## List Processing in Ocaml

Given a list of integers ns, suppose we want to return a new list of the same length in which each element is one more than the corresponding element of ns. Here's one way to express this in Java (using the IntList class you've seen in CS111 and CS230).

```
public static IntList incList (IntList ns) {
  if (IntList.isEmpty(ns)) {
    return IntList.empty();
  } else {
    return IntList.prepend(1 + IntList.head(ns), incList(IntList.tails(ns)));
  }
}
```

What are the corresponding list manipulation operators in OCAML?

Java	Ocaml
empty()	[]
<pre>prepend(x,ys)</pre>	x::ys
head(xs)	List.hd(xs)
tail(xs)	List.tl(xs)
isEmpty(xs)	xs = []

In OCAML,  $[E_1; E_2; ...; E_n]$  is syntactic sugar for  $E_1::E_2:...:E_n::[]$ . E.g., we can use this sugar to express a list of the first four positive integers as [1;2;3;4].

Here is an Ocaml transliteration of the Java inclist given above:

```
let rec incList ns =
  if ns = [] then
    []
  else
    (1+List.hd(ns))::(incList (List.tl ns))
```

However, in practice, List.hd and List.tl are rarely used to process lists in OCAML. Instead, we normally use OCAML's powerful pattern matching facility (the match ... with construct) to perform a case analysis on a list:

```
let rec incList ns =
  match ns with
    [] -> []
    | n::ns' -> (n+1)::(incList ns')
```

The expression between match and with (ns in this case) is called the **discriminant**. Following with is a sequence of clauses of the form pattern -> body. The value of the discriminant is compared against the pattern of each clause in the sequence until a match is found. The body of the matching clause is then evaluated in a context that uses the names bound by the pattern-matching process. The result of evaluating the body is returned as the value of the match expression. In the incList example, the clause [] -> [] means "if ns is the empty list, then return the empty list." The clause n::ns' -> (n+1)::(incList ns') means "if ns is a non-empty list whose head is n and whose tail is ns', then return the list that results from prepending n+1 to the result of recursively processing ns'."

The following process function is a contrived example to illustrate pattern matching:

```
let rec process ps =
  match ps with
    [(c,d);(e,f)] -> [(d,f);(c,e)]
  | p1::p2::p3::ps' -> p3::(process(p1::p2::ps'))
  | _ -> ps
```

The underscore pattern, \_, is a special pattern that matches anything without binding the underscore symbol to a value. Here are some sample uses of process:

```
# process [];;
- : ('a * 'a) list = []

# process [(1,2)];;
- : (int * int) list = [(1, 2)]

# process [(1,2);(3,4)];;
- : (int * int) list = [(2, 4); (1, 3)]

# process [(1,2);(3,4);(5,6)];;
- : (int * int) list = [(5, 6); (2, 4); (1, 3)]

# process [(1,2);(3,4);(5,6);(7,8)];;
- : (int * int) list = [(5, 6); (7, 8); (2, 4); (1, 3)]
```

Patterns cannot contain duplicates, but can have when guards:

```
let condswap xs =
  match xs with
    x1::x2::x3::xs' when x1 = x3 -> x2 :: x1 :: x3 :: xs'
    | _ -> xs;;

# condswap [1;2;1;4];;
    - : int list = [2; 1; 1; 4]

# condswap [1;2;3;4];;
    - : int list = [1; 2; 3; 4]
```

Subpatterns can be named by as patterns:

```
let condswap xs =
  match xs with
    x1::x2::((x3::_) as xs'') when x1 = x3 -> x2 :: x1 :: xs''
    | _ -> xs;;
val condswap : 'a list -> 'a list = <fun>
```

In class, we will define the following functions:

```
val sum : int list -> int
sum ns returns the sum of all the integers in a list of integers ns.

# sum [];;
- : int = 0
# sum [3];;
- : int = 3
# sum [3;2;7;5];;
- : int = 17
```

```
val range : int * int -> int list
range (lo, hi) returns a list of integers from lo up to hi, inclusive. The list is empty if lo > hi.

# range (3,7);;
- : int list = [3: 4: 5: 6: 7]
```

```
# range (3,7);;
- : int list = [3; 4; 5; 6; 7]
# range (5,5);;
- : int list = [5]
# range (6,5);;
- : int list = []
```

val squares : int list -> int list squares of the corresponding integers in the list ns.

```
# squares [3;1;5;4;2];;
- : int list = [9; 1; 25; 16; 4]
# squares [3];;
- : int list = [9]
# squares [];;
- : int list = []
```

```
val evens : int list -> int list
```

evens ns returns a list of the even integers in the list ns in the same relative order that they appear in ns. (x mod y gives the remainder of dividing the integer x by the integer y.)

```
# evens [3;1;4;2;5;8;9;6];;
- : int list = [4; 2; 8; 6]
# evens [3;1;5;9];;
- : int list = []
# evens [6;256;100];;
- : int list = [6; 256; 100]
# evens [];;
- : int list = []
```

*Note:* A key benefit of defining list-processing functions like sum, range, squares, evens is that they can be easily composed in mix-and-match ways to solve more complex problems. For example:

```
let sumOfSquaredEvensBetween (lo,hi) =
  sum(squares(evens(range(lo,hi))))
```

val remove : 'a \* 'a list -> 'a list

remove (x, ys) returns a list of all the elements in ys except for occurrences of x. The relative order of non-x elements is preserved.

```
# remove (5, [5;4;5;3;4;2;3;4;5;1;3;5;4;2;5]);;
- : int list = [4; 3; 4; 2; 3; 4; 1; 3; 4; 2]
# remove (5, [1;2;3;4]);;
- : int list = [1; 2; 3; 4]
# remove (5, []);;
- : int list = []
```

val isMember: 'a \* 'a list  $\rightarrow$  bool isMember(x,ys) returns true if x is an element of the list ys (as determined by =) and false otherwise.

```
# isMember(3,[5;2;3;1;4]);;
- : bool = true
# isMember(6,[5;2;3;1;4]);;
- : bool = false
# isMember("be",["to";"be";"or";"not";"to";"be"]);;
- : bool = true
# isMember("two",["to";"be";"or";"not";"to";"be"]);;
- : bool = false
# isMember((2,"two"), [(3,"three");(1,"one");(2,"two");(4,"four")]);;
- : bool = true
# isMember((2,"too"), [(3,"three");(1,"one");(2,"two");(4,"four")]);;
- : bool = false
```

val removeDups : 'a list -> 'a list

removeDups xs returns a list containing one occurrence of each element in xs. The order of elements in the returned list is unspecified. *Note:* There are many ways to define this function!

```
# removeDups [5;4;5;3;4;2;3;4;5;1;3;5;4;2;5];;
- : int list = [1; 3; 4; 2; 5] (* order doesn't matter *)
# removeDups ["do";"be";"do"];;
- : string list = ["be"; "do"] (* order doesn't matter *)
# removeDups ['a';'b';'r';'a';'c';'a';'d';'a';'b';'r';'a'];;
- : char list = ['c'; 'd'; 'b'; 'r'; 'a'] (* order doesn't matter *)
# removeDups [];;
- : '_a list = []
```

val isSorted : 'a list -> bool

isSorted xs returns true if the list xs is sorted from low to high according to <=, and false otherwise.

```
# isSorted [];;
- : bool = true
# isSorted [3];;
- : bool = true
# isSorted [3;1;4;2];;
- : bool = false
# isSorted [1;2;3;4];;
- : bool = true
# isSorted [false;true];;
- : bool = true
# isSorted [true;false];;
- : bool = false
# isSorted ['a';'b';'c'];;
- : bool = true
# isSorted ['c';'a';'b'];;
- : bool = false
# isSorted ["one";"two";"three"];;
- : bool = false
# isSorted ["one";"three";"two"];;
- : bool = true
# isSorted [(1,"bar");(2,"baz");(3,"foo")];;
- : bool = true
# isSorted [(1,"bar");(3,"baz");(2,"foo")];;
- : bool = false
# isSorted [(1, "foo");(2, "bar");(3, "baz")];;
- : bool = true
# isSorted [[];[1];[1;2];[1;3;2];[1;3;4];[1;4];[2]];;
- : bool = true
# isSorted [[];[1];[1;2;3];[1;2];[1;3;4];[1;4];[2]];;
- : bool = false
```

val flatten : 'a list list -> 'a list

flatten xss returns a list containing all of the elements of the lists in the list of list xss in the same order. Use the infix @ operator or prefix List.append operator to append two lists. Note: The flatten function is called List.flatten in the OCAML standard library.

```
# flatten [[4;2];[3;1;5;8];[7];[6;0;9]];;
- : int list = [4; 2; 3; 1; 5; 8; 7; 6; 0; 9]
# flatten [["foo"];["bar";"baz"];["quux"]];;
- : string list = ["foo"; "bar"; "baz"; "quux"]
# flatten [["foo"]];;
- : string list = ["foo"]
# flatten [];;
- : 'a list = []
```

val reverse : 'a list -> 'a list

reverse xs returns a list containing the elements of the list xs in reverse order. Note: This function is called List.rev in the OCAML standard library.

```
# reverse [3;1;5;4;2];;
- : int list = [2; 4; 5; 1; 3]
# reverse ["foo";"bar";"baz"];;
- : string list = ["baz"; "bar"; "foo"]
# reverse ["foo"];;
- : string list = ["foo"]
# reverse [];;
- : 'a list = []
```

```
val zip : 'a list * 'b list -> ('a * 'b) list
```

zip (xs,ys) returns a list of pairs containing the corresponding elements of the lists xs and ys. The length of the resulting list is the length of the shorter of xs and ys. Note: A curried version of this function is called List.combine in the OCAML standard library.

```
# zip ([1;2;3],['a';'b';'c']);;
- : (int * char) list = [(1, 'a'); (2, 'b'); (3, 'c')]
# zip ([1;2;3;4;5],['a';'b';'c']);;
- : (int * char) list = [(1, 'a'); (2, 'b'); (3, 'c')]
# zip ([1;2;3],['a';'b';'c';'d';'e']);;
- : (int * char) list = [(1, 'a'); (2, 'b'); (3, 'c')]
# zip ([],['a';'b';'c'']);;
- : ('a * char) list = []
# zip ([1;2;3],[]);;
- : (int * 'a) list = []
```

```
val unzip : ('a * 'b) list -> 'a list * 'b list
```

unzip ps takes a list of pairs ps and returns a pair of lists, the first of which contains all the first components of ps, and the second of which contains all the second components of ps. Note: This function is called List.split in the OCAML standard library.

```
# unzip [(1, 'a'); (2, 'b'); (3, 'c')];;
- : int list * char list = ([1; 2; 3], ['a'; 'b'; 'c'])
# unzip [(2, 'b')];;
- : int list * char list = ([2], ['b'])
# unzip [];;
- : 'a list * 'b list = ([], [])
```

val mapcons: 'a \* 'a list list  $\rightarrow$  'a list list mapcons (x,zss) returns a list containing the result of prepending x to each list in the list of lists zss.

```
# mapcons (5,[[4;1];[3];[2;1;3];[]]);;
- : int list list = [[5; 4; 1]; [5; 3]; [5; 2; 1; 3]; [5]]
# mapcons ("foo", [[]]);;
- : string list list = [["foo"]]
# mapcons ("foo", []);;
- : string list list = []
```

## val subsets : 'a list -> 'a list list

Assume that xs is a list without duplicates, and thus represents a set of elements. subsets xs returns a list of lists containing all subsets of xs. The elements of each subset must appear in the same relative order as in xs, but the order of the subsets themselves is unspecified. *Hint:* mapcons is helpful here.

```
# subsets [];;
- : '_a list list = [[]]
# subsets [4];;
- : int list list = [[]; [4]]
# subsets [3;4];;
- : int list list = [[]; [4]; [3]; [3; 4]]
# subsets [2;3;4];;
-: int list list = [[]; [4]; [3]; [3; 4]; [2]; [2; 4]; [2; 3]; [2; 3; 4]]
# subsets [1;2;3;4];;
- : int list list =
           [3]; [3; 4];
                                 [2];
                                         [2; 4];
                                                    [2; 3];
[[]; [4];
                                                              [2; 3; 4];
 [1]; [1; 4]; [1; 3]; [1; 3; 4]; [1; 2]; [1; 2; 4]; [1; 2; 3]; [1; 2; 3; 4]]
# subsets ['a';'b';'c';'d'];;
- : char list list =
[[]; ['d']; ['c']; ['c'; 'd']; ['b']; ['b'; 'd']; ['b'; 'c'];
 ['b'; 'c'; 'd']; ['a']; ['a'; 'd']; ['a'; 'c']; ['a'; 'c'; 'd']; ['a'; 'b'];
 ['a'; 'b'; 'd']; ['a'; 'b'; 'c']; ['a'; 'b'; 'c'; 'd']]
```

## val decimal : int list -> int

Assume that bs is a list of zeroes and ones. decimal bs returns an integer that is the decimal representation of the number represented in binary by bs. An empty list of bits is assumed to denote 0.

```
# decimal [];;
-: int = 0
# decimal [0];;
-: int = 0
# decimal [1];;
-: int = 1
# decimal [1;0];;
-: int = 2
# decimal [1;0;0];;
-: int = 4
# decimal [1;0;1];;
-: int =5
# decimal [1;0;1;0];;
- : int = 10
# decimal [1;0;1;1];;
- : int = 11
# decimal [1;0;1;1;0];;
-: int = 22
# decimal [1;0;1;1;1];;
-: int = 23
# decimal [1;0;1;1;1;0];;
-: int = 46
```