

You want to test whether therapy sessions decrease stress levels of patients. For this purpose you obtained 10 measurements of stress on the scale from 0 to 100. Assuming symmetrical (but not normal) probability distribution (of differences), find out if stress levels change after therapy. Use $\alpha = 0,05$

Patient	1	2	3	4	5	6	7	8	9	10
Before	75	68	83	90	70	98	72	99	75	98
After	68	70	60	95	51	90	75	88	60	80

$B_i - A_i$ 7 -2 23 -5 19 8 -3 11 15 18

$$H_0: X_{0.5} = C = 0 \quad \alpha = 0.05$$

$$H_A: X_{0.5} \neq 0$$

$$\begin{array}{cccccccccccc} & & & \nearrow & & & & & & & & \\ 2 & 3 & 5 & 7 & 8 & 11 & 15 & 18 & 19 & 23 \\ 1 & 2 & 3 & 4 & 5 & 6 & 7 & 8 & 9 & 10 \end{array}$$

Σ pořadí, které náleží $d_i > 0$

$$S^+ = 49$$

8 je hodnota z tabulky

$$\bar{W}_\alpha = \left(8; \frac{n(n+1)}{2} - 8 \right) = (8; 47)$$

$$S^+ \notin \bar{W}_\alpha \Rightarrow \text{zamítáme } H_0$$

došlo ke změně hl. stresu

You want to compare monthly income similarly employed people in 2 different regions. Since you can't account for different occupations, you expect the underlying probability distributions to be heavily skewed. Using $\alpha = 0,05$ and following data [1000 Kč], test whether the median income is the same.

X	73	<u>11.5</u>	<u>4</u>	<u>1.5</u>	<u>5</u>	<u>16</u>	<u>17</u>	<u>7</u>	<u>8</u>	<u>3</u>	
a	R 1	43,6	41,2	40,7	41,6	47,2	49,0	42,1	42,2	40,8	
10	R 2	43,7	49,5	43,1	43,4	45,2	47,0	43,6	40,7	41,8	55,2
Y	106	<u>13</u>	<u>18</u>	<u>9</u>	<u>10</u>	<u>14</u>	<u>15</u>	<u>11.5</u>	<u>1.5</u>	<u>6</u>	<u>19</u>

$$H_0: X_{0.5} = Y_{0.5}$$

$$H_A: X_{0.5} \neq Y_{0.5}$$

- Data dohromady \Rightarrow veľký soubor
- u počítať
- Suma poradií pre prvky z X

$$S^X = 73$$

$$U_x = n_x n_y + \frac{n_x(n_x+1)}{2} - S_x = 90 + 45 - 73 = 135 - 73 = \underline{\underline{62}}$$

$$\min \left\{ \begin{matrix} 180 \\ 9 \end{matrix} U_x, \begin{matrix} -62 \\ 10 \end{matrix} n_x(n_x+n_y+1) - U_x \right\} = \min \{ 62, 1183 \} = \underline{\underline{62}} = t$$

$$\bar{W}_\alpha = (20, \text{práva hranice} - 20)$$

$$t \in \bar{W}_\alpha \Rightarrow \underline{\underline{H_0 \text{ nezamietame}}}$$

Test whether there is some monotonous relation between the amount of points obtained before the exam and during the exam of some course taught at BUT. Use $\alpha = 0,05$ and following observations.

		10	8	2	5	4	6	7	9	3	1
R_x	before	40	35	21	31,5	28,5	33,5	34	38	25	20
R_y	during	60	51	42	40	43,5	47	52	58,5	55	40
		10	6	3	1.5	4	5	7	9	8	1.5

$$n = 10$$

$$\bar{R}_x = \frac{n(n+1)}{2n} = \frac{11}{2} = 5.5 = \bar{R}_y$$

$$10 \cdot 5.5 \cdot 5.5 = 302.5$$

$$\bar{R} - R$$

4.5	2.5	3.5	0.5	1.5	0.5	1.5	3.5	2.5	4.5
4.5	0.5	2.5	4	1.5	0.5	1.5	3.5	2.5	4

$$s(R_x) = 3,0277$$

$$s(R_y) = 3,0185$$

$$r(R_x, R_y) = 0.9356$$

$$t = \frac{11 \sqrt{n-2}}{\sqrt{1-R^2}} = 3,07 \quad \begin{matrix} t \notin W_\alpha \\ \Rightarrow \text{2. unit. Ho} \end{matrix}$$

$$\bar{W}_\alpha = (0; t_{1-\frac{\alpha}{2}}(n-1)) = (0; 2.306)$$

BONUS

Logistic regression model