

1) Subcarrier spacing = 30 kHz
Subcarriers = 240

$$1 \text{ CP} \Rightarrow \frac{1}{4} \cdot T_{\text{sym}} \cdot u$$

$$2 \text{ CP} \Rightarrow \frac{1}{16} T_{\text{sym}} \cdot u$$

$$T_s = T_{\text{su}} + T_{\text{CP}}$$

$$T_{\text{su}} = \frac{1}{30} \times 10^{-7} \text{ s} = 33 \mu\text{s}$$

for 1 CP case.

$$T_s = T_{\text{su}} + \frac{1}{4} T_{\text{su}} = 33 + \frac{1}{4} 33 \\ = 41.25 \mu\text{s}$$

for 2 CP case

$$T_s = T_{\text{su}} + \frac{1}{16} T_{\text{su}} = 33 + \frac{1}{16} 33 \\ = 35.06 \mu\text{s}$$

$$BW = N \times \Delta f$$

$$= 240 \times 30 \times 10^3 = 7.2 \text{ MHz}$$

$$R = \frac{M \times \Delta f}{N} \times N = 4 \times 30 \times 240 \\ = 28.8 \text{ Mbps}$$

- Guard BW $\rightarrow 10^{-7.2}$
 $= 2.8 \text{ MHz}$

- Spectrum Eff $= \frac{27.8 \text{ Mbps}}{10 \text{ MHz}} = 2.78 \text{ bps/MHz}$

- Smallest FFT is $= \frac{10 \text{ MHz}}{301 \text{ MHz}} = \frac{10 \times 10^6}{3 \times 10^8} = 33.3 \text{ subcarrier spa.}$

- 5

\therefore 512 is the smallest possible FFT

- Sampling rate $= 512 \times 30 \times 10^3 = 15.36 \text{ MHz}$

- for CP1

$$E(T_x) \text{ overhead} = 10 \log \left(\frac{T_s}{T_{\text{sym}}} \right)$$

$$= 10 \log \left(\frac{41.25}{37} \right) = 0.96 \text{ dB}$$

for CP2

$$E(T_x) \text{ overhead} = 10 \log \left(\frac{35.06}{37} \right) = 0.26 \text{ dB}$$

2) $T_{\text{sym}} = \frac{1}{\Delta f}$

$$T_{\text{sym}} + T_{\text{cp}} = T_s = \frac{1}{\Delta f} + T_{\text{cp}}$$

$$T_s = D \cdot T_{\text{cp}} + 1$$

$$T_{\text{cp}} = (T_s - 1) \frac{1}{\Delta f}$$

T_s = overall symbol period

Δf = subcarrier spacing

T_{cp} = CP length

$$\text{Transmitted energy overhead} = 10 \log \left(\frac{T_s}{T_{sym}} \right)$$

$$= 10 \log \left(\frac{\Delta f T_{cp} + 1}{T_{sym}} \right)$$

$$= 10 \log \left(\frac{\Delta f T_{cp}}{T_{sym}} + \frac{1}{T_{sym}} \right)$$

$$= 10 \log \left[(T_{cp} \Delta f + 1) \Delta f \right]$$

$$10 \log \left[(T_{cp} \Delta f + 1) \Delta f \right] \leq 0.5$$

$$\log \left[(T_{cp} \Delta f + 1) \Delta f \right] \leq 0.05$$

$$T_{cp} \Delta f^2 + \Delta f \leq 10^{0.05} = 1.122$$

$$T_{cp} \Delta f + 1 \leq 1.122$$

$$T_{cp} \Delta f \leq 0.122$$

$$\Delta f \leq \frac{0.122}{T_{cp}}$$

let's assume $T_{cp} = 6 \mu s$

$$\Delta f = \frac{0.122}{6 \times 10^{-6}}$$

$$\Delta f = 20 \text{ kHz}$$