07 Univariate Linear Regression ANOVA and intervals

A research team conducted a longitudinal study of participants between 25 and 30 years of age. They measured each participant's level of education at age 25. They also measured each participant's earnings at age 30. The team collected data on $n =$ 314 participants. The average level of education at age 25 was 15.3, with an observed standard deviation of 3.1 (the divisor in the underlying variance calculation was $n - 1$). The average earnings (in thousands of dollars) was 54.9, with an observed standard deviation of 14.9 (the divisor in the underlying variance calculation was $n-1$). The Pearson product moment correlation coefficient between the two variables was 0.76. The research team seeks to estimate the regression of participant earnings at age 30 on participant education at age 25.

a. Complete the analysis of variance table for the regression of participant earnings at age 30 on participant education at age 25. Test the null hypothesis that the slope of this regression is zero at levels of significance 0.10, 0.05, and 0.01. This part is worth 25 points.

	MEAN	SD
IV = EDUCATION	15.3	3.1
DV = EARNINGS	54.9	14.9.

$n = 314.$

$SS\ TOTAL = (n-1)(SD_{DV})^2$

$= 313\,(14.9)^2 = 69\,489.13$ ON 313 DF.

$\sum (x_i - \bar{x}_m)^2 = (n-1)(SD_{IV})^2$

$= 313\,(3.1)^2 = 3007.93$

$SSREG = (r(DV, IV))^2\ SS\ TOTAL$

$= (.76)^2\ SS\ TOTAL = 40,136.92$ ON 1 DF.

$SSERR = (1 - r^2)\ SS\ TOTAL$

$= (1 - .76^2)\ SS\ TOTAL$

$= 29,352.21$ ON 312 DF.

ANOVA TABLE
LIN REG OF EARNINGS ON EDUCATION

SOURCE	DF	SS	MS
REGRESSION	1	40,136.92	40136.92
ERROR	312	29,352.21	94.08
TOTAL	313	69489.13	

MODEL $Y_i = \beta_0 + \beta_1 x_i + \sigma \varepsilon_i$

$H_0: \beta_1 = 0$

$H_1: \beta_1 \neq 0$

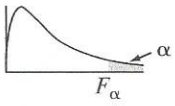
TEST STATISTIC: $F = \frac{MSREG}{MSERR}$

$F = \frac{40136.92}{94.08} = 426.63$ on (1, 312) DF.

α	$F(1,312)$	$F(1,\infty)$	DECISION
.10	2.722	2.706	REJECT
.05	3.871	3.842	REJECT
.01	6.717	6.637	REJECT

TABLE 8

Percentage points of the F distribution (df_2 at least 40)



		df_1									
df_2	α	1	2	3	4	5	6	7	8	9	10
40	.25	1.36	1.44	1.42	1.40	1.39	1.37	1.36	1.35	1.34	1.33
	.10	2.84	2.44	2.23	2.09	2.00	1.93	1.87	1.83	1.79	1.76
	.05	4.08	3.23	2.84	2.61	2.45	2.34	2.25	2.18	2.12	2.08
	.025	5.42	4.05	3.46	3.13	2.90	2.74	2.62	2.53	2.45	2.39
	.01	7.31	5.18	4.31	3.83	3.51	3.29	3.12	2.99	2.89	2.80
	.005	8.83	6.07	4.98	4.37	3.99	3.71	3.51	3.35	3.22	3.12
	.001	12.61	8.25	6.59	5.70	5.13	4.73	4.44	4.21	4.02	3.87
60	.25	1.35	1.42	1.41	1.38	1.37	1.35	1.33	1.32	1.31	1.30
	.10	2.79	2.39	2.18	2.04	1.95	1.87	1.82	1.77	1.74	1.71
	.05	4.00	3.15	2.76	2.53	2.37	2.25	2.17	2.10	2.04	1.99
	.025	5.29	3.93	3.34	3.01	2.79	2.63	2.51	2.41	2.33	2.27
	.01	7.08	4.98	4.13	3.65	3.34	3.12	2.95	2.82	2.72	2.63
	.005	8.49	5.79	4.73	4.14	3.76	3.49	3.29	3.13	3.01	2.90
	.001	11.97	7.77	6.17	5.31	4.76	4.37	4.09	3.86	3.69	3.54
90	.25	1.34	1.41	1.39	1.37	1.35	1.33	1.32	1.31	1.30	1.29
	.10	2.76	2.36	2.15	2.01	1.91	1.84	1.78	1.74	1.70	1.67
	.05	3.95	3.10	2.71	2.47	2.32	2.20	2.11	2.04	1.99	1.94
	.025	5.20	3.84	3.26	2.93	2.71	2.55	2.43	2.34	2.26	2.19
	.01	6.93	4.85	4.01	3.53	3.23	3.01	2.84	2.72	2.61	2.52
	.005	8.28	5.62	4.57	3.99	3.62	3.35	3.15	3.00	2.87	2.77
	.001	11.57	7.47	5.91	5.06	4.53	4.15	3.87	3.65	3.48	3.34
120	.25	1.34	1.40	1.39	1.37	1.35	1.33	1.31	1.30	1.29	1.28
	.10	2.75	2.35	2.13	1.99	1.90	1.82	1.77	1.72	1.68	1.65
	.05	3.92	3.07	2.68	2.45	2.29	2.18	2.09	2.02	1.96	1.91
	.025	5.15	3.80	3.23	2.89	2.67	2.52	2.39	2.30	2.22	2.16
	.01	6.85	4.79	3.95	3.48	3.17	2.96	2.79	2.66	2.56	2.47
	.005	8.18	5.54	4.50	3.92	3.55	3.28	3.09	2.93	2.81	2.71
	.001	11.38	7.32	5.78	4.95	4.42	4.04	3.77	3.55	3.38	3.24
240	.25	1.33	1.39	1.38	1.36	1.34	1.32	1.30	1.29	1.27	1.27
	.10	2.73	2.32	2.10	1.97	1.87	1.80	1.74	1.70	1.65	1.63
	.05	3.88	3.03	2.64	2.41	2.25	2.14	2.04	1.98	1.92	1.87
	.025	5.09	3.75	3.17	2.84	2.62	2.46	2.34	2.25	2.17	2.10
	.01	6.74	4.69	3.86	3.40	3.09	2.88	2.71	2.59	2.48	2.40
	.005	8.03	5.42	4.38	3.82	3.45	3.19	2.99	2.84	2.71	2.61
	.001	11.10	7.11	5.60	4.78	4.25	3.89	3.62	3.41	3.24	3.09
inf.	.25	1.32	1.39	1.37	1.35	1.33	1.31	1.29	1.28	1.27	1.25
	.10	2.71	2.30	2.08	1.94	1.85	1.77	1.72	1.67	1.63	1.60
	.05	3.84	3.00	2.60	2.37	2.21	2.10	2.01	1.94	1.88	1.83
	.025	5.02	3.69	3.12	2.79	2.57	2.41	2.29	2.19	2.11	2.05
	.01	6.63	4.61	3.78	3.32	3.02	2.80	2.64	2.51	2.41	2.32
	.005	7.88	5.30	4.28	3.72	3.35	3.09	2.90	2.74	2.62	2.52
	.001	10.83	6.91	5.42	4.62	4.10	3.74	3.47	3.27	3.10	2.96