

08-10-24

## Algorithm for 8 puzzle using DFS

- \* Considering  $3 \times 3$  {2D} grid  
initialise the problem
- \* Define the initial state of puzzle ( $3 \times 3$  grid)
- \* Define goal state
- \* Randomly arranged list of range [1-8]
- \* Define 1 empty block / space as '0' called tiles

### Step 2: Define the DFS Function

Defining the function of DFS briefly  
inputs :- current state, goal state,  
path, visited.

- \* current state is equal to goal state:  
return path taken to reach goal
- \* Add current state to visited set

- 3) Generating possible moves:-  
find position of blank (0) space &  
generate all possible new states by  
sliding adjacent tiles.

- 4) Iterate through possible moves  
for each next-state generated:  
if next-state has not been visited  
recursively call DFS function with  
next-state, goal state, updated path  
\* if a solution is found (return value is  
not None):  
return that solution

3) Backtrack:

If no solution are found after exploring all tree from current state, remove current state from linked list & back track indicate no solution in this path.

Initial state

2	3	5
7	1	4
0	8	6

Our goal

1	2	3
4	5	6
7	8	0

Solving 8 puzzle using Manhattan Distance

① Initialize the problem

- \* Define the initial state of puzzle ( $3 \times 3$  grid)
- \* Define goal state
- \* Randomly, arrange the list of range (1 to 8)
- \* Define 1 empty block as 0 called tile.

② Defining Heuristic Function :-

Create a Function manhattan(state);

initialize variable distance to 0

for each tile set in state

calculate forget position based on tile value.

Add absolute difference in row & column index to distance and store distance

- \* input :- Current state, goal state, g-cost visited path
  - : if current state is equal to goal state
    - Returns path.

### 3) Generating Possible moves

- \* calculate g-cost as g-cost + 1
- \* calculate heuristic h-cost using manhattan-distance (next-state)
- \* calculate total cost f-cost = g-cost + h-cost

if next state not visited

Add ( $f$ -cost, next-state, updated state) to priority queue

### 4) Process of priority queue

while priority queue not empty  
pop state lowest total cost ( $f(n)$ )

mark it as visited

call the function recursively with state & updated costs

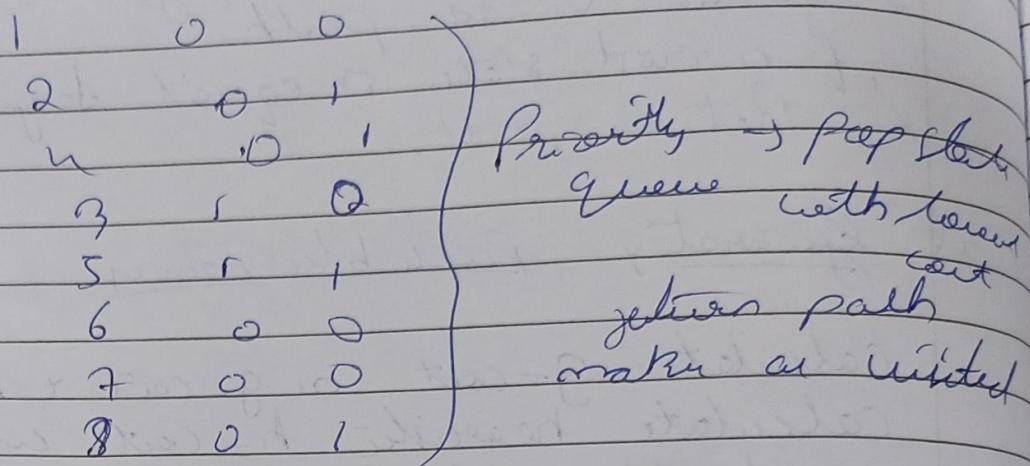
### 5) Backtrack

~~If no solution occurs return to previous position~~

### Initial State

2	0	1	1
5	4	6	
7	8	3	

1	2	3
4	5	6
7	8	0



Code:

```
def DFS_8_Puzzle(initial_state,  
goal_state)
```

```
stack = [initial_state, 0]
```

```
visited = set()
```

```
while stack:
```

```
    current_state, depth = stack.pop()
```

```
    if current_state == goal_state:
```

```
        return goal_state achieved
```

~~```
def find_blank_tile(stack):
```~~~~```
    return stack nodes(0)
```~~~~```
def sweep(state, i, j)
```~~~~```
    new_state = state[:]
```~~~~```
    new_state[i], new_state[j] = merge
```~~~~```
    return new_state;
```~~~~```
def get_neighbours(state)
```~~~~```
    neighbours = []
```~~~~```
    index = find_blank_tile(state)
```~~~~```
    row, col, nodes, ...
```~~

`mover = ((-1, 0), (1, 0), (0, 1), (0, -1))`

in mover:

`new_row, new_col = row + move[0], col + move[1]`

`if 0 <= new_row < 3 and 0 <= new_col < 3`

`new_state = (state, index, new_row, new_col)`

`neighbour = append (new_state)`

`if current_state == goal_state`

`return path + (current_state)`

`if (tuple neighbour) not in visited:`

`stack.append (neighbour, path + [current])`

`if solution != solution:`

`put_puzzle (state)`

`else`

`put (solution)`

Output:

|   |   |   |  |
|---|---|---|--|
| 1 | 3 | 2 |  |
| 4 | 6 | 5 |  |
| 2 | 7 | - |  |

|   |   |   |  |
|---|---|---|--|
| 1 | 2 | 3 |  |
| 4 | 5 | 6 |  |
| 7 | 8 | - |  |



|   |   |   |  |
|---|---|---|--|
| 1 | 3 | 2 |  |
| 4 | 6 | 5 |  |
| 2 | - | 7 |  |



|   |   |   |  |
|---|---|---|--|
| 1 | 3 | 8 |  |
| 4 | - | 5 |  |
| 2 | 6 | 7 |  |

|   |   |   |  |
|---|---|---|--|
| 1 | 3 | 8 |  |
| - | 2 | 5 |  |
| 6 | 2 | 4 |  |

|   |   |   |  |
|---|---|---|--|
| 1 | 2 | 8 |  |
| 3 | 6 | 5 |  |
| 2 | - | - |  |

Manhattan

from collection import deque

$$\text{GOAL-STATE} = [(1, 2, 3), (4, 5, 6), (7, 8, \dots)]$$

$$\text{MOVES} = [(-1, 0), (1, 0), (0, -1), (0, 1)]$$

def manhattan\_distance(state):  
 distance = 0

for i in range(3):

for j in range(3):

if state[i][j] != '-':

goal\_i, goal\_j = divmod(state

[i][j], 3)

$$\text{distance} += \text{abs}(i - \text{goal}_i) + \text{abs}(j - \text{goal}_j)$$

return distance

def get\_neighbour(state):

neighbour = []

for i in range(3):

for j in range(3):

if state[i][j] == '-':

for move in MOVES:

new\_i, new\_j = i + move[0],

j + move[1]

if 0 < new\_i < 3 and 0 < new\_j < 3:

new\_state = [row[:] for row in

state]

new\_state[i][j], new\_state[new\_i][new\_j],

new\_state[new\_i][j] = new\_state[i][j], new\_state[new\_i][new\_j],

new\_state[i][j]

neighbour.append(new\_state)

return neighbors

def dfs(state):

queue = deque([(state, state)])

visited = set()

while queue:

current\_state, path = queue.popleft()

if current\_state == goal\_state (current\_state):

return path

if tuple(map(tuple, current\_state)) in visited:

continue

visited.add(tuple(map(tuple, current\_state)))

for neighbor get\_neighbor(current\_state):

queue.append((neighbor, path + [neighbor]))

return None

initial\_state = [[6, 1, 3],  
[3, 2, 6],  
[5, 8, -1]]

path = dfs(initial\_state)

if path:

print("Solution found: ")

for state in path:

for row in state:

print(row);

print().

else:

print("No solution found")

Output

$$\begin{bmatrix} 1, 2, 3 \\ 4, 5, 6 \\ 7, 8, - \end{bmatrix} \rightarrow \begin{bmatrix} 1, 2, 3 \\ 4, 5, 6 \\ 5, -8 \end{bmatrix} \rightarrow \begin{bmatrix} 4, 1, 3 \\ -2, 6 \\ 7, 5, 8 \end{bmatrix}$$

↓

$$\begin{bmatrix} 1, 2, 3 \\ 4, 5, 6 \\ 7, -8 \end{bmatrix} \leftarrow \begin{bmatrix} 1, -3 \\ 4, 2, 6 \\ 7, 5, 8 \end{bmatrix} \leftarrow \begin{bmatrix} -1, 3 \\ 4, 2, 6 \\ 7, 5, 8 \end{bmatrix}$$

↓

$$\begin{bmatrix} 1, 2, 3 \\ 4, 5, 6 \\ 7, 8, - \end{bmatrix}$$

DFS:

class PuzleState:

def \_\_init\_\_(self, board, zero\_position, move = [ ]):

self.board = board

self.zero\_position = zero\_position

self.move = move

def isGoal(self):

return self.board == [[1, 2, 3], [4, 5, 6], [7, 8, -1]]

def get\_possible\_moves(self):

row, col = self.zero\_position

possible\_moves = []

directions = [(-1, 0), (1, 0), (0, -1), (0, 1)]

for dx, dc in direction:

new row, new col = new - dr,  
col + dc

if 0 < new - row < 3 and 0 < new - col < 3:  
possible\_moves.append((new - row,  
new - col)))

return possible\_moves

def move(self, new\_zero\_position):  
new row, new col = new\_zero\_position  
row, col = self.zero\_position  
new\_board = [x[:] for x in self.  
board[]]

new\_board[new][col], new\_board[new][row]  
[new - row], [new - col])

[new - col] - new\_board[new - row]  
[new - col],  
new\_board[new][col])

return puzzle\_state(new\_board,  
new\_zero\_position, self.moves +  
[(new - row, new - col)])

def dfs(puzzle\_state, visited):

if puzzle\_state == goal:

return puzzle\_state, moves

visited.add(tuple(map(tuple,  
puzzle\_state.board)))

for new\_zero\_position in puzzle\_state:

get\_possible\_moves)

new\_state = puzzle\_state.move(new  
zero\_position)

if tuple(map(tuple, new\_state.  
board))

not in visited:

result = dfs(new\_state, visited).

if result is not None:  
 returns result

return None

def solve\_8\_puzzle (initial\_board):  
 zero\_partition = next ((i, j))  
 for i, row in enumerate (initial  
 board):

for j, val in enumerate (row):  
 if (val == 0)

initial\_state = PuzzleState (initial\_board, zero\_partition)  
 visited = set()

return dfs (initial\_state, visited)

def name == "main":

initial\_board = [[1, 2, 3], [4, 5, 6],  
 [7, 8, 0]]

solution = solve\_8\_puzzle (initial\_board)

if solution is not None:

print ("Solution found!")

else

print ("No sol? Escut.")

Output

|   |               |   |               |   |
|---|---------------|---|---------------|---|
| $\begin{array}{ c c c } \hline 1 & 2 & 3 \\ \hline 4 & 0 & 6 \\ \hline 7 & 5 & 8 \\ \hline \end{array}$ | $\rightarrow$ | $\begin{array}{ c c c } \hline 1 & 2 & 3 \\ \hline 4 & 5 & 6 \\ \hline 7 & 0 & 8 \\ \hline \end{array}$ | $\rightarrow$ | $\begin{array}{ c c c } \hline 1 & 2 & 3 \\ \hline 4 & 5 & 6 \\ \hline 7 & 8 & 0 \\ \hline \end{array}$ |
|---|---------------|---|---------------|---|