# Object projected from a horizontal surface

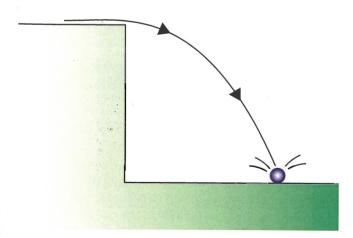
Special considerations:

- Initial vertical velocity = 0
- $\theta = 0^{\circ}$

### **QUESTIONS**

For each of the problems below, consider a projectile dropped vertically out of a moving object such as a plane, thrown horizontally out from the top of a cliff, or fired horizontally and landing on a surface as shown in the diagram. For each find any of the quantities which are not in the given data (not necessarily in the order given).

- (a) The initial velocity of the projectile.
- (b) Its initial horizontal velocity.
- (c) Its initial vertical velocity.
- (d) Its range.
- (e) Its final horizontal velocity.
- (f) Its final vertical velocity.
- (g) Its final velocity.
- (h) The time taken to fall.
- (i) The height from which it was thrown or dropped.
- (j) Its velocity 3 seconds after dropping.
- (k) Its height 5 seconds after dropping.



- 1. A lifeboat is dropped from a plane moving at 140 m s<sup>-1</sup> from a height of 1102.5 m.
- 2. A box of supplies is dropped from a helicopter moving at 80 m s<sup>-1</sup>. They hit the ground 9.0 s later.

- 3. A ball is thrown horizontally from the top of a building and lands in a bucket on the ground 50 m in front of the building 3.0 s later.
- 4. A rock is thrown horizontally out from the top of a 147 m cliff. It hits the ground 80 m from the base of the cliff.
- 5. A ball thrown horizontally out from the top of a cliff hits the ground 6 s later at 30° to the vertical, and moving at 67.9 m s<sup>-1</sup>.
- **6.** A cannonball is fired horizontally from a castle. It hits its target 150 m away after 7.5 s.
- 7. An arrow is fired horizontally at the centre of a target 50 m away. Unfortunately, the archer made no allowance for gravity, and the arrow hit 0.8 m below centre.
- 8. A cannon fires a ball at 150 m s<sup>-1</sup> which hits its target 675 m away.
- 9. A lifeboat is dropped from a plane moving at 80 km h<sup>-1</sup>. It lands in the water 8 s later.
- 10. A projectile hits the centre of a target at an angle of 15° to the vertical 15 s after being dropped from a helicopter.

#### Now answer these questions

- 11. A car, moving at 30 m s<sup>-1</sup>, goes over the edge of a cliff and into the water 58.8 m below.
  - (a) Calculate the time it takes the car to hit the water.
  - (b) Calculate the distance from the cliff that the car hits the water.
  - (c) Calculate the speed of the car just as it hits the water.
- 12. A group of lemmings run over the edge of a 200 m cliff at  $0.6 \text{ m s}^{-1}$ .
  - (a) Calculate their time to fall to the bottom of the cliff.
  - (b) Calculate their velocity halfway down.
  - (c) Calculate the time their speed will be  $30.0 \text{ m s}^{-1}$ .
  - (d) Calculate the speed at which they hit the ground.

- 4. (a) From  $F_{\text{parallel}} = mg \sin \theta = 6 \times 9.8 \times \sin 35^{\circ} = 33.73 \text{ N}$ 
  - (b) From  $F_N = mg \cos \theta = 6 \times 9.8 \times \cos 35^\circ = 48.2 \text{ N up, perpendicular to the surface}$
  - (c) From F = ma, net force =  $6 \times 3.4 = 20.4$  N down the incline
  - (d) From net force = parallel component friction, 20.4 = 33.73 friction, so friction = 13.33 N up the slope
- (a) From  $F_{\text{parallel}} = mg \sin \theta = 200 \times 9.8 \times \sin 35^{\circ} = 1124.2 \text{ N}$ 
  - (b) From  $F_N = mg \cos \theta = 200 \times 9.8 \times \cos 35^\circ = 1605.5 \text{ N up, perpendicular to the surface}$
- 6. From  $F = ma = 735 \times 0.15 = 110.25 \text{ N}$  up the slope (a)
  - (b) Tension = friction + net force = 510.25 N both ways in the rope
  - (c) From  $F_N = mg \cos \theta = 735 \times 9.8 \times \cos 15^\circ = 6957.6 \text{ N up at } 90^\circ \text{ to the surface}$
- 7. (a) From  $F = ma = 73 \times 0.75 = 54.75$  N down the slope
  - (b) From  $F_{\text{parallel}} = mg \sin \theta = 73 \times 9.8 \times \sin 12^{\circ} = 148.74 \text{ N}$
  - Net force = component down the slope friction = 54.75 = 148.75 friction, so friction = 94 N up the slope (c)
- From  $F = ma = 5000 \times 0 = \text{zero (constant velocity)}$ 8. (a)
  - (b) From  $F_{\text{parallel}} = mg \sin \theta = 5000 \times 9.8 \times \sin 7.5^{\circ} = 6395.8 \text{ N}$
  - (c) 6395.8 up the slope
  - (d) Slow down, stop momentarily and then accelerate down the incline, all at  $1.28 \text{ m s}^{-2}$
- (a) From  $F_{\text{parallel}} = mg \sin \theta = 40 \times 9.8 \times \sin 37^{\circ} = 235.9 \text{ N}$  down the slope (b) From  $F = ma = 40 \times 0.6 = 24 \text{ N}$  up the slope

  - (c) Tension = net force + component down slope = 24 + 235.9 = 259.9 N (acting both ways)
  - (d) If acceleration is the same, the net force acting will be the same = 32 N up the slope
  - Tension in the rope will also include 5.0 N to overcome friction, so, tension = 331.3 + 32 + 5 = 368.3 N (e)
- 10. (a) From  $F = ma = 80 \times 0.4 = 32$  N up the slope
  - (b) From  $F_{\text{parallel}} = mg \sin \theta = 80 \times 9.8 \times \sin 25^{\circ} = 331.3 \text{ N down the slope}$
  - Total force to move block up slope = component down + net = 331.3 + 32 = 363.3 N But rope is inclined at  $20^{\circ}$ , so tension in rope = total force/cos  $20^{\circ}$  = 386.6 N acting both ways

#### 11 Projectile Motion

1. For projectile at 30° to horizontal:

 $u_{\rm s} = 40 \sin 30^{\circ} = 20 \text{ m s}^{-1}$ 

From  $v_{top} = 0 = u_v + gt = 34.641 - 9.8t$ 

Time to rise = 2.0408 s

So, time of flight = 4.0816 s

Therefore range, =  $u_x \times t_{flight} = 40 \cos 30^{\circ} \times 4.0816 = 141.39 \text{ m}$ 

For projectile at 60° to horizontal:

 $u_{\cdot \cdot} = 40 \sin 60^{\circ} = 34.641 \text{ m s}^{-1}$ 

From  $v_{top} = 0 = u_x + gt = 34.641 - 9.8t$ 

Time to rise = 3.5347 s

So, time of flight = 7.0796 s

Therefore range, =  $u_x \times t_{flight} = 40 \cos 30^{\circ} \times 7.0696 = 141.39 \text{ m}$ 

Therefore, on the basis of this one calculation, Galileo's prediction is supported.

## 12 Projectile Motion Problems 1

All answers in order of information requested in the chapter (answers may differ slightly due to rounding errors).

- 140 m s<sup>-1</sup>, 140 m s<sup>-1</sup>, 0, 2100 m, 140 m s<sup>-1</sup>, 147 m s<sup>-1</sup>, 203 m s<sup>-1</sup> at 46.4° to horizontal, 15 s, 1102.5 m,  $143.1 \text{ m s}^{-1}$  at  $11.9^{\circ}$  to horizontal, 980 m
- $80~m~s^{-1}$ ,  $80~m~s^{-1}$ , 0, 720~m,  $80~m~s^{-1}$ ,  $88.2~m~s^{-1}$ ,  $119.1~m~s^{-1}$  at  $47.8^{\circ}$  to horizontal, 9~s, 396.9~m, 85.2 m s<sup>-1</sup> at 20.2° to horizontal, 274.4 m
- 3.  $16.7 \text{ m s}^{-1}$ ,  $16.7 \text{ m s}^{-1}$ , 0, 50 m,  $16.7 \text{ m s}^{-1}$ , 29.4 m s $^{-1}$ , 33.8 m s $^{-1}$  at 60.4° to horizontal, 3 s, 44.1 m, 33.8 m s<sup>-1</sup> at 60.4° to horizontal, 0 m
- 4.  $14.6 \text{ m s}^{-1}$ ,  $14.6 \text{ m s}^{-1}$ , 0, 80 m,  $14.6 \text{ m s}^{-1}$ ,  $53.6 \text{ m s}^{-1}$ ,  $55.6 \text{ m s}^{-1}$  at  $74.8^{\circ}$  to horizontal, 5.5 s, 147 m,  $32.8 \text{ m s}^{-1}$  at  $63.6^{\circ}$  to horizontal, 24.5 m
- 5.  $33.95 \text{ m s}^{-1}$ ,  $33.95 \text{ m s}^{-1}$ , 0, 203.7 m,  $33.95 \text{ m s}^{-1}$ ,  $58.8 \text{ m s}^{-1}$ ,  $67.9 \text{ m s}^{-1}$  at  $60^{\circ}$  to horizontal, 6.0 s,  $176.4~m,\,44.9~m~s^{\text{--}1}$  at  $40.9^{\circ}$  to horizontal, 53.9~m
- 6.  $20 \text{ m s}^{-1}$ ,  $20 \text{ m s}^{-1}$ , 0, 150 m,  $20 \text{ m s}^{-1}$ ,  $73.5 \text{ m s}^{-1}$ ,  $76.2 \text{ m s}^{-1}$  at  $74.8^{\circ}$  to horizontal, 7.5 s, 275.6 m,  $35.6 \text{ m s}^{-1}$  at  $55.8^{\circ}$  to horizontal, 153.1 m
- $125~m~s^{-1},\,125~m~s^{-1},\,0,\,50~m,\,125~m~s^{-1},\,3.92~m~s^{-1},\,125.1~m~s^{-1}~at~1.8^{\circ}~to~horizontal,\,0.4~s,\,0.8~m,\,0,\,0~m$
- 8.  $150 \text{ m s}^{-1}$ ,  $150 \text{ m s}^{-1}$ , 0, 675 m, 150 m s $^{-1}$ , 44.1 m s $^{-1}$ , 156.3 m s $^{-1}$  at 16.4° to horizontal, 4.5 s, 99.2 m, 152.9 m s $^{-1}$  at 11.1° to horizontal, 0 m
- $22.2~m~s^{-1},\,22.2~m~s^{-1},\,0,\,177.8~m,\,22.2~m~s^{-1},\,78.4~m~s^{-1},\,81.5~m~s^{-1}~at~74.2^{\circ}~to~horizontal,\,8~s,\,313.6~m,\,$  $36.8~m~s^{-1}$  at  $52.9^{\circ}$  to horizontal, 191.1~m
- $10.\ 39.4\ m\ s^{-1},\ 39.4\ m\ s^{-1},\ 0,\ 590.8\ m,\ 39.4\ m\ s^{-1},\ 147\ m\ s^{-1};\ 152.2\ m\ s^{-1}\ at\ 75^{\circ}\ to\ horizontal,\ 15\ s,\ 1102.5\ m,\ 49.2\ m\ s^{-1}\ at\ 36.7^{\circ}\ to\ horizontal,\ 980\ m$ 11. (a) 3.46 s
  - - (b) 103.9 m
    - (c)  $45.3 \text{ m s}^{-1}$
- 12. (a) 6.4 s
  - (b) 44.3 m s<sup>-1</sup> at 89.2° down from horizontal
  - (c) 3.06 s
  - (d) 62.72 m s<sup>-1</sup> at 89.5° (If you forgot to take the initial horizontal component into account your answer will be 62.610.)