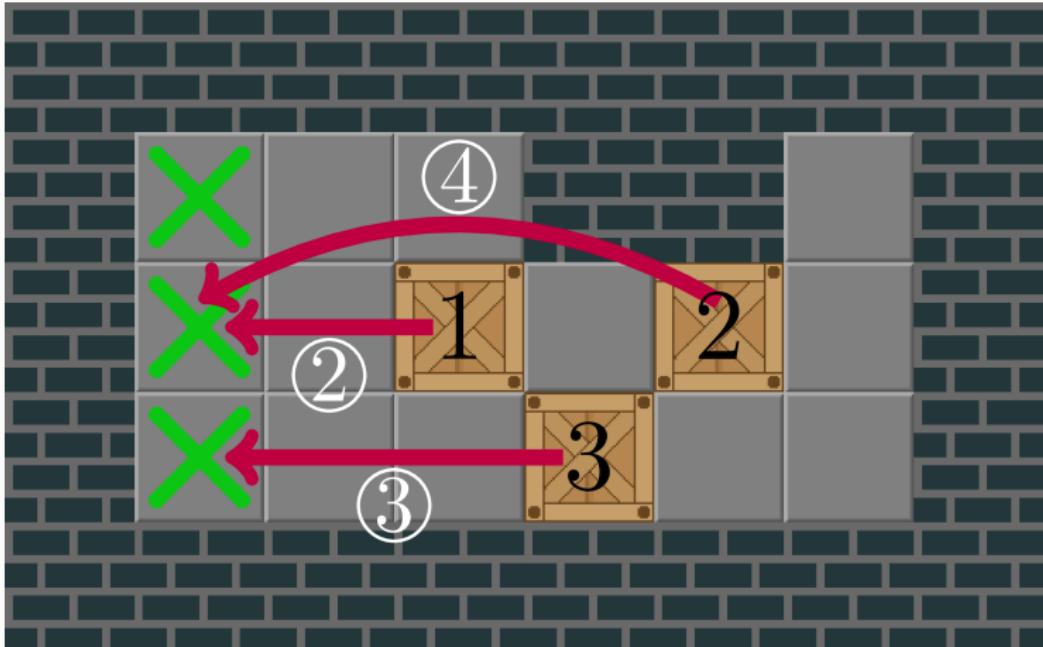
## **Recherche dirigée par une heuristique**

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## Heuristique simple (*Simple Lower Bound*)

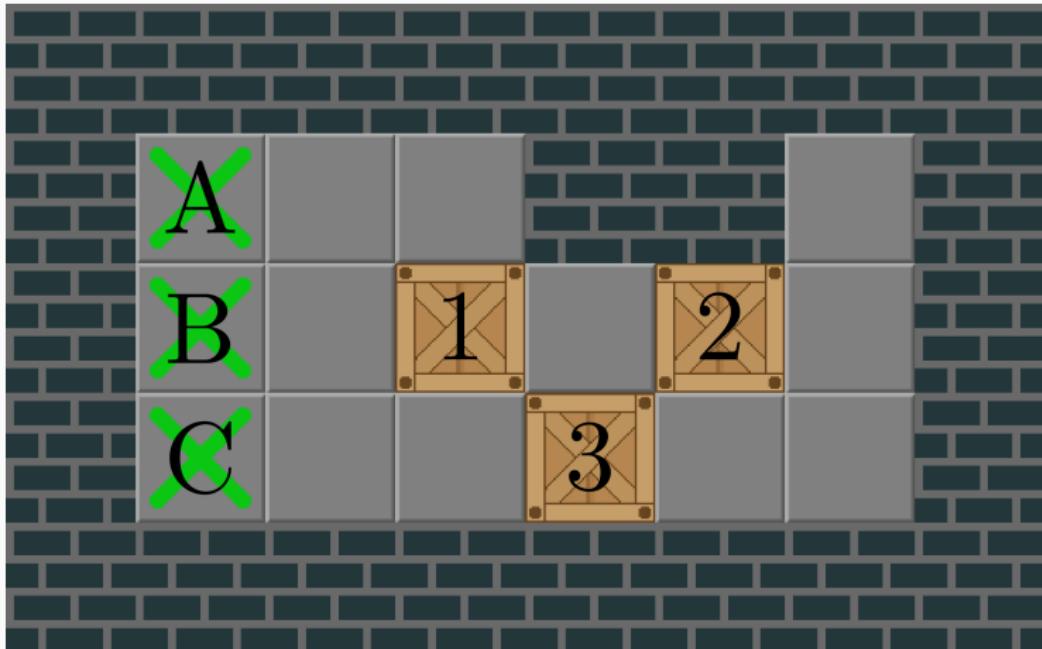


## Heuristique simple (*Simple Lower Bound*)

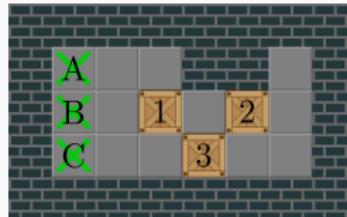


$$2 + 4 + 3 = 9$$

## Heuristique gloutonne (*Greedy Lower Bound*)



# Heuristique gloutonne (*Greedy Lower Bound*)

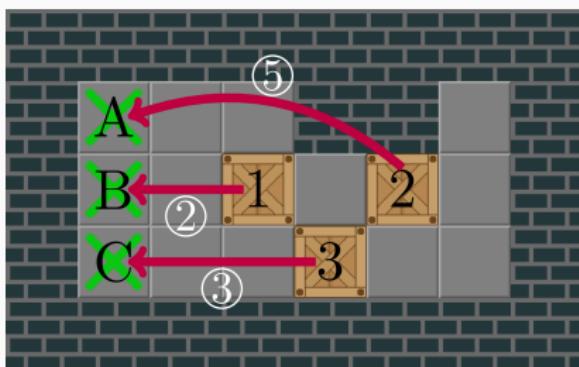
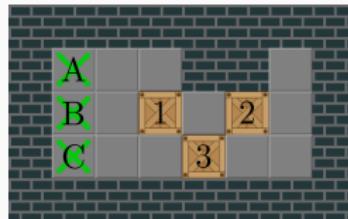


| Caisse → Cible | Distance |
|----------------|----------|
| 1 → A          | 3        |
| 1 → B          | 2        |
| 1 → C          | 3        |
| 2 → A          | 4        |
| 2 → B          | 4        |
| 2 → C          | 5        |
| 3 → A          | 5        |
| 3 → B          | 4        |
| 3 → C          | 3        |

Tri →

| Caisse → Cible | Distance |
|----------------|----------|
| <b>1 → B</b>   | <b>2</b> |
| 1 → A          | 3        |
| 1 → C          | 3        |
| <b>3 → C</b>   | <b>3</b> |
| 2 → B          | 4        |
| 3 → B          | 4        |
| 2 → A          | 5        |
| 2 → C          | 5        |
| <b>3 → A</b>   | <b>5</b> |

# Heuristique gloutonne (*Greedy Lower Bound*)



$$2 + 3 + 5 = \mathbf{10}$$

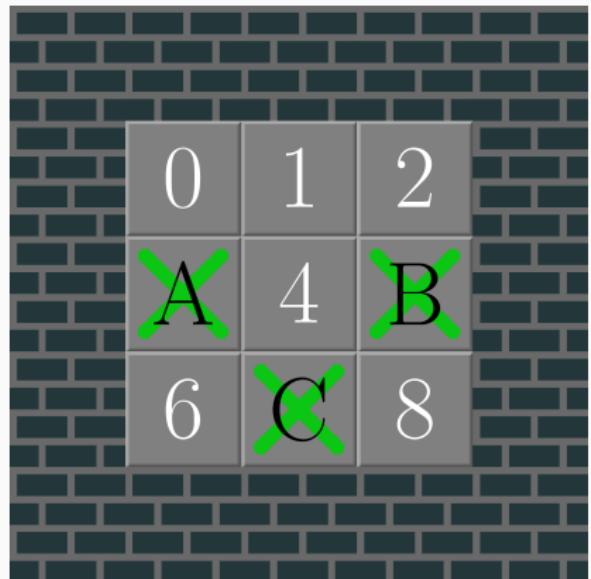
| Caisse → Cible | Distance |
|----------------|----------|
| <b>1 → B</b>   | 2        |
| 1 → A          | 3        |
| 1 → C          | 3        |
| <b>3 → C</b>   | <b>3</b> |
| 2 → B          | 4        |
| 3 → B          | 4        |
| 2 → A          | 5        |
| 2 → C          | 5        |
| <b>3 → A</b>   | <b>5</b> |

## Optimisations

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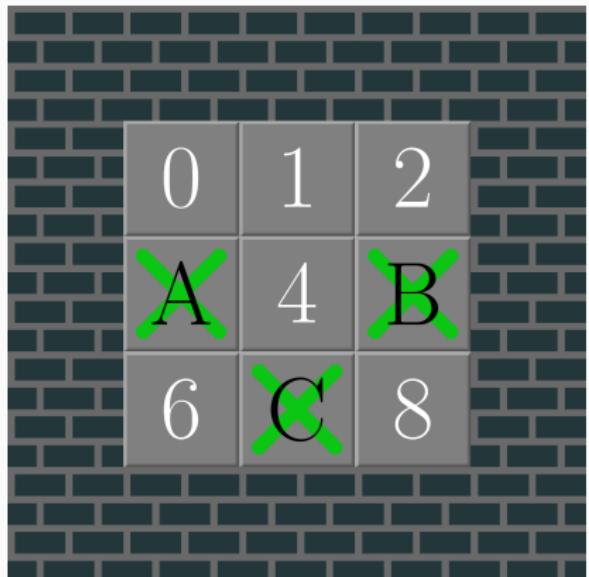
# Précalcul des distances caisses-cibles

| Case | Distances |   |   |
|------|-----------|---|---|
|      | A         | B | C |
| 0    | 1         | 3 | 3 |
| 1    | 2         | 2 | 2 |
| 2    | 3         | 1 | 3 |
| 3    | 0         | 2 | 2 |
| 4    | 1         | 1 | 1 |
| 5    | 2         | 0 | 2 |
| 6    | 1         | 3 | 1 |
| 7    | 2         | 2 | 0 |
| 8    | 3         | 1 | 1 |

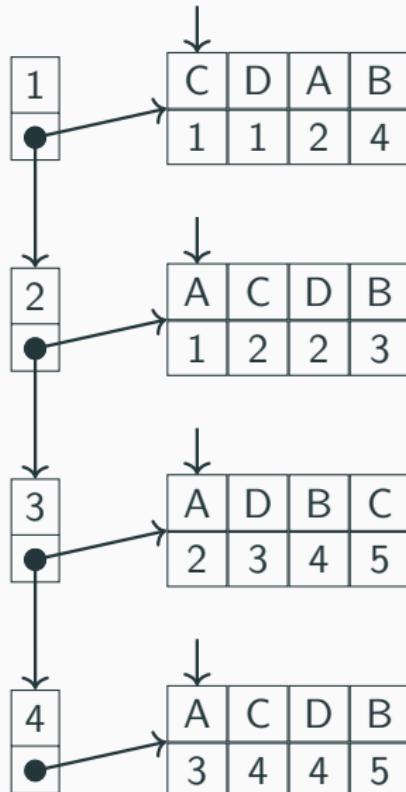


# Précalcul des distances caisses-cibles

| Case | Distances triées |       |       |
|------|------------------|-------|-------|
| 0    | A : 1            | B : 3 | C : 3 |
| 1    | A : 2            | B : 2 | C : 2 |
| 2    | B : 1            | A : 3 | C : 3 |
| 3    | A : 0            | B : 2 | C : 2 |
| 4    | A : 1            | B : 1 | C : 1 |
| 5    | B : 0            | A : 2 | C : 2 |
| 6    | A : 1            | C : 1 | B : 3 |
| 7    | C : 0            | A : 2 | B : 2 |
| 8    | B : 1            | C : 1 | A : 3 |

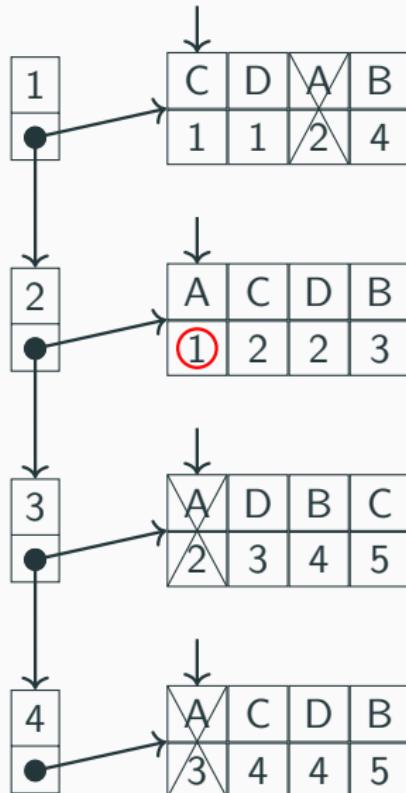


## Greedy Lower Bound en $\mathcal{O}(n^2)$



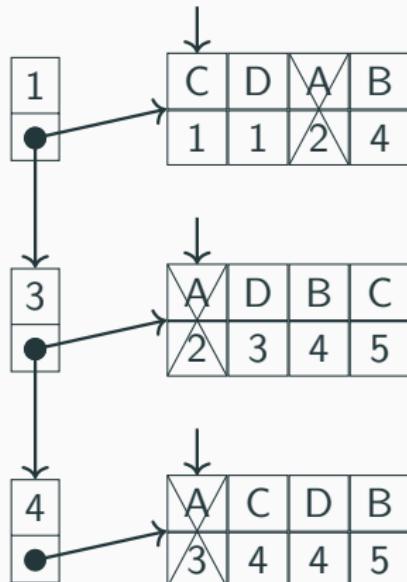
$h =$

## Greedy Lower Bound en $\mathcal{O}(n^2)$



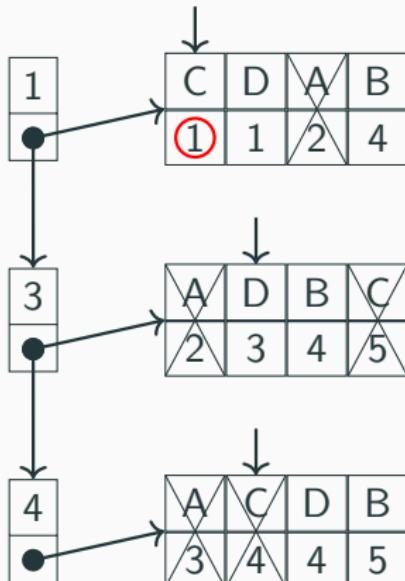
$$h = 1 +$$

## Greedy Lower Bound en $\mathcal{O}(n^2)$



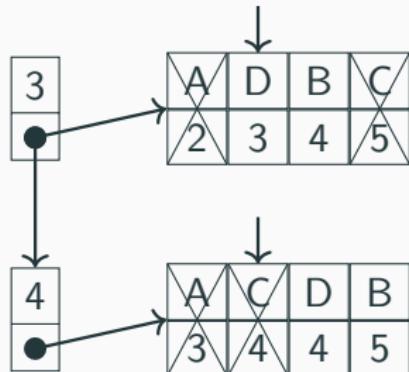
$$h = 1 +$$

## Greedy Lower Bound en $\mathcal{O}(n^2)$



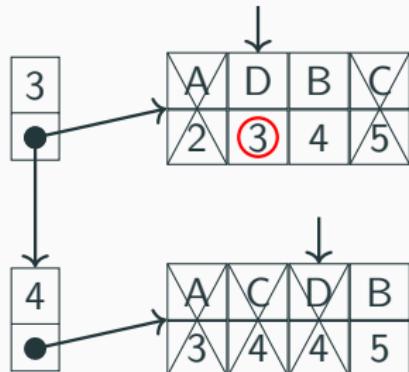
$$h = 1 + 1 +$$

## *Greedy Lower Bound* en $\mathcal{O}(n^2)$



$$h = 1 + 1 +$$

## Greedy Lower Bound en $\mathcal{O}(n^2)$



$$h = 1 + 1 + 3 +$$

## *Greedy Lower Bound* en $\mathcal{O}(n^2)$



$$h = 1 + 1 + 3 + 5 = 10$$

# Parcours de graphes : démarquer tous les nœuds en $\mathcal{O}(1)$

nœud marqué *ssi* valeur =  $m$

$m = 0$

|    |    |    |    |    |
|----|----|----|----|----|
| -1 | -1 | -1 | -1 | -1 |
| -1 | X  | X  | -1 | -1 |
| -1 | -1 | -1 | -1 | -1 |
| -1 | -1 | -1 | -1 | -1 |
| -1 | -1 | -1 | -1 | -1 |

$m = 0$

|    |    |    |    |    |
|----|----|----|----|----|
| -1 | -1 | -1 | -1 | -1 |
| -1 | X  | X  | -1 | -1 |
| -1 | -1 | -1 | -1 | -1 |
| -1 | 0  | -1 | -1 | -1 |
| -1 | -1 | -1 | -1 | -1 |

$m = 0$

|    |    |    |    |    |
|----|----|----|----|----|
| -1 | -1 | -1 | -1 | -1 |
| -1 | X  | X  | -1 | -1 |
| -1 | 0  | 0  | -1 | -1 |
| -1 | 0  | 0  | -1 | -1 |
| -1 | -1 | -1 | -1 | -1 |

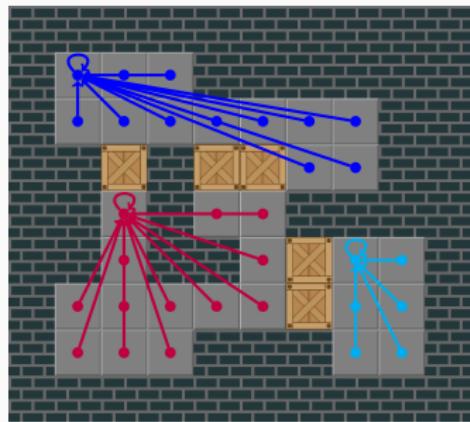
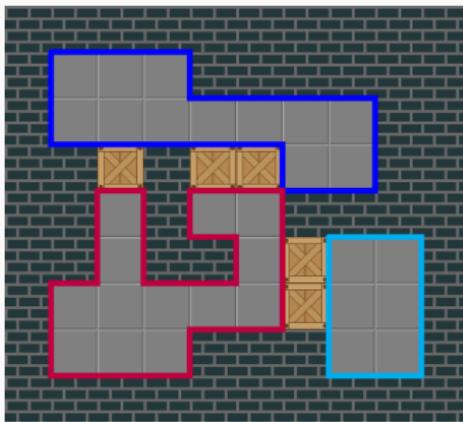
$m = 1$

|    |    |    |    |    |
|----|----|----|----|----|
| -1 | -1 | -1 | -1 | -1 |
| -1 | X  | X  | -1 | -1 |
| -1 | 0  | 0  | -1 | -1 |
| -1 | 0  | 0  | -1 | -1 |
| -1 | -1 | -1 | -1 | -1 |

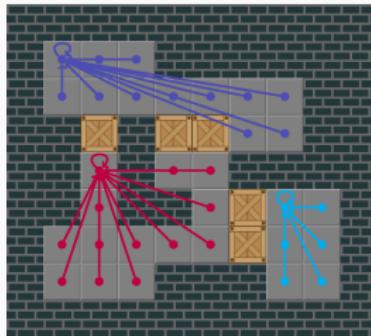


# Calcul des *corrals* en $\mathcal{O}(wh)$

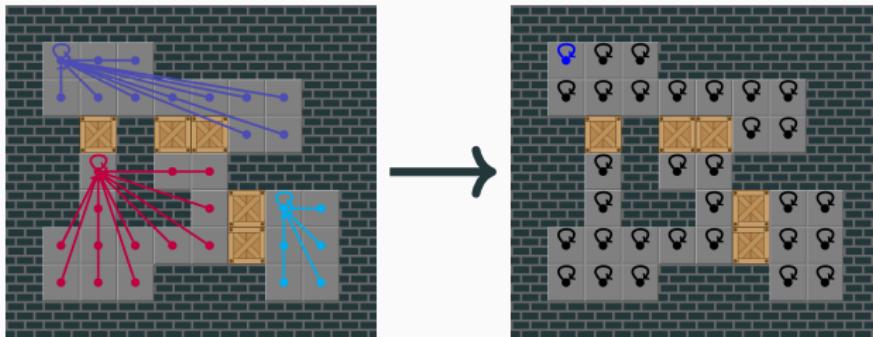
Utilisation de *Union-Find* : partition de  $\llbracket 0; wh - 1 \rrbracket$ .



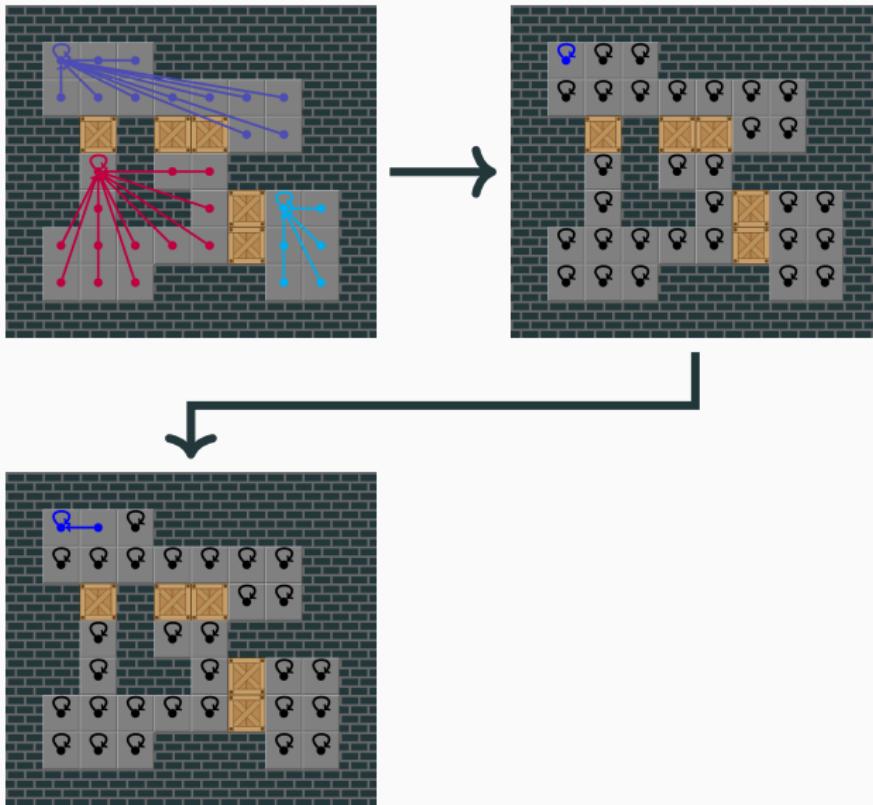
# Calcul des *corrals* en $\mathcal{O}(wh)$



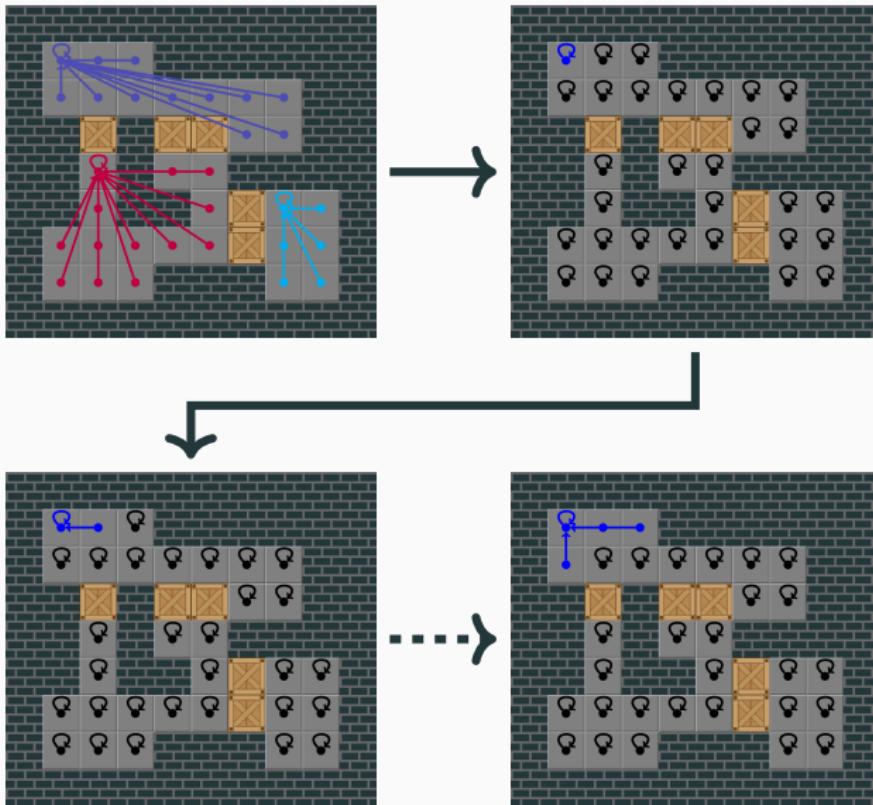
## Calcul des *corrals* en $\mathcal{O}(wh)$



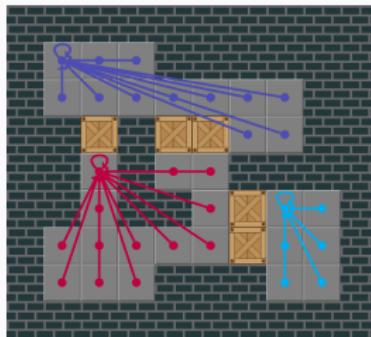
# Calcul des *corrals* en $\mathcal{O}(wh)$



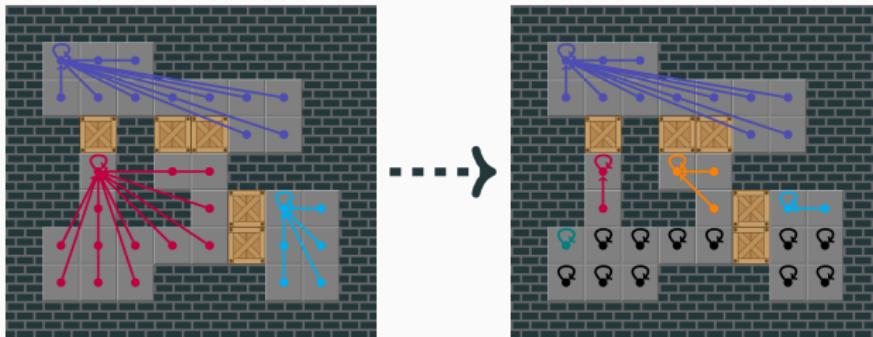
# Calcul des *corrals* en $\mathcal{O}(wh)$



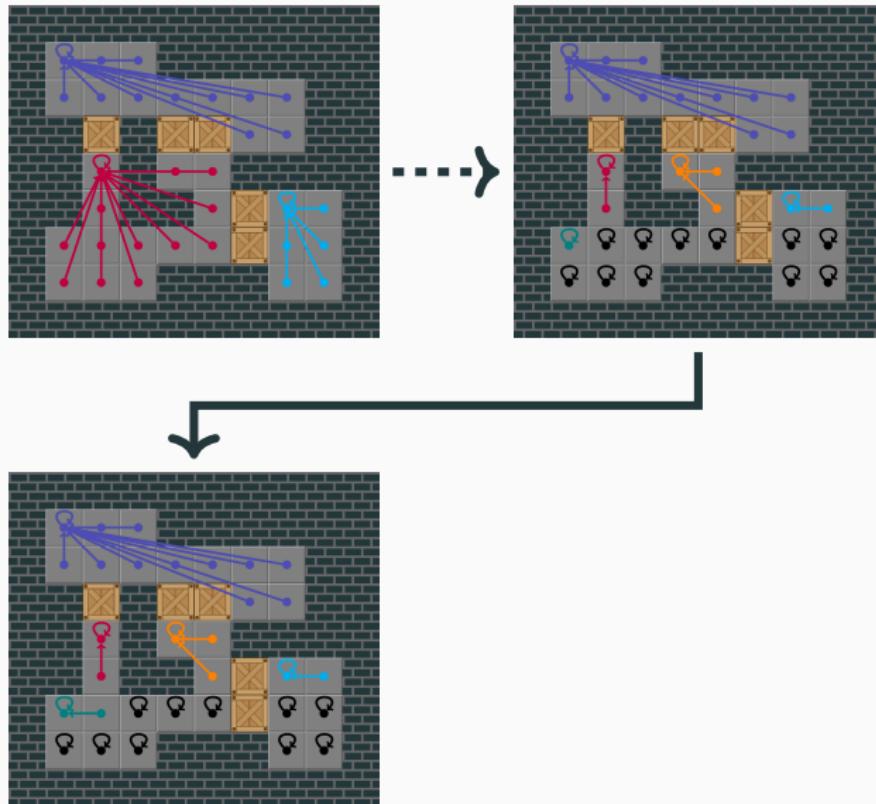
# Calcul des *corrals* en $\mathcal{O}(wh)$



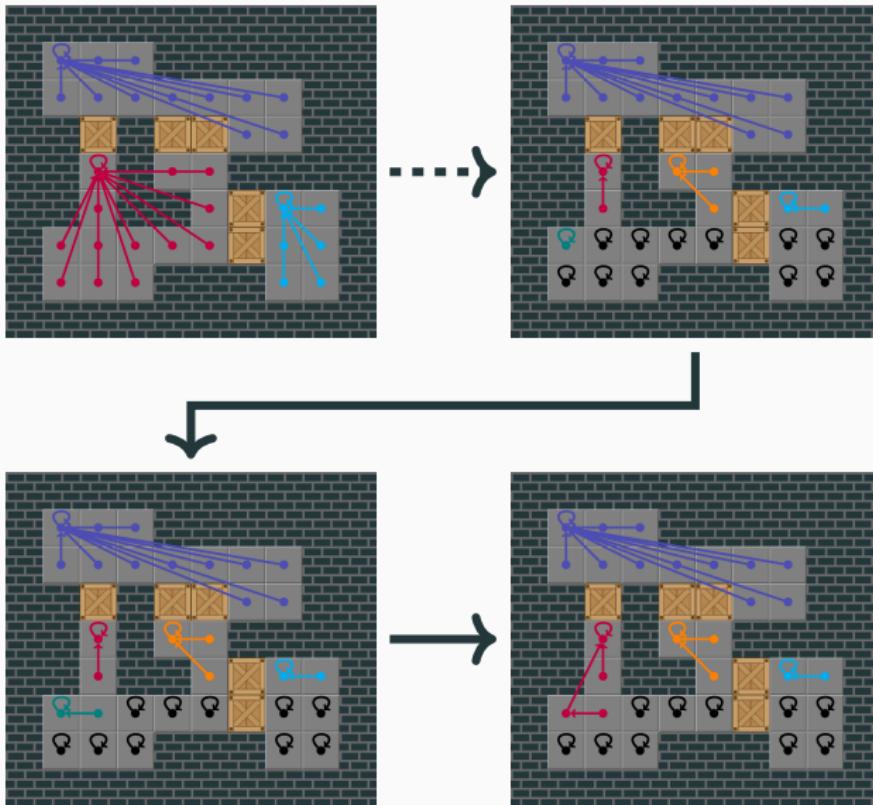
# Calcul des *corrals* en $\mathcal{O}(wh)$



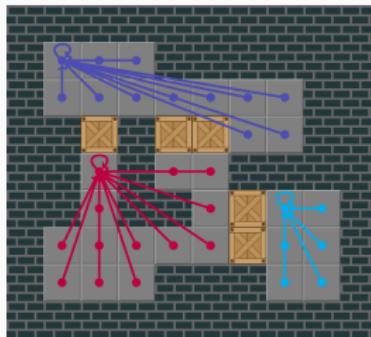
# Calcul des *corrals* en $\mathcal{O}(wh)$



# Calcul des *corrals* en $\mathcal{O}(wh)$



# Calcul des *corrals* en $\mathcal{O}(wh)$



## Résultats

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# Nombre de niveaux résolus

Limite de temps : 10 min. Limite de RAM : 32 Gio.

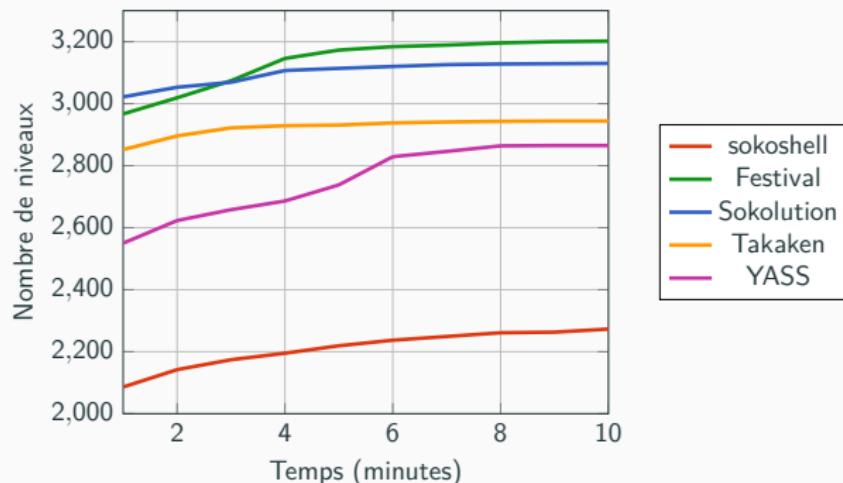
| Ensemble de niveaux            | XSokoban  | <i>Large test suite</i> |
|--------------------------------|-----------|-------------------------|
| Nombre de niveaux              | 90        | 3272                    |
| <b>A*</b>                      | <b>11</b> | <b>2204</b>             |
| <b>fess0</b>                   | <b>15</b> | <b>2273</b>             |
| Festival (Yaron Shoham)        | 90        | 3202                    |
| Sokolution (Florent Diedler)   | 90        | 3130                    |
| Takaken (Ken'ichiro Takahashi) | 90        | 2944                    |
| YASS (Brian Damgaard)          | 89        | 2865                    |

# Statistiques

## Temps moyen passé par niveaux

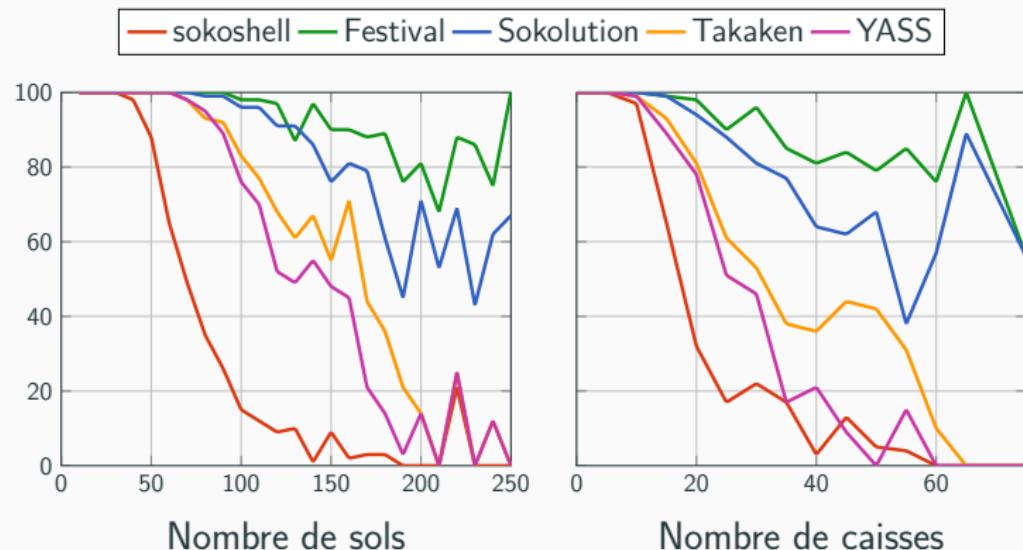
| Solveur     | A*       | fess0    | Festival | Sokolution | Takaken | YASS |
|-------------|----------|----------|----------|------------|---------|------|
| Temps moyen | 3min 28s | 3min 16s | 3s       | 2s         | 7s      | 24s  |

## Nombre de niveaux résolus (cumulés) en fonction du temps



# Statistiques

Pourcentage de niveaux résolus selon la composition des niveaux



## **Annexe**

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# Tableau des complexités