

Value-Suppressing Uncertainty Palettes

Leave Authors Anonymous
for Submission
City, Country
e-mail address

Leave Authors Anonymous
for Submission
City, Country
e-mail address

Leave Authors Anonymous
for Submission
City, Country
e-mail address

ABSTRACT

Understanding uncertainty is critical for many analytical tasks. One common approach is to encode data values and uncertainty values independently, using two visual variables. These resulting bivariate maps can be difficult to interpret, and interference between visual channels can reduce the discriminability of marks. To address this issue, we contribute Value-Suppressing Uncertainty Palettes (VSUPs). VSUPs allocate larger ranges of a visual channel to data when uncertainty is low, and smaller ranges when uncertainty is high. This non-uniform budgeting of the visual channels makes more economical use of the limited visual encoding space when uncertainty is low, and encourages more cautious decision-making when uncertainty is high. We demonstrate several examples of VSUPs, and present a crowdsourced evaluation showing that, compared to traditional bivariate maps, VSUPs encourage people to more heavily weight uncertainty information in decision-making tasks.

ACM Classification Keywords

H.5.0. Information Interfaces and Presentation (e.g. HCI): General

Author Keywords

Uncertainty Visualization; Color Perception; Thematic Maps; Semiotics.

INTRODUCTION

Uncertainty is an inescapable component of collecting, analyzing, and presenting data. A common goal in the communication of uncertainty is promoting *uncertainty-aware decisions*: the audience should be aware of the risks and rewards of certain decisions, modulate their confidence in their conclusions, and perhaps refrain from making a decision at all if there is too much uncertainty. A way that designers can contribute to this goal is by ensuring that uncertainty information is *well-integrated* with the rest of the data. That is, it should be difficult to discount or ignore the uncertainty in a dataset.

Simultaneous presentation of uncertainty and value necessitates the construction of a bivariate map — a relation, in terms

Permission to make digital or hard copies of all or part of this work for personal or classroom use is granted without fee provided that copies are not made or distributed for profit or commercial advantage and that copies bear this notice and the full citation on the first page. Copyrights for components of this work owned by others than the author(s) must be honored. Abstracting with credit is permitted. To copy otherwise, or republish, to post on servers or to redistribute to lists, requires prior specific permission and/or a fee. Request permissions from permissions@acm.org.

CHI'16, May 07–12, 2016, San Jose, CA, USA

© 2016 Copyright held by the owner/author(s). Publication rights licensed to ACM. ISBN 123-4567-24-567/08/06...\$15.00

DOI: http://dx.doi.org/10.475/123_4

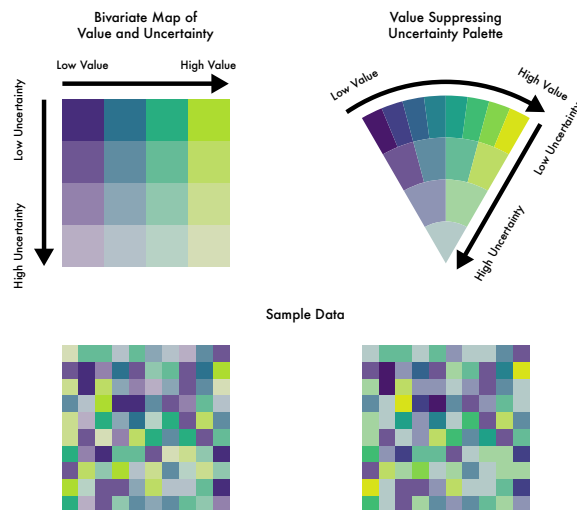


Figure 1: A standard bivariate map (left) and a VSUP (right), used to encode an identical 10x10 grid of random data. Both use the same visual channels to encode value (position along the Viridis [42] color map) and uncertainty (lightness and saturation). However, the VSUP uses a tree-like structure to allocate colors, defining more bins when uncertainty is low. This non-uniform budgeting affords better discrimination between values when uncertainty is low, even though the VSUP has fewer color bins (in this case, 15 to the bivariate map's 16). This tree-like structure also discourages analysis in regions where uncertainty may be unacceptably high.

of visual variables, between 2-tuples (value, uncertainty) and mark properties. Due to the interference and interplay between different visual variables, bivariate maps may suffer from limited discriminability.

In this paper, we contribute **Value-Suppressing Uncertainty Palettes** (VSUPs) for integrating data and uncertainty information in visualizations. VSUPs intentionally alias together data values with high uncertainty, affording greater discriminability as uncertainty decreases. Traditional bivariate maps might be thought of as a 2D square, with differing outputs for each combination of value and uncertainty. In contrast, VSUPs can be conceptualized as arcs: as uncertainty increases, values are mapped to smaller and smaller sets of outputs, culminating in a singularity where all inputs are mapped to an identical, highly uncertain mark regardless of data value. Figure 1 shows examples of both a traditional bivariate map and a VSUP.

We describe the motivations for VSUPs, provide examples of their utility for decision-making under uncertainty, and assess VSUPs in a crowdsourced experiment. Our results indicate that VSUPs create close integration between uncertainty and data, resulting in better performance at data tasks with uncertainty components.

RELATED WORK

Despite the acknowledged importance of uncertainty in understanding data, explicit representations of uncertainty are often missing from visualizations [5]. This is partially due to the complexity of uncertainty as a concept. In typologies from Thomson et al. [38] and Buttenfield & Beard [7], the authors note that many, occasionally contradictory, concepts can fall under the category of “uncertainty,” including data quality, sampling error, credibility, and provenance.

Reviewing the state of the art in uncertainty visualization in the field, Greithe et al. [17] and Brodlie et al. [6] present lists of potential techniques for conveying uncertainty in concert with data. Some of these options (interaction, animation, and sonification) are not applicable for static charts; even for dynamic charts, many users do not interact with charts in sufficient detail to recover uncertainty information [40]. While we acknowledge the potential utility of these techniques in uncertainty visualization (for instance, the animation used to convey sampling error in Hullman et al.’s Hypothetical Outcome Plots [20]), we limit the scope of our discussion to techniques which center on static charts.

Visual Variables for Uncertainty

One challenge of uncertainty visualization is that the decision to explicitly encode uncertainty increases the dimensionality of the data, and so requires the use of (at least one) additional visual channel [6]. Uncertainty therefore inherently increases the visual complexity of a visualization. When the data are already complex to convey, and many of the more common or accurate visual variables are in use, allocating an additional dimension is non-trivial. As the number of dimensions increases, finding visual variables that are both perceptually accurate (in either estimation of quantity or discrimination of category) as well as perceptually separable from all the other encoding channels, becomes increasingly difficult.

A further hurdle is that not all visual variables are well-suited for conveying uncertainty. MacEachren et al. [23] evaluate a number of visual variables with respect to their *semiotic fit* for representing uncertainty. They observe that certain visual variables such as blurriness and transparency seem to have a more intuitive connection to uncertainty than other variables such as shape or hue. Unfortunately, Boukhelifa et al. [4] find that many visual variables habitually used for conveying uncertainty, such as blur and value, are also difficult to estimate. This results in a preference/performance gap where designers must choose between encoding uncertainty in a way that is intuitive but error prone, or use higher fidelity channels that may not intuitively convey uncertainty.

Bivariate Maps

While uncertainty can be visualized entirely separately from the rest of the data (for instance, in a juxtaposed chart), this

runs the risk that uncertainty information becomes *ignorable* [26]. It also complicates analysis, as interpreting the value and uncertainty of a given data point requires consulting two separate charts. To integrate uncertainty information into an analysis, we focus on the construction of *bivariate maps*, where value and uncertainty information is displayed simultaneously in a spatially co-located manner.

Bivariate maps can, in principle, be constructed from the combination of any two visual variables (such as shape and color, or size and texture). For example Ware’s “textons” [45] overlay glyphs on top of regions to simultaneously encode two quantitative values. However, for spatial visualizations like choropleth maps, heatmaps, and treemaps, visual channels such as position and length are reserved for data variables other than value (such as geographic location or relative size). In these situations, data value is often encoded using color. Bivariate maps in these settings therefore typically rely on a visual channel related to color for encoding a secondary variable, such as opacity [35] or pixel noise [22].

Colors in univariate quantitative color maps should be sufficiently far apart as to be perceptually distinguishable [44], and vary in lightness as well as hue to afford an implicit ordering of value [2, 33]. Different choices of color maps can highlight different features of the data, and should be chosen with care [34]. These principles extend to bivariate color maps, with the additional consideration that our perception of color channels lacks *orthogonality*. That is, while we can perceive e.g., the height of a bar in a bar chart independently of its width, a particular property of a color (e.g., its redness, saturation, transparency, etc.) affect how its other properties are perceived [15, 46]. Many color channels such as hue and saturation are therefore perceptually *integral*, which complicates their use in bivariate maps.

Another recurring design consideration when constructing color maps is whether to quantize data into a discrete set of colors, or to encode data using a continuous mapping. While continuous color maps afford greater fidelity in presenting values [27], non-linearity in human color perception introduces errors in extracting numeric values from continuous colors [2]. Quantizing a color map is therefore an exercise in balancing *perceptual error* and *quantization error* [13]. Discrete maps offer finer control over this balance, which can result in better performance in tasks involving heatmaps [30].

In general, the quality of bivariate color maps is a multivariate measure involving consideration of not just the component color channels, but also the interpolation scheme and the color of the surround [1]. However, even simple bivariate maps can be difficult for a general audience to interpret: due to their additional complexity, Wainer & Francolini [43] reported high levels of error for participants even for “elementary” graph reading tasks, and additionally that bivariate legends were more difficult to memorize and internalize than their univariate equivalents. Therefore, bivariate maps in practice are often limited to a small set of output colors [32, 39] (say, a 4x4 matrix as in Figure 1).

Given that bivariate maps, for reasons of either practicality or perceptual fidelity, have only a limited budget of outputs, we adapt an insight from Dunn [14] that these limited categories ought to be assigned with regards to their importance to analysis tasks, rather than uniformly. Our Value-Suppressing Uncertainty Palettes apply this insight to data with uncertainty. Frequently, uncertain information ought to be weighted less heavily in a decision-making process, or at least have less prominence in an analysis, than certain information.

Correll et al. [8, 9] use a precursor of VSUPs in their LayerCake genomics visualization tool, where marks representing genomic data with increasing uncertainty are mapped to a smaller and smaller set of increasingly grey colors, creating the effect of uncertain values retreating into a “confidence fog” while highly certain values remain prominent. Other bivariate visualizations implicitly alias together uncertain values through perceptual integrality. For instance, if uncertainty is encoded by transparency, a maximally uncertain glyph may be entirely transparent, and so impossible to distinguish from any other maximally uncertain glyph. Other channels with a semiotic connection to uncertainty, such as saturation, value, blur, or size, have similar deleterious effects on the disambiguation of colors and shapes. In both cases, the property of aliasing is *ad hoc*, and places no guarantees on the discriminability of colors. The binning and degradation approach of VSUPs makes the choice to alias values explicit to both the designer and the viewer, and results in a bivariate mapping with known perceptual properties.

VALUE-SUPPRESSING UNCERTAINTY PALETTES

Value-Suppressing Uncertainty Palettes (VSUPs) are a technique for creating bivariate maps of data *value* and *uncertainty*. VSUPs make two central assumptions about bivariate maps:

1. There is a limited *budget* for perceptual discriminability.
2. Differences among *certain* data are more germane than differences among *uncertain* data.

In some cases, these assumptions are violated. For instance, an analyst might be interested in “long tail risks” or other “black swan events,” where the impact of a value, no matter how uncertain, must be considered and planned for [37]. Other analysis tasks (such as filtering out outliers), require increased, rather than decreased, discriminability when uncertainty is high. However, for many information fusion tasks, the assumption is that uncertainty is related to data quality, or the uncertainty of data values [31].

If both of these assumptions hold, then it follows that the designer of a bivariate map should allocate more mark types to certain values, and fewer mark types to uncertain values. VSUPs codify this decision by *reducing the number of mark categories for representing value as uncertainty increases*. This means that data encoded using a VSUP will make visible only the largest of differences in uncertain data, but highlight comparatively small differences in value when uncertainty is low. VSUPs therefore act as both a filtering mechanism (in that values with too much uncertainty are mapped to the same glyph), as well as an implicit test of effect size (in that smaller and smaller changes in value are visible as uncertainty

decreases). This strategy of dampening low quality or highly uncertain values in maps in order to focus on more informative regions has measurable benefits, including the removal of statistically spurious visual patterns, and the highlighting of regions of interest [11].

VSUPs rely on an underlying **quantization tree** that governs how values are discretized. Values about a certain uncertainty threshold are mapped to a singular “root” node. As uncertainty decreases, the tree branches into leaves, which evenly divide the data domain. The data value of a parent is the midpoint of all of its children. These leaves can then branch again, up to a designer-specified stopping point. The layers quantize the uncertainty domain, and sibling nodes quantize the data domain. Figure 1 shows a VSUP with a tree with a branching factor of 2 and 4 layers, resulting in an output range with 15 distinct colors.

Since the visual channel used to encode uncertainty (e.g., saturation, lightness, transparency) often reduces the ability of people to distinguish colors, VSUPs have the added benefit of creating bivariate palettes that are perceptually easier to distinguish, by reducing color resolution in precisely the areas where color disambiguation would be most difficult anyway. For instance, the two closest colors in the VSUP in Figure 1 are 1.4 units farther apart in CIELAB color space than the two closest colors in the traditional bivariate map.

JavaScript code for generating VSUPs for use in D3 [3] charts is available at [URL-REMOVED-FOR-REVIEW](#).

Design Considerations

There are multiple choices that designers must make before creating a VSUP. Specifically, they must choose which visual channels map to value (1), uncertainty (2), and the structure of the underlying VSUP tree (3).

When selecting a visual channel to represent uncertainty, we recommend channels with both a strong semiotic connection to uncertainty (such as those recommended by MacEachren et al. [23]) as well as a relatively large number of perceptually distinguishable levels (such as those evaluated by Boukhelifa et al. [4]). Here, we focus on a combination of increasing color value and decreasing saturation. Correll & Gleicher [10] provide evidence that even audiences without statistical training can successfully interpret uncertainty information encoded in these channels.

When selecting a visual channel to represent value, the designer should consider the perceptual integrality of the value and uncertainty visual channels. For instance, we use the Viridis [42] color map frequently in this paper, as many standard color ramps (such as sequential ColorBrewer [19] ramps), following usual best practices, interpolate in both hue and luminance [44]. This interpolation in luminance interferes with our uncertainty encoding, introducing ambiguity. Ramps such as Viridis, which avoid very light and very dark colors, reduce this ambiguity.

When determining the quantization tree, the design should be careful to avoid having too many output colors. For reasons of memorability and complexity, Wainer & Francolini [43]

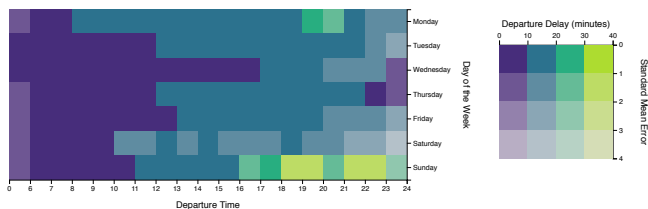


Figure 2: Average departure delay for different times of the day and days of the week visualized with a 2D uncertainty map. Horizontal position is the hour of scheduled departure, and vertical position is the day of the week.

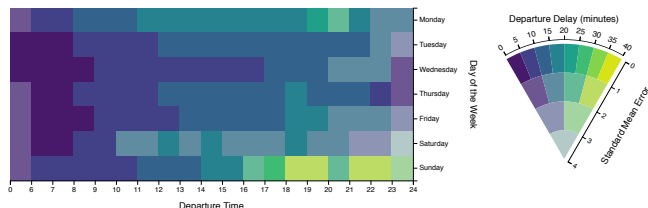


Figure 3: Flight delay data encoded with a VSUP.

suggest no more than 16 distinct outputs in bivariate maps. For a binary quantization tree, this results in a maximum tree depth of 4, as seen in Figure 1. In general, for tasks that require finer-grade distinctions between uncertainty, the depth of the tree could be increased. For tasks involving finer-grade distinctions between value, the branching factor of the tree could be increased. However, these factors increase the number of colors, and so designers should moderate between legend complexity and data fidelity. Beyond these two parameters, non-uniform binning would allow the designer to target particular distributions or important subregions of the data that would otherwise be difficult to visualize in a limited palette, as in Dunn’s [14] dynamic bivariate maps. As an additional form of control, prior tools using VSUP-like techniques, such as LayerCake [8], allow the analyst to control the bins in the tree through interaction with the color legend.

EXAMPLES

We present a set of examples showing how VSUPs can be applied to real-world datasets. VSUPs allocate color bins asymmetrically amongst value and uncertainty regions, affording greater discriminability in regions of the chart that warrant closer scrutiny, while discouraging exploration of regions with noisy or unreliable signals.

Air Travel Delay

Using a public data set from the U.S. Bureau of Transportation Statistics [29], we created a heatmap showing average flight delay for different times of the day and days of the week for U.S. carriers in January 2017. We use standard error (σ/\sqrt{n}) as our measure of uncertainty. We created two alternate heatmaps of this delay information. Figure 2 shows a traditional bivariate map, whereas Figure 3 shows a VSUP generated under the same constraints.

Both maps illustrate a similar trend: flight delays are shorter towards the beginning of the day, increasing on average over

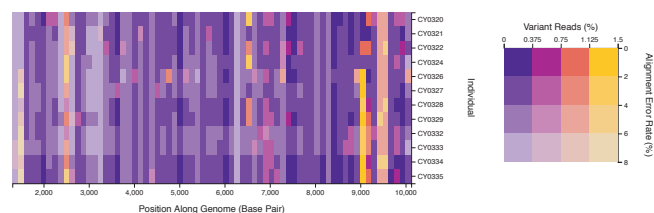


Figure 4: Variability for 12 different viral populations of the SIV virus, encoded with a traditional 2D bivariate map. Horizontal position denotes location along the SIV genome. Each row is the viral population of a different infected animal. Error in aligning short reads can lead to poor quality data, and so the amount of these errors is encoded as the uncertainty.

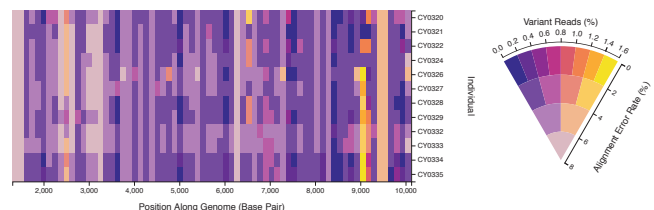


Figure 5: Variability for 12 different viral populations of SIV, encoded with a VSUP. By suppressing uncertain information, the VSUP version removes the apparent spike in value at the second column, which is an artifact of sampling error due to poor coverage in that region. It also suppresses apparent inter-species variability in the solid orange spike at location 9,500, which, again, is a function of poor coverage rather than a genuine per-strain difference.

time. The traditional bivariate map affords only a coarse examination of this trend: two visible “blocks” of color, early in the day, and later in the afternoon. The VSUP, in contrast, has sufficient color resolution to show a quasi-linear trend. Uncertainty is high only for a few bins for which there are small number of flights, either on the weekends or late at night. The VSUP does not obscure any significant trends in the high uncertainty data, despite having fewer color categories overall.

Viral Mutation

Next generation sequencing allows biologists to collect and analyze large amounts of genomics data. However, these techniques often create data quality issues, as they must align large numbers of potentially ambiguous “reads” of relatively small numbers of base pairs. Using a dataset from a group of virologists interested in the population dynamics of viral mutation [28], we visualized the variability in viral genomes across 25 populations of the simian immunodeficiency virus (SIV). In the dataset here, it is important not only to identify hotspots in the viral genome (locations with high rates of mutation or variability), but also to not be distracted by false positives. The traditional bivariate map (Figure 4) has many locations with apparent inter-population variance.

VSUPs (Figure 5) enable biologists to explore interesting patterns while deemphasizing noise. Orange hot spots towards the beginning (the second column) and end of the genome

(around reference nucleotide 9,500) could be considered potential regions of interest in the 2D map; in the VSUP these are encoded as highly uncertain and of ambiguous value. In fact, these regions have systematically low coverage; the lack of reliable data for these regions should discourage analysts from giving their apparent pattern equal consideration from the stronger signals elsewhere in the genome.

EVALUATION

We performed two crowdsourced experiments on Amazon’s Mechanical Turk to evaluate the effectiveness of VSUPs for integrating uncertainty and value information in visualizations. This focus on integration meant that we limited our experimental tasks to scenarios where the participants needed to consider both value and uncertainty before making a decision. Each experiment focused on one of two separate tasks:

1. An **identification** task, where we gave participants charts with value and uncertainty information, and asked them to locate specific regions. E.g., “click on the region of the chart with a value of 0.1 and an uncertainty of 0.2.”
2. A **prediction** task, inspired by the game Battleship, where we gave participants charts with both *forecast* and *forecast uncertainty* information, and asked the participants to place tokens on the board in order to optimize expected value. E.g., “place your 5 ships on safe locations on the board.”

We limited our population to Turkers from the United States, with a prior task approval rate of at least 90%. As the experimental tasks required multi-hue color perception, we presented participants with a set of Ishihara plates [18] as a pre-test, and excluded participants who either misidentified the values in the plates, or who self-reported as having a color vision deficiency (CVD) in the post-test. Based on piloting, we paid participants \$2 dollars for participation, for a target rate of \$8/hour. After completion of the main tasks, we solicited demographic information, including a risk aversion assay from Mandrik & Bao [24]. Participants from the first experiment were excluded from participating in the second.

Experimental materials, including data tables and stimuli generation code, are available at [URL-REMOVED-FOR-REVIEW](#).

Identification Experiment

We wished to determine what effects, if any, our various design considerations had on performance at a basic analysis task: using a bivariate legend to interpret a heatmap. There are a number of design decisions to be made even after one has determined which two visual channels will be used to encode value and uncertainty. In particular:

1. Whether or not to *juxtapose* or *superimpose* the data and uncertainty maps.
2. Whether or not to *discretize* each visual channel, or encode values *continuously*.
3. Whether or not to use a *square* legend, which gives equal area to each bin, or a *wedge* legend, which reduces in size as uncertainty increases.

4. If discretizing, whether to employ a *VSUP* or a *standard* quantization scheme.

For the identification task, we gave participants a 5x5 heatmap, and asked them to click on a region of the heatmap that encodes a particular (value, uncertainty) pair. To support comparability across conditions, we chose a set of target pairs such that each target mapped to a unique color across all encoding types. This resulted in $(4+4+2+1)=11$ valid targets. For each trial, we placed one example of each of these 11 targets randomly in a heatmap; the remaining 13 cells of the heatmap were randomly sampled from this target list. Thus there could be multiple correct locations in each trial, deterring a strategy of looking for “oddball” colors.

We selected this task both as a way of assessing the ability of people to successfully encode and decode values using a bivariate map, and to provide training for the prediction task (since we re-used the bivariate maps in that task). We measured performance both in terms of accuracy (did the participant select the correct point) as well as response time.

We recruited 24 participants for this task: 12 female, 12 male, ($M_{\text{age}} = 31$, $SD_{\text{age}} = 7.8$). Each of the participants saw the data encoded as each of 8 types of bivariate encoding and legend, with 8 replications, for a total of 64 stimuli. Figure 6 shows these factor levels.

Hypotheses

We had two initial hypotheses, informed by prior work:

1. Juxtaposed maps, by introducing a second search task to the identification task (searching for the proper values in two, rather than one map), would have poorer performance than other conditions.
2. Continuous maps require more specific and accurate color matching between value and color, and so would have poorer performance than discrete conditions.

We had no strong hypotheses about the shape of the legend (square vs. wedge), but, as the wedge shape makes more uncertain bins in the legend smaller (and thus potentially harder to disambiguate), we included it as a check against VSUPs which explicitly alias uncertain values. For this identification task, which did not involve reasoning with uncertainty, but simply matching colors to a color legend, we also did not have strong hypotheses about performance differences between VSUPs and traditional discrete bivariate maps.

Results

We performed a repeated measures ANOVA on our results to measure the effect of juxtaposed versus superimposed maps, and continuous versus discrete legends, on accuracy. Participant ID was included as a random effect. Figure 7 shows the performance of each of our 8 conditions.

The results support our first hypothesis. Juxtaposition was a significant effect ($F(1, 166) = 5.5, p = 0.02$). A post-hoc t-test confirmed ($t = 2.5, p = 0.01$) that superimposed charts ($M = 0.58, SD = 0.5$) performed significantly better than juxtaposed ($M = 0.51, SD = 0.49$) ones. For our identification task, juxtaposition requires at least two search tasks (one to

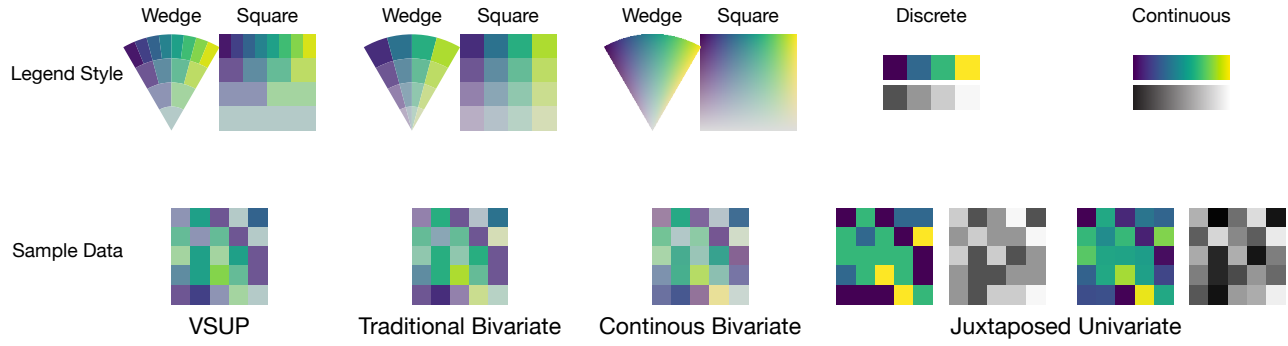


Figure 6: The 8 conditions from the identification experiment. Juxtaposed maps require a participants to make an error-prone connection between areas in two separate maps in order to make a decision that integrates value and uncertainty. Traditional bivariate maps integrate both value and uncertainty. VSUPs attempt to improve on traditional bivariate maps by reducing color resolution as uncertainty increases, discouraging conclusions based on noisy or imprecise data.

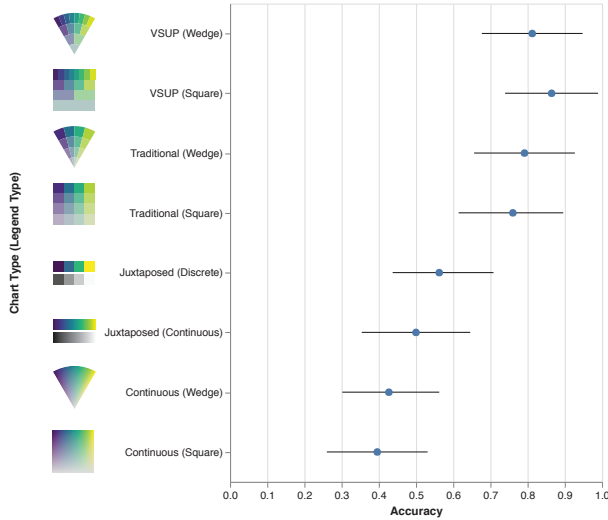


Figure 7: Accuracy results for the identification experiment. For examples of each condition, see Figure 6. Juxtaposing two univariate maps for both value and uncertainty requires an error-prone search task for identification tasks. Continuous rather than discrete bivariate maps requires an error-prone color encoding and estimation task. Discrete bivariate maps, both VSUPs and otherwise, avoid these issues. The confidence intervals are bootstrapped 95% CIs of trimmed means.

locate squares with the correct data value, another to locate ones with the correct uncertainty value), which introduces additional error compared to conditions where value and uncertainty are displayed simultaneously. This is reflected also in response times, which, although highly variable, were highest in juxtaposed conditions ($M = 19s$, $SD = 65$), than the other conditions ($M = 13s$, $SD = 38$), although this difference was not significant ($t = 1.64$, $p = 0.1$).

The results also support our second hypothesis. Discretization was a significant effect ($F(1, 166) = 30$, $p < 0.01$). A post-hoc t-test confirmed ($t = 6.1$, $p < 0.01$) that charts with discrete bins ($M = 0.63$, $SD = 0.48$) performed significantly better than charts with continuous color maps ($M = 0.47$, $SD = 0.5$). The lack of quantization bias in continuous maps is countered by the perceptual error in precisely estimating value from color. Relying on a discrete set of output colors simplifies this task.

We performed a second ANOVA among the superimposed discrete charts to determine the effect of legend shape (wedge or square) and quantization scheme (VSUP or standard) on performance, with participant ID as a random factor. We did not find a significant effect for either the legend shape ($F(1, 70) = 0.03$, $p = 0.084$) or the quantization scheme ($F(1, 70) = 1.4$, $p = 0.24$).

Prediction Experiment

For the prediction task, we gave participants the rules of a game similar to Battleship. Greis et al. [16] employ these game-like experimental tasks to assess how different visual designs communicate uncertainty information, which can be abstract or complex, to the general audience. In our task, the participant and a (fictional) adversary have to place tokens representing ships on a 5x5 spatial grid, with the expectation that certain squares will be hit by missiles. Players have to place all their tokens before continuing. The objective is to minimize the number of your own ships that are hit. In our task, participants were given a map representing the predictions of missile strikes in each location on the grid. The *value* component was the ship's *danger* if placed on the square. The *uncertainty* component was the confidence in this prediction. Other studies of uncertainty representation,

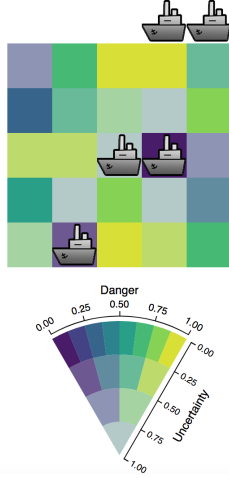


Figure 8: The prediction task. The participant has a list of locations, and ought to place their ships on locations with low probability of attack, and high certainty in this probability.

such as in Cox et al. [12], have used "prediction + prediction uncertainty" stimuli to elicit differences in decision-making between visualizations of uncertainty.

Our stimuli were created by randomly sampling from values that fell within each of the 16 bins of the 4x4 2D bivariate color map. This resulted in 16 samples. The remaining 9 samples were "bad" values, with low safety and high certainty. This created 4 quartile categories of uncertainty, with a skew towards the highest quartile. This stimuli design meant that, while participants had at least one "safe" square (low danger with high certainty), they were forced to make at least some guesses in other quartiles.

We selected this task in order to promote risk-averse behavior. Tversky & Kahneman [41] illustrate that framings in terms of gains or losses produce reliably different outcomes. In particular, there is greater perceived value in avoiding large losses as opposed to striving for a large gain [21].

The ideal strategy from a value-maximizing standpoint would be to place tokens on areas with the highest expected value (lowest danger), ignoring the uncertainty information. However, as with roulette and other similar games of chance, the *variability* in expected value is relevant when considering where to place bets [25]. A risky player would choose guesses with high expected value, regardless of the uncertainty of those points. A more conservative guesser might eschew high-risk, high-reward locations, resulting in a lower average value of guesses, but also lower uncertainty. We therefore measured the distribution of both *value* and *uncertainty* of the tokens placed by the participants.

We recruited 24 participants for this task: 12 female, 12 male, ($M_{age} = 37$, $SD_{age} = 9.8$). Our results from the prior study indicate that discrete, non-juxtaposed maps outperformed the other bivariate maps we selected, so we limited our study to only 4 types: square and wedge bivariate maps. These in turn were either VSUPs or traditional bivariate maps, for a 2 (square

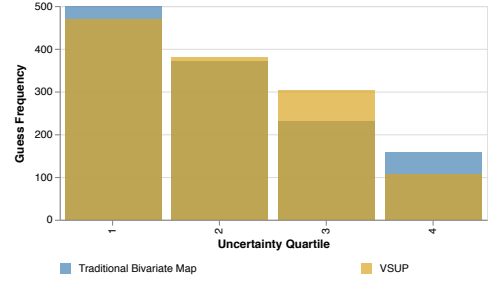


Figure 9: Overlaid histograms of the distribution of uncertainty across all participants' guesses from the prediction experiment. For each trial, participants made 5 guesses. While participants generally favored low uncertainty in guesses, our stimuli design encouraged them to make at least some guesses with higher uncertainty. VSUPs encouraged more guesses with middling uncertainty, and discouraged highly uncertain guesses.

or wedge legend) x 2 (VSUP or standard) factorial design, with 6 replications, for a total of 24 stimuli. Prior to the main task, we included a short replication of the identification task from the prior experiment (with 12 stimuli) for training and exclusion purposes. 3 people with unacceptably low accuracy on the training task (6%, 6%, and 25% accuracy compared to a mean of 70%) were excluded from analysis.

Hypotheses

We had two hypotheses, stemming from our belief that VSUPs promote better *integration* between uncertainty and value information, and encourage *caution* by highlighting the ambiguity introduced by uncertain data. In particular:

1. Participants would avoid targets with **high uncertainty** when using a VSUP.
2. This would result in a tradeoff where they would also choose targets with **lower expected value** when using a VSUP.

As with the prior experiment, we had no strong hypotheses for square vs. wedge-shaped legends, but included both as a check against the potential implicit VSUP-like properties of wedge-shaped legends.

Results

Consistent with our first experiment, we found no significant effect of legend shape on either uncertainty ($F(1, 61) = 0.01$, $p = 0.92$) or value ($F(1, 61) = 3.1$, $p = 0.08$) of guesses. This result suggests that wedge- and square-shaped legends promote similar patterns of decision-making. Overall, we prefer to employ the wedge-shaped legend for VSUPs, and the square-shaped legend for traditional maps, as it makes the conceptual differences between the two more apparent.

The results partially support our first hypothesis. We performed a repeated measures ANOVA on our results to measure the effect of VSUP versus standard quantizations, and square-versus wedge-shaped legends, on average uncertainty in bets. We found no significant effect of quantization scheme on average guess uncertainty ($F(1, 61) = 0.05$, $p = 0.83$). This result

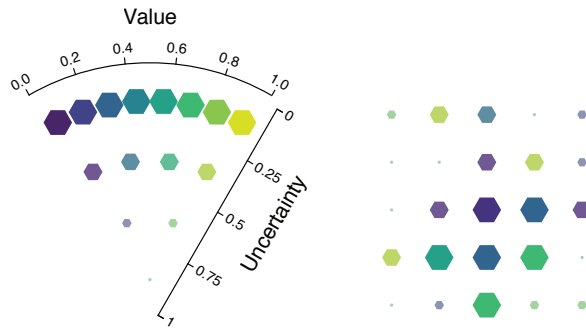


Figure 10: A VSUP where value is mapped to color, and uncertainty is mapped to glyph area. As glyphs become smaller, it becomes more difficult to distinguish their colors [36]. VSUPs, by reducing the number of color categories as uncertainty increases, account for this ambiguity. On the right, the VSUP has been used to encode a 5x5 grid of random data.

indicates that there does not appear to be a uniform pattern of risk aversion between the two scale types. However, given our quartile-based stimuli design, the central tendency of uncertainty would not necessarily capture caution in guesses. To capture differences in this non-normal distribution, and to test our belief that VSUP users would avoid highly uncertain regions, we performed a one-sided two-sample, Kolmogorov-Smirnov test on the distributions of uncertainty in guesses in the VSUP and traditional bivariate conditions. We found a significant difference ($D = 0.5$, $p = 0.03$), and an inspection of the distribution shows that participants using VSUPs were less likely to make guesses with very high uncertainty. Figure 9 shows this result.

The results support our second hypothesis. A similar ANOVA for average danger value of guesses found a significant effect of quantization scheme ($F(1, 59) = 17$, $p < 0.01$). A post-hoc t-test confirmed ($t = 2.3$, $p = 0.02$) that guesses made with VSUPs had significantly higher average danger ($M = 0.32$, $SD = 0.17$) (and so lower expected value) than traditional maps ($M = 0.29$, $SD = 0.18$).

These two results, taken together, suggest that VSUPs led participants to moderate their guesses: avoiding highly uncertain regions, but willing to “gamble” more on regions of middling certainty. In our design, where these gambles were usually poor (due to the predominance of “bad” cells), this moderation resulted in lower expected values. However, when value and uncertainty are orthogonal, this moderation can be beneficial, or at least not harmful. Indeed, for guesses with middling and low uncertainty (quartiles 1-3), where this orthogonality was present, there was no significant difference ($t = 1.56$, $p = 0.11$) in average danger between VSUP ($M = 0.30$, $SD = 0.24$) and traditional ($M = 0.29$, $SD = 0.24$) conditions.

DISCUSSION

The results from our initial evaluation of VSUPs are promising, showing that a general audience can make use of uncertainty information in a reasonable way. The way that uncertainty

information is presented can have a measurable impact on decision-making. The VSUP strategy of only emphasizing differences when uncertainty is sufficiently low is somewhat analogous to the inferential statistics such as effects tests. VSUPs might therefore be used to promote more caution in judgments, and lead analysts away from spurious signals in data.

Bivariate maps have an inherent limitation in that visual channels are often difficult to attend to separately or orthogonally. Bivariate maps are also complex to interpret. Systems which simultaneously display large amounts of value and uncertainty data to general audiences (such as Pangloss [26]) avoid them for precisely these reasons, relying instead on juxtaposed maps. Our results indicate that juxtaposition produces additional problems, forcing users that wish to integrate uncertainty and data to locate an item of interest, and then re-locate that same item in a visually distant map, which may have few visual landmarks in common. This additional step before information fusion is reflected in longer response times, and patterns of decision-making that are less mindful of risk.

Limitations and Future Work

VSUPs assume that uncertain values ought to have less visual impact than highly certain values. VSUPs therefore act both as a kind of filtering device as well as a bivariate representation. This assumption holds in scenarios like the virology dataset (Figure 5), where the expectation is that highly uncertain data is unreliable or should otherwise be downweighted in analysis. If the analyst has a different interpretation of uncertainty, or wishes to quickly and orthogonally analyze the distributions of uncertainty and value, other strategies, such as juxtaposed maps, may be more appropriate. VSUPs are designed for the *integration* of value and uncertainty. Designers should take care in considering when and how this integration is desirable.

Our experiments dealt with cases where both uncertainty and value were represented by color. The perceptual non-separability of color channels is well-known [15, 46], and so the concept of a limited “budget” of distinguishable marks easier to quantify and illustrate. In principle, a VSUP can be created for any combination of visual variables. All that is required is a perceptual model of the interaction between these two variables. Where these models exist, as with the interaction between size and color [36], the creation of VSUPs is straightforward. Where these models do not exist, or where the perceptual interaction is too complex to efficiently model, experimental work remains to be done before VSUPs can be considered a feasible design strategy. We are currently experimenting with the creation of VSUPs using these other channels, as in Figure 10.

VSUPs, like other mappings involving quantization, are also highly sensitive to the binning scheme used. Uncertain data with values that fall very close to bin boundaries may end up having large color differences, even though they may be close in value. The comparison to effects tests is therefore imperfect, and a particular item’s encoding in a VSUP cannot be used as a proxy for a test of statistical significance. As with other quantized forms of data analysis, including histograms and geospatial binning, analysts and designers should consider the distribution of values before quantizing.

Conclusion

Uncertainty, data quality, or confidence values are often considered separately from the data itself, relegated to tooltips or visually distant supplemental charts. We contend, in contrast, that uncertainty information ought to be directly integrated within a shared chart. This integration introduces additional complexity in the design and presentation of data. Value-Suppressing Uncertainty Palettes represent one strategy for dealing with this complexity, by assigning mark properties in a way that supports the disambiguation of values in data where uncertainty is low, but suppresses these judgments when uncertainty is high. This decision of how to allocate visual variables promotes patterns of decision-making that make responsible use of uncertainty information, discouraging comparison of values in unreliable regions of the data, and promoting comparison in regions of high certainty.

REFERENCES

1. Jürgen Bernard, Martin Steiger, Sebastian Mittelstädt, Simon Thum, Daniel Keim, and Jörn Kohlhammer. 2015. A survey and task-based quality assessment of static 2D colormaps. In *SPIE/IS&T Electronic Imaging*. International Society for Optics and Photonics, 93970M–93970M.
2. David Borland and Russell M Taylor II. 2007. Rainbow color map (still) considered harmful. *IEEE computer graphics and applications* 27, 2 (2007).
3. Michael Bostock, Vadim Ogievetsky, and Jeffrey Heer. 2011. D³ data-driven documents. *IEEE transactions on visualization and computer graphics* 17, 12 (2011), 2301–2309.
4. Nadia Boukhelifa, Anastasia Bezerianos, Tobias Isenberg, and Jean-Daniel Fekete. 2012. Evaluating sketchiness as a visual variable for the depiction of qualitative uncertainty. *IEEE Transactions on Visualization and Computer Graphics* 18, 12 (2012), 2769–2778.
5. Nadia Boukhelifa and David John Duke. 2009. Uncertainty visualization: why might it fail?. In *CHI'09 Extended Abstracts on Human Factors in Computing Systems*. ACM, 4051–4056.
6. Ken Brodlie, Rodolfo Allendes Osorio, and Adriano Lopes. 2012. A review of uncertainty in data visualization. In *Expanding the frontiers of visual analytics and visualization*. Springer, 81–109.
7. Barbara Buttenfield and M Kate Beard. 1994. Graphical and geographical components of data quality. *Visualization in geographic information systems* (1994), 150–157.
8. Michael Correll, Adam L Bailey, Alper Sarikaya, David H O'Connor, and Michael Gleicher. 2015. LayerCake: a tool for the visual comparison of viral deep sequencing data. *Bioinformatics* (2015), btv407.
9. Michael Correll, Subhadip Ghosh, David O'Connor, and Michael Gleicher. 2011. Visualizing virus population variability from next generation sequencing data. In *Biological Data Visualization (BioVis), 2011 IEEE Symposium on*. IEEE, 135–142.
10. M Correll and Michael Gleicher. 2013. Error bars considered harmful. *IEEE Visualization Poster Proceedings. IEEE* (2013).
11. Michael Correll and Jeffrey Heer. 2017. Surprise! Bayesian Weighting for De-Biasing Thematic Maps. *IEEE Transactions on Visualization and Computer Graphics* 23, 1 (2017), 651–660.
12. Jonathan Cox, Donald House, and Michael Lindell. 2013. Visualizing uncertainty in predicted hurricane tracks. *International Journal for Uncertainty Quantification* 3, 2 (2013).
13. Michael W Dobson. 1973. Choropleth maps without class intervals?: a comment. *Geographical Analysis* 5, 4 (1973), 358–360.
14. Richard Dunn. 1989. A dynamic approach to two-variable color mapping. *The American Statistician* 43, 4 (1989), 245–252.
15. W. R. Garner and G. L. Felfoldy. 1970. Integrality of stimulus dimensions in various types of information processing. *Cognitive Psychology* 1, 3 (1970), 225–241.
16. Miriam Greis, Passant El Agroudy, Hendrik Schuff, Tonja Machulla, and Albrecht Schmidt. 2016. Decision-Making under Uncertainty: How the Amount of Presented Uncertainty Influences User Behavior. In *Proceedings of the 9th Nordic Conference on Human-Computer Interaction*. ACM, 52.
17. Henning Griethe, Heidrun Schumann, and others. 2006. The visualization of uncertain data: Methods and problems.. In *SimVis*. 143–156.
18. LeGrand H Hardy, Gertrude Rand, and M Catherine Rittler. 1945. Tests for the detection and analysis of color-blindness. I. The Ishihara test: an evaluation. *JOSA* 35, 4 (1945), 268–275.
19. Mark Harrower and Cynthia A Brewer. 2003. ColorBrewer. org: an online tool for selecting colour schemes for maps. *The Cartographic Journal* 40, 1 (2003), 27–37.
20. Jessica Hullman, Paul Resnick, and Eytan Adar. 2015. Hypothetical outcome plots outperform error bars and violin plots for inferences about reliability of variable ordering. *PloS one* 10, 11 (2015), e0142444.
21. Daniel Kahneman and Amos Tversky. 1979. Prospect theory: An analysis of decision under risk. *Econometrica: Journal of the econometric society* (1979), 263–291.
22. Lydia R Lucchesi and Christopher K Wikle. 2017. Visualizing uncertainty in areal data with bivariate choropleth maps, map pixelation and glyph rotation. *Stat* (2017).
23. Alan M MacEachren, Robert E Roth, James O'Brien, Bonan Li, Derek Swingley, and Mark Gahegan. 2012. Visual semiotics & uncertainty visualization: An empirical study. *IEEE Transactions on Visualization and Computer Graphics* 18, 12 (2012), 2496–2505.

24. Carter A Mandrik and Yeqing Bao. 2005. Exploring the concept and measurement of general risk aversion. *NA-Advances in Consumer Research Volume 32* (2005).
25. Leonard Mlodinow. 2009. *The drunkard's walk: How randomness rules our lives*. Vintage. 81–104 pages.
26. Dominik Moritz, Danyel Fisher, Bolin Ding, and Chi Wang. 2017. Trust, but Verify: Optimistic Visualizations of Approximate Queries for Exploring Big Data. In *ACM Human Factors in Computing Systems (CHI)*. <http://idl.cs.washington.edu/papers/trust-but-verify>
27. Jean-Claude Muller. 1979. Perception of Continuously Shaded Maps. *Annals of the Association of American Geographers* 69, 2 (1979), 240–249.
28. Shelby L O'Connor, Ericka A Becker, Jason T Weinfurter, Emily N Chin, Melisa L Budde, Emma Gostick, Michael Correll, Michael Gleicher, Austin L Hughes, David A Price, and others. 2012. Conditional CD8+ T cell escape during acute simian immunodeficiency virus infection. *Journal of virology* 86, 1 (2012), 605–609.
29. Bureau of Transportation Statistics. 2016. Airline Delays, Cancellations and Tarmac Times. (2016). http://www.rita.dot.gov/bts/data_and_statistics/by_mode/airline_and_airports/airline_delay.html
30. Lace Padilla, P Samuel Quinan, Miriah Meyer, and Sarah H Creem-Regehr. 2017. Evaluating the Impact of Binning 2D Scalar Fields. *IEEE Transactions on Visualization and Computer Graphics* 23, 1 (2017), 431–440.
31. Maria Riveiro. 2007. Evaluation of uncertainty visualization techniques for information fusion. In *Information Fusion, 2007 10th International Conference on*. IEEE, 1–8.
32. Philip K Robertson and John F O'Callaghan. 1986. The generation of color sequences for univariate and bivariate mapping. *IEEE Computer Graphics and Applications* 6, 2 (1986), 24–32.
33. Bernice E Rogowitz and Alan D Kalvin. 2001. The "Which Blair Project": a quick visual method for evaluating perceptual color maps. In *Visualization, 2001. VIS'01. Proceedings*. IEEE, 183–556.
34. Bernice E Rogowitz, Lloyd A Treinish, Steve Bryson, and others. 1996. How not to lie with visualization. *Computers in Physics* 10, 3 (1996), 268–273.
35. Robert E Roth, Andrew W Woodruff, and Zachary F Johnson. 2010. Value-by-alpha maps: An alternative technique to the cartogram. *The Cartographic Journal* 47, 2 (2010), 130–140.
36. Maureen Stone, Danielle Albers Szafir, and Vidya Setlur. 2014. An engineering model for color difference as a function of size. In *Color and Imaging Conference*, Vol. 2014. Society for Imaging Science and Technology, 253–258.
37. Nassim Nicholas Taleb and Mark Blyth. 2011. The black swan of Cairo: How suppressing volatility makes the world less predictable and more dangerous. *Foreign Affairs* (2011), 33–39.
38. Judi Thomson, Elizabeth Hetzler, Alan MacEachren, Mark Gahegan, and Misha Pavel. 2005. A typology for visualizing uncertainty. In *Electronic Imaging 2005*. International Society for Optics and Photonics, 146–157.
39. Bruce E Trumbo. 1981. A theory for coloring bivariate statistical maps. *The American Statistician* 35, 4 (1981), 220–226.
40. Archie Tse. 2016. Why We Are Doing Fewer Interactives. (2016). <https://github.com/archietse/malofiej-2016/blob/master/tse-malofiej-2016-slides.pdf> Malofiej.
41. Amos Tversky and Daniel Kahneman. 1985. The framing of decisions and the psychology of choice. In *Environmental Impact Assessment, Technology Assessment, and Risk Analysis*. Springer, 107–129.
42. StÅlfan van der Walt and Nathaniel Smith. 2015. mpl colormaps. <https://bids.github.io/colormap/>, (2015).
43. Howard Wainer and Carl M Francolini. 1980. An Empirical Inquiry Concerning Human Understanding of Two-Variable Color Maps. *American Statistician* (1980), 81–93.
44. Colin Ware. 1988. Color sequences for univariate maps: Theory, experiments and principles. *IEEE Computer Graphics and Applications* 8, 5 (1988), 41–49.
45. Colin Ware. 2009. Quantitative texton sequences for legible bivariate maps. *IEEE Transactions on Visualization and Computer Graphics* 15, 6 (2009).
46. Colin Ware. 2012. *Information visualization: perception for design*. Elsevier.