

# GATE 2022 BIOMEDICAL ENGINEERING

EE:1205 Signals and systems  
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## I. QUESTION 40

The block diagrams of an ideal system and a real system with their impulse responses are shown below. An auxiliary path is added to the delayed impulse response in the real system.

For a unit impulse input ( $x(t) = \delta(t)$ ) to both systems, gain  $\beta$  is chosen such that  $y(4T)$  is same for both systems. The value of  $\beta$  is:

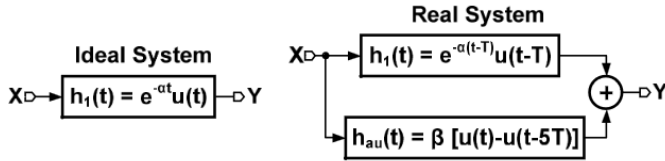
For both signals to be equal at  $t = 4T$ :

$$e^{-\alpha 4T} u(4T) = \left[ \beta (u(4T) - u(-T)) + e^{-\alpha(3T)} u(3T) \right] \quad (3)$$

$$e^{-\alpha 4T} = \beta + e^{-\alpha 3T} \quad (4)$$

$$\Rightarrow \beta = e^{-3\alpha T} (1 - e^{-\alpha T}) \quad (5)$$

Hence the answer is (C)



(A)  $e^{-3\alpha T} (1 - e^{-2\alpha T})$

(B)  $-e^{-\alpha T} (1 - e^{-3\alpha T})$

(C)  $e^{-3\alpha T} (1 - e^{-\alpha T})$

(D)  $e^{-2\alpha T} (1 - e^{-2\alpha T})$

## II. SOLUTION

Let the output of the ideal system be  $y_I$  and output of the real system be  $y_R$

$$y_I = e^{-\alpha t} u(t) \quad (1)$$

$$y_R = \left[ \beta (u(t) - u(t - 5T)) + e^{-\alpha(t-T)} u(t - T) \right] \quad (2)$$

At time  $t = 4T$ , both the signals are equal (for a unit impulse)