Kinetic energy backscatter (KEB) parameterizations for NEMO: documentation

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Abstract

This document describes the code of KEB parameterizations developed by the author for NEMO ocean model Perezhogin [2020]. Compared to publication, code was significantly refactored, adopted to curvilinear coordinates and partially tested in NNATL12 configuration.

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1 Fast start

1.1 Install NEMO

• Let you have installed libraries nectdf4, hdf5, zlib and xios2, and they are in system PATH. Download NEMO 3.6:

```
svn co http://forge.ipsl.jussieu.fr/nemo/svn/NEMO/releases/release-3.6/NEMOGCM
```

• Go to folder ARCH and create file arch-myarch.fcm similar to ones presented in this folder, where set compilers (like mpiifort) and directly set path to mentioned libraries, for example:

```
%NCDF_INC -I/netcdf4/include
%NCDF_LIB -L/netcdf4/lib64 -L/hdf5/lib64 -lnetcdf -lnetcdff -lhdf5 -lhdf5_hl -lz
%XIOS_INC -I/xios-2.0/inc
%XIOS_LIB -L/xios-2.0/lib -lxios
```

• Compile clean GYRE configuration in folder GYRE_XIOS, i.e. in folder CONFIG execute:

```
./makenemo -m myarch -r GYRE_XIOS -n GYRE_XIOS -j 8
```

1.2 Import KEB library

- Copy folder GYRE_KEB from this repository to folder CONFIG.
- Compile with command:

```
./makenemo -m myarch -r GYRE_XIOS -n GYRE_KEB -j 8
```

• In folder GYRE_KEB there are three experiments:

```
/EXP_bare - configuration without backscatter
/EXP_AR1 - autoregressive stochastic KEB
/EXP_negvisc - negative viscosity KEB
```

• You need to make link to executable file:

```
ln -s /direct/path/to/GYRE_KEB/BLD/bin/nemo.exe EXP_bare/opa
ln -s /direct/path/to/GYRE_KEB/BLD/bin/nemo.exe EXP_AR1/opa
ln -s /direct/path/to/GYRE_KEB/BLD/bin/nemo.exe EXP_negvisc/opa
```

• Each experiment can be executed with

```
mpirun -n 32 ./opa
```

This takes approximately 2 hours. Experiments are launched for 30 years at resolution R4 from snapshot of R9 model in statistical equilibrium.

1.3 Check results

- There are 5d files and time series just to look at with ncview.
- If you follow instruction, results are saved as single netcdf files. Copy content of folder plot_figures from this repository to each experiment folder. Run Python script:

```
python processing.py
```

This gives result.pdf with figures which should be compared to figures in Perezhogin [2020]. Scripts

```
processing_AR1.py, processing_negvisc.py
```

being applied to respective experiments will give KEB statistics. Examples of these figures together with paper Perezhogin [2020] are given in this repository in folder materials.

Troubleshooting

I suppose you have python 3 installed. Most likely, you will need to load additional modules using command (no need for root):

```
python -m pip install netCDF4 --user
python -m pip install matplotlib --user
python -m pip install numpy --user
```

Possibly, some libraries else... see error if it exists.

2 Code overview

- KEB parameterizations consume no more than 15% of runtime, see figure 1. Additionally 10% may be consumed by routine collecting statistics KEB_statistics(), depending on how many fields defined in file_def.xml.
- Energy dissipation is collected in dynldf_bilap.F90 and then processed in module KEB_module.F90. Main routines of this module are shown in orange and main variables in green, see figure 2.

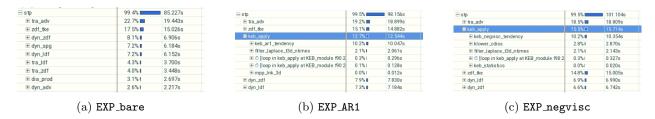


Figure 1: Model runtime according to Intel Advisor for 500 steps on 1 core.

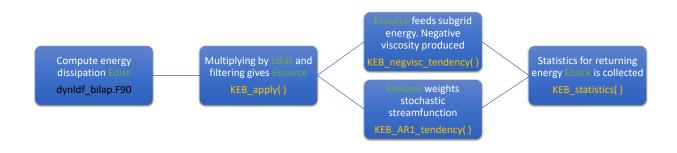


Figure 2: How KEB library works.

3 Modifications of clean NEMO code

Already existing files were modified. You can see them by checking difference between commits Clean NEMO and Modifications of clean NEMO. Click here.

Main modifications:

- ullet nemogcm.F90 $-\operatorname{run}$ KEB_init
- step.F90 run KEB_apply and KEB_rst
- dynldf_bilap.F90 compute Ediss

To reproduce my experiments (KEB can be compiled without these modifications):

- istate.F90 start from R9 snapshot
- diaprod.F90, diawri.F90 statistics
- dom_oce.F90 fix integer4 sec counter
- iom.F90, iodef.xml, field_def.xml fix scalars in xios

KEB library:

- KEB_module.F90 routines KEB_init, KEB_rst, KEB_apply
- KEB_operators.F90 all spatial operators
- KEB_testing.F90 test operators

4 KEB namelist

Code behaviour is set in namelist_cfg:

```
_____
&KEB_prms ! parameters of backscatter parameterization
KEB_on
          = .true.
                                ! turn on backscatter
KEB\_test
          = .false.
                                ! turn on testing KEB operators
! Ediss parameters
constant_cdiss = .true.
                                ! true = constant cdiss, false = cdiss varies
c_diss
              = 0.8
                                ! constant backscatter rate
             = 0.5
R_diss
                               ! non-constant backscatter rate, from Klower formula
                               ! number of filters for Ediss
ndiss
             = 2
dirichlet_filter = .false.
                               ! True: zero Dirichlet, false: zero Neumann for Ediss
! negative viscosity KEB parameters
KEB_negvisc
             = .false.
                               ! turn on negative viscosity KEB
tke_adv
              = .true.
                               ! turn on advection of TKE
tke_diff
                               ! turn on diffusion of TKE
              = .true.
                               ! True: zero Dirichlet, false: zero Neumann for TKE
dirichlet_TKE = .true.
             = 300.
                               ! diffusivity of subgrid TKE, m2/s
nu_TKE
              = .false.
tke_filter
                               ! filtering TKE in z direction (for numerical stabil.)
                                ! negative viscosity ~ c_back * sqrt(TKE)
c_back
              = 0.1
                                ! number of filters for negvisc. tendency.
nback
! stochastic KEB parameters
        = .true.
KEB_AR1
                                ! turn on autoregressive in time KEB
                                ! number of filters for stochastic streamfunction
nstoch
                                ! decorrelation time in sec, for AR1
T_decorr
          = 86400.
```

KEB_on turns on backscatter, KEB_test is described in appendix A.

4.1 Ediss parameters

Block Ediss parameters describes how Esource is computed. General formula:

```
Esource = filter(local_cdiss * Ediss)
```

Filter is applied ndiss times. Its boundary conditions set by dirichlet_filter.

If constant_cdiss = .true., then

```
local_cdiss = c_diss
```

otherwise Klower formula Klöwer et al. [2018] is used:

```
local_cdiss = 1 / (1+R_local/R_diss)
```

where R_local - local deformation rate scaled by Coriolis parameter (see Klower_cdiss() in KEB_operators.F90).

4.2 stochastic KEB parameters

Only number of filters for stochastic field nstoch and decorrelation time T_decorr are specified. General formula for stochastic streamfunction:

$$psi(i, j, k) \sim filter(phi(i, j)\sqrt{Esource(i, j, k)})$$
 (1)

where phi(i, j) – Gaussian white noise. Exact equality (1) treated similarly to dissertation O'Neill [2016]. After that time correlation introduced which does not change variance Schumann [1995]:

Aposteriori correction averages energy input from stochastic streamfunction Estoch and compares it to desired energy input Esource. Correction of amplitude:

```
amp_increase = Esource_mean / Estoch_mean
```

Parameters of averaging are hardcoded. In aposteriori_correction() in KEB_operators.F90 time window set to 30 days, initial values of Esource_mean and Estoch_mean set to 1e-9 (typical values) in KEB_module.F90. Min-max values of amp_increase are bounded by $\sqrt{2}$ and $1/\sqrt{2}$.

4.3 negative viscosity KEB parameters

Parameters tke_adv, tke_diff, dirichlet_TKE, nu_TKE set advection-diffusion of subgrid energy TKE, nback sets number of filters for momentum tendency (analogous to Juricke et al. [2020]). Negative viscosity is controlled by c_back as:

```
nu2t = sqrt(2) * c_back * sqrt(e12t * max(TKE,0))
```

Equation for subgrid energy reads:

```
TKE = TKE + (rhs_adv + rhs_diff + Esource - Eback) * rdt
```

Finally, tke_filter is vertical diffusion. Use only if you face with numerical stability issues of advection.

5 Backscatter parameters and interpretation of results

5.1 General comments

• How to set backscatter ratio cdiss?

Estimate resolved energy in model with twice finer resolution and increase cdiss until this level will be reached in coarse model. In case of Klower formula and dirichlet B.C. for filters, resulting backscatter ratio is unclear a priori and can be found in avr_cdiss in output time series. If there is no additional dissipation in the model (i.e. conservative numerical schemes and no isopycnal diffusion/Gent-McWilliams), acceptable values lie in interval (0.7, 0.8). Otherwise, I suppose, cdiss=1 will be ok.

- What dissipative operators supported?
 In this code only biharmonic viscosity. Although, in NNATL12 I produced similar code for biharmonic Smagorinsky. Some estimates of dissipation are already contained in the clean NEMO code under flags like dispkexyfo.
- Can this code be launched with isopycnal diffusion? Yes, results in model R4 are even better (in North latitudes), and less restrictions on backscatter ratio cdiss.
- With Gent-Mcwilliams?

 I am not sure, although Jansen et al. [2019] do it, but with some modifications of subgrid energy equation.
- In some parts of the ocean, eddies are fully resolved, on the others they are fully underresolved. Where to turn off backscatter?

 Jansen et al. [2019] suggests to turn off backscatter if eddies are resolved. Also there is a belief that backscatter should amplify existing eddy filaments, so it should be turned off for underresolved simulations. In my experience, backscatter returns energy in energy-containing scale for any resolution Perezhogin and Glazunov [2021]. However, as a starting point it is reasonable to turn on backscatter only for midlatitudes (multiply local_cdiss by some latitude function).

5.2 negvisc parameterization

- What default parameters correspond to?

 They are as close as possible to Juricke et al. [2020], but with advection of subgrid energy.
- How well model simulates subgrid energy?

 There is an estimate of subgrid energy for barotropic fluid Perezhogin and Glazunov [2021]:

$$tke_est = \frac{\Delta^2}{48}(|D|^2 + \omega^2), \tag{2}$$

where |D| – deformation rate, ω – vorticity, Δ – filter width of the coarse model. You can compare simulated tke and estimation (tke_est) in output files. They are different in spatial distribution, spatial scale and may be different in amount of 10 times (see time series). An amount of tke in statistical equilibrium is mainly controlled by parameter c_back. Changing it in range from c_back = 0.4 Jansen et al. [2015] to c_back=0.1 Juricke et al. [2020] leads to an increase of tke in 10 times. Also I found that in decaying turbulence an optimal value of this parameter is significantly resolution-dependent.

• Should we optimize simulation of subgrid energy?

My beliefe is that its amount does not matter. However, its amount increases together with subgrid energy live time, and it again can range from 2 days for c_back = 0.4 to 60 days for c_back=0.1. Live time is estimated as:

tke_time = TKE / Eback

and can be seen in output.

• Do we know subgrid energy live time?

We know that subgrid energy can be generated elsewhere in the basin and be returned in intergyre jet Grooms et al. [2013]. This should take several months. Usually we can optimize either live time of subgrid energy, either its amount, but not both. My belief is that live time is more important.

- Finally, how to set c_back?
 - Use reference values and check energy live time in output (tke_time). If it is about 2 days, energy returned at the same location where it is dissipated. If 60 days, it can spread over the basin.
- How to choose model for subgrid energy, tke_adv?

 Often it is argued that we do not know model for subgrid energy and its advection is omitted. However, we know that subgrid closure must be galilean invariant, and advection guarantees it. Galilean not-invarianse means that energy will be returned behind the mesoscale eddy path. If subgrid energy live

invarianse means that energy will be returned behind the mesoscale eddy path. If subgrid energy live time about 2 days, advection does not matter, if 60 days it matters. Especially, for large live time mean Eback is located downstream of the intergyre jet, while Ediss is located near the boundary (see materials/EXP_negvisc/result_KEB.pdf).

• How to choose model for subgrid energy, nu_TKE?

I suggest to set TKE diffusivity same as average diffusion coefficient for active tracers. An importance of this parameter mostly depends on subgrid energy live time.

• How to choose B.C. for filter (dirichlet_filter) and for TKE (dirichlet_TKE)? In Perezhogin [2020] both B.C. are Neumann, in Juricke et al. [2020] both are Dirichlet (private communication).

Pros of Neumann B.C.:

An amount of backscattered energy is directly controlled by c_diss.

Cons of Neumann B.C.:

Subgrid energy accumulates near boundaries, where most dissipation occurs. This accumulation is unphysical (as compared to tke_est).

- Does Klower formula for c_diss prevent from accumulation of subgrid energy near the boundary? In my experience no. Dirichlet B.C. much more efficient.
- How to choose number of filters for negvisc tendency, nback?
 Following Juricke, I suggest to use this parameter mainly to prevent numerical instabilities. Improvement of the physics of backscatter with this parameter for me is unclear.
- Can subgrid energy be negative?
 - In this library Eback and Ediss are positive definite. So, negative values can came only from time integration, non-positivity of advection and so on. You can check tke_min in the output.
- Why not to filter Eback as in Juricke et al. [2020]?

 This filtering leads to negative values of subgrid energy, because sink of subgrid energy spreads to regions where there is not subgrid energy.
- Why negative subgrid energy is bad? It can accumulate in some very unphysical locations. For example, at the second grid layer to the boundary.

5.3 AR1 parameterization

for energy inflow

Some comments above also relevant to stochastic parameterization. Additionally:

- What default parameters correspond to?

 They are as close as possible to Perezhogin [2020], but with correlation in time.
- How to choose decorrelation time, T_decorr?

 This parameter should be used to filter out 1 day time scale where inertial oscillations reside. I recommend to use default value. Larger decorrelation time will lead to significant inaccuracy in formula

$$Eback = T_{-}decorr\langle (\nabla^{\perp}\psi)^{2}\rangle$$
(3)

because time scale of linear operators (like biharmonic viscosity) is smaller.

- How to choose number of filters, nstoch?
 In my experience, eddies arising in turbulent field are of spatial scale of stochastic forcing. So, spatial scale of stochastic forcing should be similar to eddy size (check spatial scale of stochastic forcing in file _psi). Unfortunately, turbulent statistics almost insensitive to nstoch parameter, though turbulent field may look differently. So, I recommend default value.
- Why a posteriori correction is needed? Formula for energy inflow (3) is correct only for dynamical system without any other RHS. Usually, a priori estimate gives insufficient energy inflow.
- When a posteriori correction work? It is hard coded that amplitude can be changed within a range $[1/\sqrt{2}, \sqrt{2}]$. It is easy to make a configuration when this range is insufficient: use long time scale together with small spatial scale.
- How to check that a posteriori correction works well?
 Check in output series increase in amplitude (SKEB_amp) and mean backscatter ratio (avr_cdiss). The last parameter should approach specified value of c_diss.
- Can we use Klower formula for cdiss together with AR1 parameterization?

 It can be done in the library. But I do not recommend. An actual energy inflow from stochastic parameterization can be estimated only when there is sufficiently large number of statistical samples. Klower formula may give locally or in average large values of cdiss which are close to 1. This may lead to significant increase in total energy. And we cannot control it because a posteriori correction itself works on time scale of 30 days.
- Is this parameterization Galilean-invariant?

 No. And most of the stochastic backscatter parameterizations with AR1 process are not galilean-invariant, but in different extent. True invariant parameterization must include advection of stochastic field Schumann [1995]. My parameterization may return energy behind eddy path for large decorrelation time. Thats why I again recommend to use decorrelation time no more than 1 day.
- Why don't to filter only 2d stochastic field?

 Because in this case spatial scale of Esource will dominate in resulting parameterization. This filtering is useless after some time, and we must filter Esource then. So, filtering of 3D field is inevitable.

References

- I. Grooms, L.-P. Nadeau, and K. S. Smith. Mesoscale eddy energy locality in an idealized ocean model. Journal of physical oceanography, 43(9):1911–1923, 2013.
- M. F. Jansen, I. M. Held, A. Adcroft, and R. Hallberg. Energy budget-based backscatter in an eddy permitting primitive equation model. *Ocean Modelling*, 94:15–26, 2015.
- M. F. Jansen, A. Adcroft, S. Khani, and H. Kong. Toward an energetically consistent, resolution aware parameterization of ocean mesoscale eddies. *Journal of Advances in Modeling Earth Systems*, 11(8):2844–2860, 2019.
- S. Juricke, S. Danilov, N. Koldunov, M. Oliver, and D. Sidorenko. Ocean kinetic energy backscatter parametrization on unstructured grids: Impact on global eddy-permitting simulations. *Journal of Advances in Modeling Earth Systems*, 12(1):e2019MS001855, 2020.
- M. Klöwer, M. F. Jansen, M. Claus, R. J. Greatbatch, and S. Thomsen. Energy budget-based backscatter in a shallow water model of a double gyre basin. *Ocean Modelling*, 132:1–11, 2018.
- J. J. O'Neill. A new stochastic backscatter model for large-eddy simulation of neutral atmospheric flows. PhD thesis, University of Birmingham, 2016.
- P. Perezhogin and A. Glazunov. A priori and a posteriori analysis in large eddy simulation of the two-dimensional decaying turbulence using an explicit filtering approach. rejected JFM:), 2021.
- P. A. Perezhogin. Testing of kinetic energy backscatter parameterizations in the nemo ocean model. Russian Journal of Numerical Analysis and Mathematical Modelling, 35(2):69–82, 2020.
- U. Schumann. Stochastic backscatter of turbulence energy and scalar variance by random subgrid-scale fluxes. Proceedings of the Royal Society of London. Series A: Mathematical and Physical Sciences, 451 (1941):293–318, 1995.

A Appendix. KEB_test

Before first use in new configuration, you must check that all operators works well and there are no numerical noise.

I suggest to check for numerical noise in 5d files with endings _KEB, _surf, _check_noise. Examples of numerical noise in NNATL12 configuration are given in figure 3.

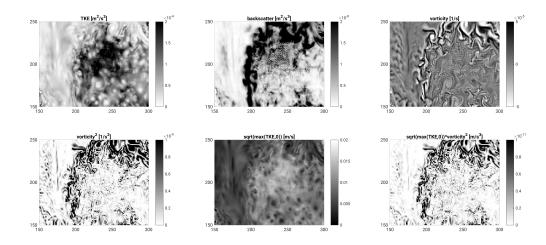


Figure 3: Numerical noise for negvisc KEB in NNATL12.

First, check that all numerics are well. Set KEB_test = .true. For negvisc there should be in ocean.output like:

```
~~~~~~~ KEB negvisc testing ~~~~~~~
! ------! advection ------!
positiveness:
       1.850456085375350E-007 1.864908854464843E-007
min ok:
max ok:
       8.217884550423646E-002 8.073860079089856E-002
conservation:
               (1e-20 ok): -1.589053089423563E-020
no-flux
linear free-surface (1e-8 ok): 1.929998521663570E-008
CFL (<1 ok) = 0.234377548802137
! ------ Eback integration -----!
Eback ok
! ------!
no-flux (1e-20 ok): -1.064180091878790E-021
Dirichlet (1e-4 ok): -1.252268632356181E-004
positiveness:
       1.850456085375350E-007 1.856420384649364E-007
min ok:
```

```
8.217884550423646E-002 8.206124773202066E-002
 ! ------!
 positiveness:
 min ok: 1.850456085375350E-007 1.850865339105703E-007
 max ok: 8.217884550423646E-002 8.066954583786658E-002
 conservation (1e-20 ok): -7.289300561377718E-020
 ! ------! local c_diss ------!
 min value for c_diss (0 ok): 0.220658658338855
 max value for c_diss (1 ok): 0.999355240226306
 ! -----! laplace filter -----!
 filter_laplace_T3D_ntimes, no-flux:
 conservation (1e-20 ok): -9.063963607859050E-022
 min ok: 9.955149248888630E-013 8.190910945193417E-012
 max ok: 1.660738531266926E-006 9.642326610140910E-007
 filter_laplace_T3D_ntimes, Dirichlet:
 conservation (1e-4 ok): 1.169620783571850E-004
 min ok: 9.955149248888630E-013 7.332608706254202E-012
        1.660738531266926E-006 6.331578763746706E-007
 max ok:
 filter_laplace_f3D_ntimes, Dirichlet:
 conservation (1e-4 ok): 1.754927424015464E-004
 min ok: -6.504060701236480E-005 -2.154674296598676E-005
 max ok: 7.392464158314793E-005 2.079623471246499E-005
 ! -----! conservation of momentum for negvisc KEB -----!
 KEB_ldf_lap u trend (1e-20 ok): -3.694647365733425E-020
 \label{eq:KEB_ldf_lap} \mbox{ KEB\_ldf\_lap v trend (1e-20 ok): } -3.575109685101534E-020
 ! ----- conservation of vorticity for negvisc KEB -----!
 KEB_ldf_lap (1e-5 ok): 2.933273928166026E-005
 ! -----!
 KEB_ldf_lap (1e-26 ok): 7.425251269832589E-027
 ! ------! accuracy of Eback estimate
 KEB_1df_1ap, % (1-3\% ok) = 1.73893261182348
 ! ------! accuracy of Ediss estimate
 dynldf_bilap.F90, % (1% ok) = -1.41936718676091
 end of KEB negvisc testing """"
For AR1 there should be like:
  ----- KEB AR1 testing
 ! ---- conservation of momentum for curl of scalar field ----!
 horizontal_curl u trend (1e-20 ok): 2.778398219086012E-019
```

```
horizontal_curl v trend (1e-20 ok): -3.462986254015147E-019
! ------! laplace filter ------!
filter_laplace_T3D_ntimes, no-flux:
conservation (1e-20 ok): -3.544553728101773E-021
       5.139279367434660E-013 8.546036738813375E-012
max ok:
       5.526657690610851E-006 2.128308641583762E-006
filter_laplace_T3D_ntimes, Dirichlet:
conservation (1e-4 ok): 4.496564765648987E-005
       5.139279367434660E-013 6.378930541417978E-012
min ok:
max ok:
       5.526657690610851E-006 2.128308641583762E-006
filter_laplace_f3D_ntimes, Dirichlet:
conservation (1e-4 ok): 1.229041937804671E-004
min ok: -4.327175452894625E-005 -2.043950665604553E-005
max ok: 1.087831942419077E-004 1.811167495622946E-005
! ------! local c_diss -----!
! ------! accuracy of Ediss estimate
dynldf_bilap.F90, % (1% ok) = -1.39592065029580
end of KEB AR1 testing
```

If noise still arise with negvisc:

- Check CFL and positiveness of advection in KEB_test output. Check minimal value of TKE (tke_min in time series). It should not be too negative.
- Does not help? Try vertical filter tke_filter=.true.
- Does not help? Turn off advection tke_adv=.false.
- Does not help? Increase filtering of momentum tendency nback.
- Does not help? Reduce backscatter power by c_diss or R_diss.
- Does not help? Turn off backscatter in problem regions (for example in equatorial waveguide) by multiplying local_cdiss by some latitude function in KEB_module.F90.