

Supervised learning

- Supervised learning is like teaching a computer how to do something by showing it examples.
- In supervised learning, the model learns from labeled training data.

Example: Email Spam Detection

Step1: Data Collection

Step2: Training

Step3: Testing

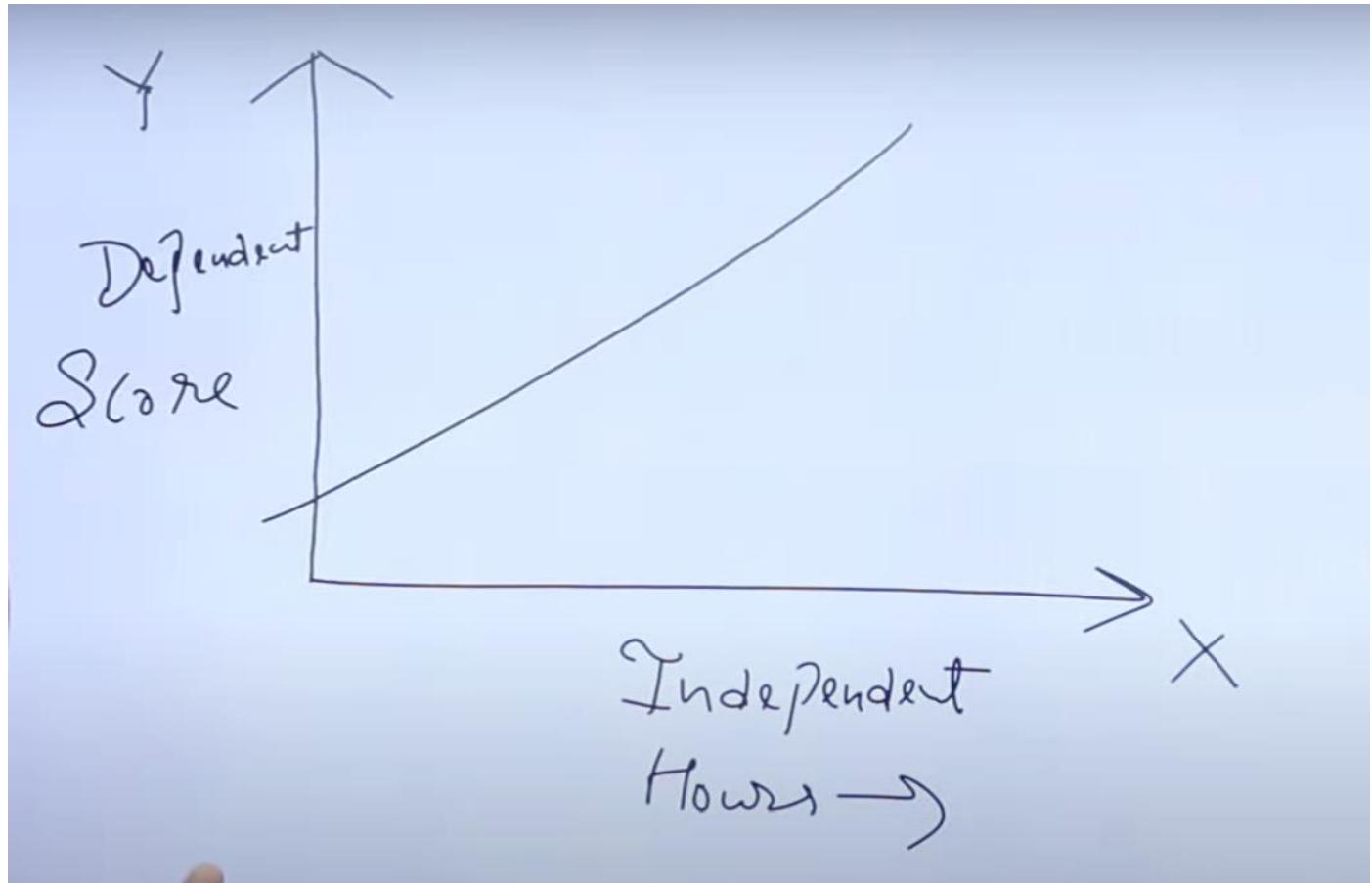
Algorithms

- Classification goal is to assign input data to predefined categories or classes. Algorithms like K-Nearest Neighbors (KNN), Logistic Regression, Decision Trees, Support Vector Machines, and Neural Networks are commonly used for classification tasks.
- Regression goal is to predict a numerical value based on input features. Algorithms like Linear Regression, Polynomial Regression, and various types of regression trees are used for regression tasks.

Regression

- Regression is a statistical method that helps us understand and predict the relationship between variables.
- Describes how one variable (dependent variable) changes as another variable (independent variable) changes.
- Dependent Variable: We are trying to predict or explain(Y).
- Independent Variable: that are used to predict or explain the changes in the dependent variable(X).

For example: predicting salary based on years of experience, predicting exam score based on study hours, predicting resale price based on vehicle age.



Linear Regression

Equation of linear regression: $Y = mx + b$

- Y represents the dependent variable
- X represents the independent variable
- m is the slope of the line (how much Y changes for a unit change in X).
- b is the intercept (the value of Y when X is 0).

Project: Predicting Pizza Prices

Step1: Data Collection

Step2: Calculations

Step3: Prediction

Step4: Visualization

Diameter(X) In Inches	Price(Y) In Dollars	Mean(X)	Mean(Y)	Deviations(X)	Deviations(Y)	Product of Deviations	Sum of Product of Deviations	Square of Deviations for X
8	10	10	13	-2	-3	6	12	4
10	13			0	0	0		0
12	16			2	3	6		4

$$12/8 = 1.5$$

Calculate $m = \text{Sum of product of deviations} / \text{Sum of square of deviation for } X$

Calculate $b = \text{Mean of } Y - (m * \text{Mean of } X)$

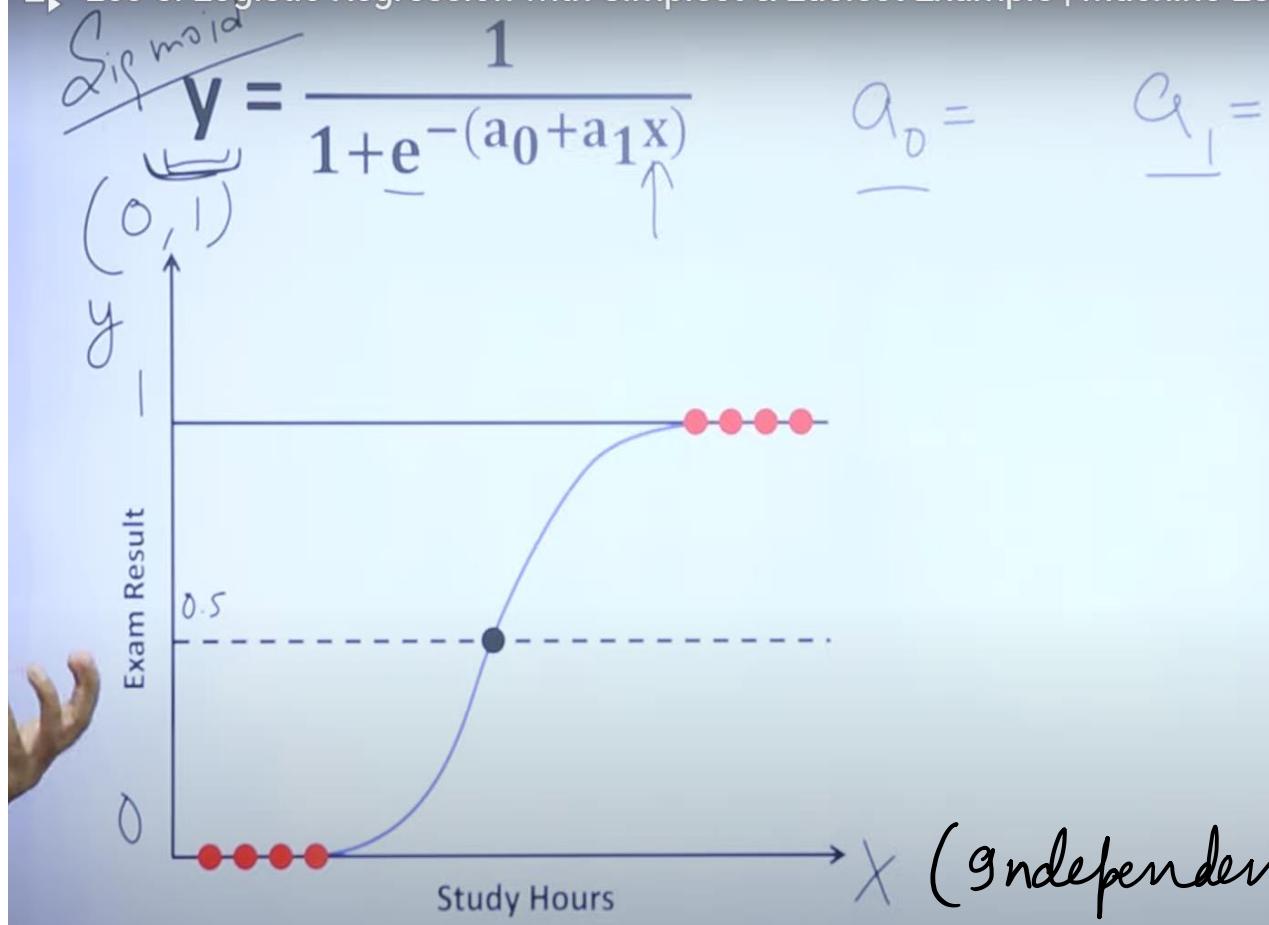
$$Y = mX + b$$

$$13 - (1.5 \times 10) = 30 - 2 = 28$$

visualization



Lec-5: Logistic Regression with Simplest & Easiest Example | Machine Learning



Linear Regression

- supervised regression model
- the dependent variable (the variable you want to predict) is continuous.

- Equation of linear regression:

$$\underline{y} = \underline{a_0} + \underline{a_1} \underline{x_1}$$

- we predict the value by an integer number.

Logistic Regression

- supervised classification model
- dependent variable is categorical and binary (0 or 1), making it suitable for calculating the probability of an event.

- Equation of logistic regression:

Sigmoid $y = \frac{1}{1+e^{-(a_0+a_1x)}}$

- we predict the value by 1 or 0.

Classification (predicting classes)

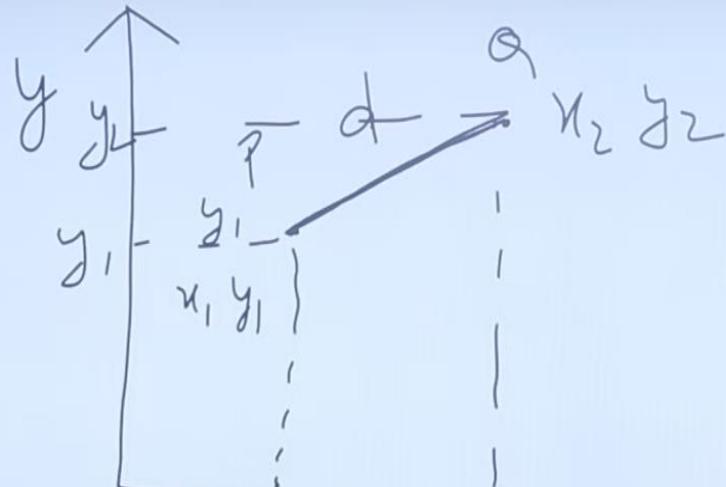
- k -nearest neighbors algorithm (k -NN)
- Example: Predicting Movie Genre

IMDb Rating	Duration	Genre
8.0 (Mission Impossible)	160	Action
6.2 (Gadar 2)	170	Action
7.2 (Rocky & Rani)	168	Comedy
8.2 (OMG 2)	155	Comedy

- Now predict the genre of "Barbie" movie with IMDb rating 7.4 and duration 114 minutes.



Euclidean distance



$$d(p, q) = \sqrt{(x_2 - x_1)^2 + (y_2 - y_1)^2}$$

Step 1: Calculate Distances $x_1 = 7.4, y_1 = 114$

Calculate the Euclidean distance between the new movie and each movie in the dataset.

$$\text{Distance to } (8.0, 160) = \sqrt{(7.4 - 8.0)^2 + (114 - 160)^2} = \sqrt{0.36 + 2116} \approx 46.00$$

$$\text{Distance to } (6.2, 160) = \sqrt{(7.4 - 6.2)^2 + (114 - 170)^2} = \sqrt{1.44 + 3136} \approx 56.01$$

$$\text{Distance to } (7.2, 168) = \sqrt{(7.4 - 7.2)^2 + (114 - 168)^2} = \sqrt{0.04 + 2916} \approx 54.00$$

$$\text{Distance to } (8.2, 155) = \sqrt{(7.4 - 8.2)^2 + (114 - 155)^2} = \sqrt{0.64 + 1681} \approx 41.00$$

Lowest $\rightarrow K=1$

$K=3$

Take 3 value
and choose
majority one.

Step 2: Select K Nearest Neighbors

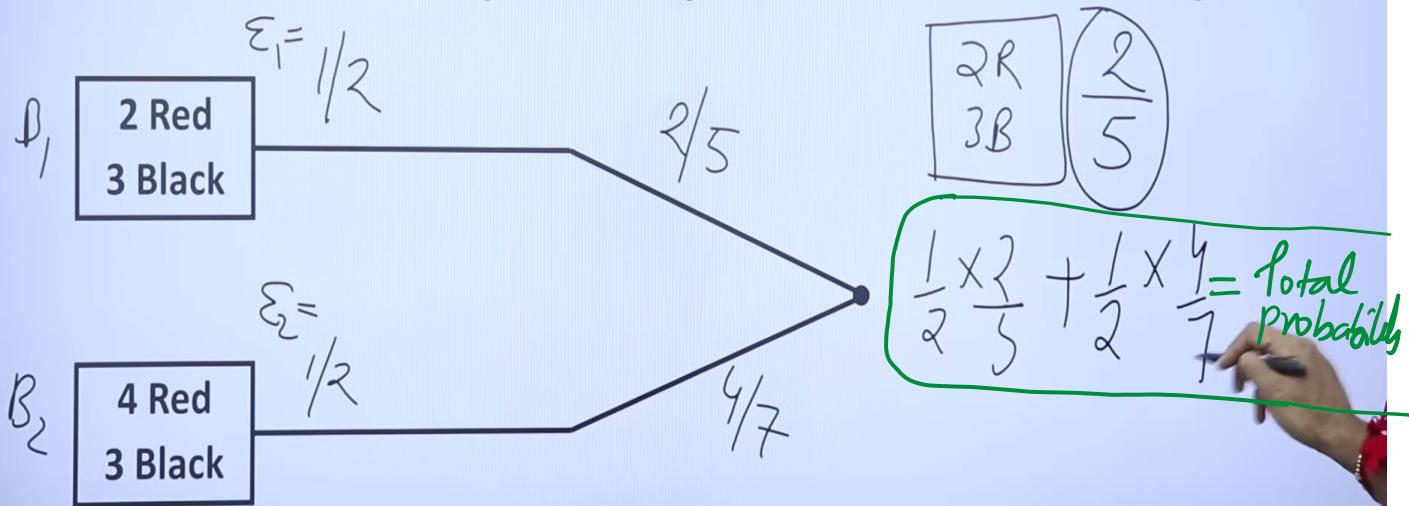
A, C, C

Step 3: Majority Voting (Classification)



Understand Bayes' Theorem With Example

- Bag 1 contain 2 Red and 3 Black balls. Bag 2 contain 3 Red and 4 Black Balls. One ball is drawn at random from one of these bags and its red. Find the probability that it is drawn from Bag 1.



$$P(Y/X) = \frac{P(X|Y) * P(Y)}{P(X)} = \frac{\frac{2}{5} * \frac{1}{2}}{\frac{1}{2}}$$

Baye's theorem

$$P(Y|X_1, X_2, \dots, X_n) = \frac{P(X_1|Y)*P(X_2|Y)*P(X_3|Y)\dots P(X_n|Y)*P(Y)}{P(X_1)*P(X_2)*P(X_3)\dots P(X_n)}$$

$P(Y/X)$ { Finding probability of Y if value of X is given }

$$P(N/X) = \frac{P(X|N) * P(N)}{P(X)}$$

$$P(N|X_1, X_2, \dots, X_n) = \frac{P(X_1|N)*P(X_2|N)*P(X_3|N)\dots P(X_n|N)*P(N)}{P(X_1)*P(X_2)*P(X_3)\dots P(X_n)}$$

Person	X_1 COVID (Yes/No)	X_2 Flu (Yes/No)	Fever (Yes/No)
1	Yes	No	Yes ✓
2	No	Yes	Yes ✓
3	Yes	Yes	Yes ✓
4	No	No	No
5	Yes	No	Yes ✓
6	No	No	Yes ✓
7	Yes	No	Yes ✓
8	Yes	No	No
9	No	Yes	Yes ✓
10	No	Yes	No

Given Person(flu, Covid) = Yes

$$P(\text{yes} | \text{flu, Covid}) = P(\text{flu} | \text{yes}) * P(\text{covid} | \text{yes}) * P(\text{yes})$$

$$P(\text{NO} | \text{flu, Covid}) = P(\text{flu} | \text{NO}) * P(\text{covid} | \text{NO}) * P(\text{NO})$$

Step-1: Prior Probability:

$$P(\text{fever} = \text{yes}) = 7/10$$

$$P(\text{fever} = \text{no}) = 3/10$$

Step-2: Conditional Probability:

	Yes	No
Covid	$4/7$	$2/3$
Flu	$3/7$	$2/3$

$$\frac{12}{70} = \frac{6}{35}$$

greater value

$$\begin{aligned}
 &= \frac{4}{7} \times \frac{3}{7} \times \frac{7}{10} \\
 &= \frac{2}{3} \times \frac{2}{3} \times \frac{7}{10} = \frac{4}{9} = \frac{2}{15} \\
 &\boxed{13}
 \end{aligned}$$

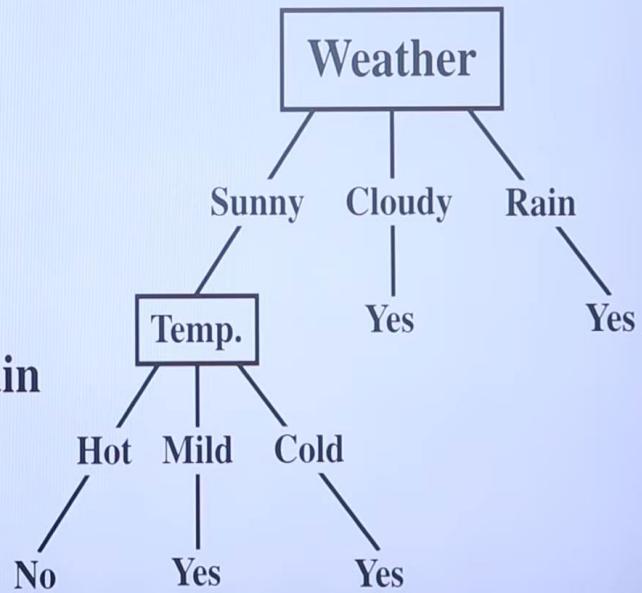
SUBSCRIBE

Naive Bayes Classification

- Supervised learning algorithm
- Based on applying Bayes' Theorem.
- First Understand the Bayes' Theorem.

Decision Tree

- Machine learning algorithm used for both classification and regression tasks.
- Tree Structure
- Decision Nodes
- Leaf Nodes
- Splitting
- Entropy and Information Gain
- Pruning



Day	Weather	Temperature	Humidity	Wind	Play Football?
Day 1	Sunny	Hot	High	Weak	No
Day 2	Sunny	Hot	High	Strong	No
Day 3	Cloudy	Hot	High	Weak	Yes
Day 4	Rain	Mild	High	Weak	Yes
Day 5	Rain	Cool	Normal	Weak	Yes
Day 6	Rain	Cool	Normal	Strong	No
Day 7	Cloudy	Cool	Normal	Strong	Yes
Day 8	Sunny	Mild	High	Weak	No
Day 9	Sunny	Cool	Normal	Weak	Yes
Day 10	Rain	Mild	Normal	Weak	Yes
Day 11	Sunny	Mild	Normal	Strong	Yes
Day 12	Cloudy	Mild	High	Strong	Yes
Day 13	Cloudy	Hot	Normal	Weak	Yes
Day 14	Rain	Mild	High	Strong	No

Calculate IG of Weather

- Step1: Entropy of entire dataset

$$S\{+9,-5\} = -\frac{9}{14} \log_2 \frac{9}{14} - \frac{5}{14} \log_2 \frac{5}{14} = 0.94$$

- Step2: Entropy of all attributes:

- Entropy of Sunny $\{+2,-3\} = -\frac{2}{5} \log_2 \frac{2}{5} - \frac{3}{5} \log_2 \frac{3}{5} = 0.97$

- Entropy of Cloudy $\{+4,-0\} = -\frac{4}{4} \log_2 \frac{4}{4} - \frac{0}{4} \log_2 \frac{0}{4} = 0$

- Entropy of Rain $\{+3,-2\} = -\frac{3}{5} \log_2 \frac{3}{5} - \frac{2}{5} \log_2 \frac{2}{5} = 0.97$

- Information Gain = $\text{Entropy}(\text{whole data}) - \frac{5}{14} \text{Ent}(S) - \frac{4}{14} \text{Ent}(C) - \frac{5}{14} \text{Ent}(R)$
 $= 0.246$

Calculate IG of Temperature

- Step1: Entropy of entire dataset

$$S\{+9,-5\} = -\frac{9}{14} \log_2 \frac{9}{14} - \frac{5}{14} \log_2 \frac{5}{14} = 0.94$$

- Step2: Entropy of all attributes:

- Entropy of Hot $\{+2,-2\} = -\frac{2}{4} \log_2 \frac{2}{4} - \frac{2}{4} \log_2 \frac{2}{4} = 1.0$

- Entropy of Mild $\{+4,-2\} = -\frac{4}{6} \log_2 \frac{4}{6} - \frac{2}{6} \log_2 \frac{2}{6} = 0.91$

- Entropy of Cold $\{+3,-1\} = -\frac{3}{4} \log_2 \frac{3}{4} - \frac{1}{3} \log_2 \frac{1}{3} = 0.81$

- Information Gain = $\text{Entropy}(\text{whole data}) - \frac{4}{14} \text{Ent}(H) - \frac{6}{14} \text{Ent}(M) - \frac{4}{14} \text{Ent}(C)$

- $= 0.029$

Calculate IG of Humidity

- Step1: Entropy of entire dataset

$$S\{+9,-5\} = -\frac{9}{14} \log_2 \frac{9}{14} - \frac{5}{14} \log_2 \frac{5}{14} = 0.94$$

- Step2: Entropy of all attributes:

$$\text{Entropy of High } \{+3,-4\} = -\frac{3}{7} \log_2 \frac{3}{7} - \frac{4}{7} \log_2 \frac{4}{7} = 0.98$$

$$\text{Entropy of Normal } \{+6,-1\} = -\frac{6}{7} \log_2 \frac{6}{7} - \frac{1}{7} \log_2 \frac{1}{7} = 0.59$$

$$\begin{aligned} \text{Information Gain} &= \text{Entropy(whole data)} - \frac{7}{14} \text{Ent(H)} - \frac{7}{14} \text{Ent(N)} \\ &= 0.15 \end{aligned}$$

Calculate IG of Wind

- Step1: Entropy of entire dataset

$$S\{+9,-5\} = -\frac{9}{14} \log_2 \frac{9}{14} - \frac{5}{14} \log_2 \frac{5}{14} = 0.94$$

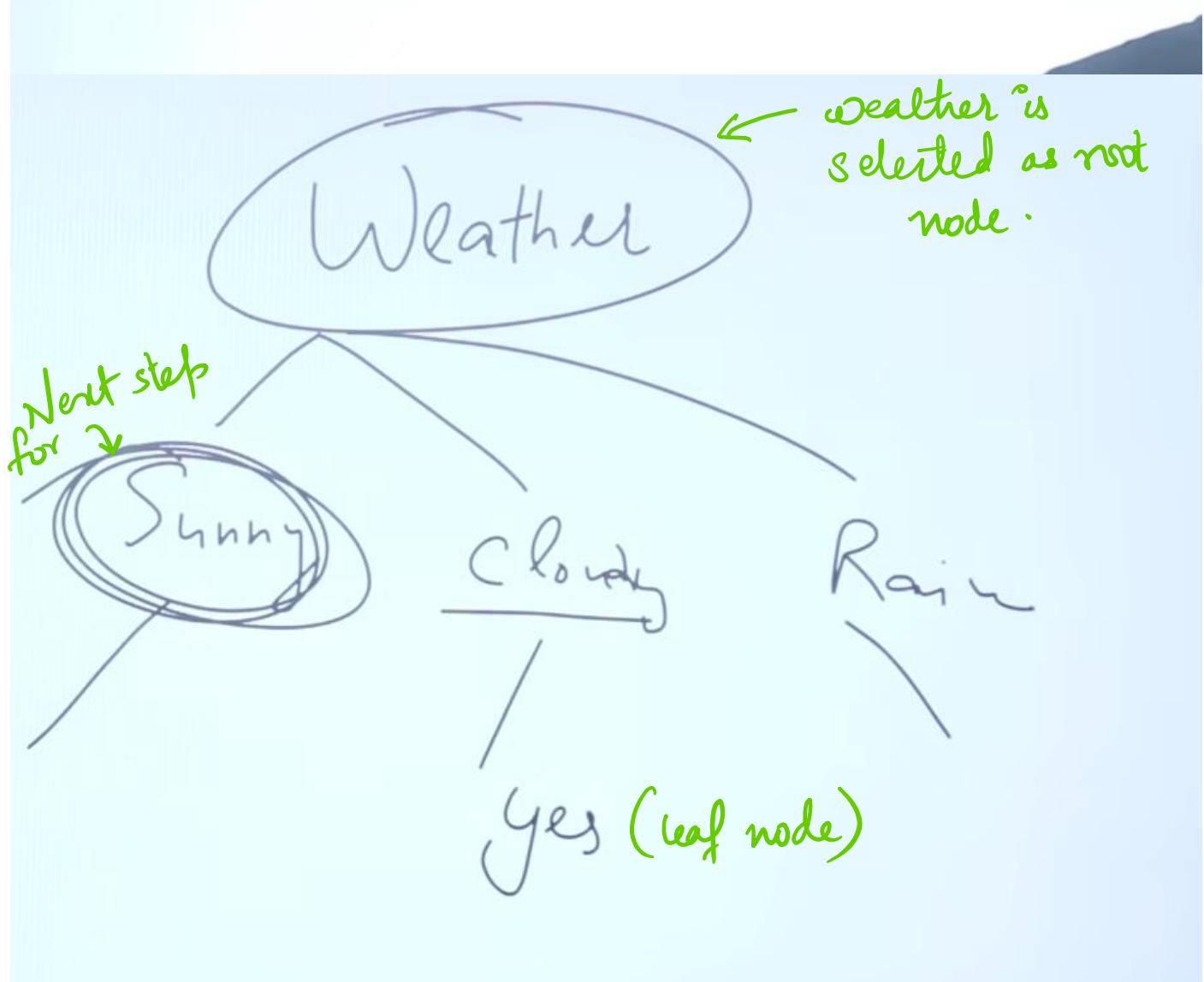
- Step2: Entropy of all attributes:

$$\text{Entropy of Strong } \{+3,-3\} = -\frac{3}{6} \log_2 \frac{3}{6} - \frac{3}{6} \log_2 \frac{3}{6} = 1.0$$

$$\text{Entropy of Normal } \{+6,-2\} = -\frac{6}{8} \log_2 \frac{6}{8} - \frac{2}{8} \log_2 \frac{2}{8} = 0.81$$

$$\begin{aligned} \text{Information Gain} &= \text{Entropy(whole data)} - \frac{6}{14} \text{Ent(S)} - \frac{8}{14} \text{Ent(W)} \\ &= 0.0478 \end{aligned}$$

- Gain (S, Weather) = **0.246** — *greater value*
- Gain (S, Temp) = **0.029** —
- Gain (S, Humidity) = **0.15** —
- Gain (S, Wind) = **0.0478** —



Day	Weather	Only Sunny data are selected			Play Football?
		Temperature	Humidity	Wind	
Day 1	Sunny	Hot	High	Weak	No
Day 2	Sunny	Hot	High	Strong	No
Day 8	Sunny	Mild	High	Weak	No
Day 10	Sunny	Cool	Normal	Weak	Yes
Day 11	Sunny	Mild	Normal	Strong	Yes

Calculate IG of Temperature

- Step1: Entropy of Sunny $\{+2, -3\} = -\frac{2}{5} \log_2 \frac{2}{5} - \frac{3}{5} \log_2 \frac{3}{5} = 0.97$
- Step2: Entropy of all attributes:
 - Entropy of Hot $\{+0, -2\} = -\frac{0}{2} \log_2 \frac{0}{2} - \frac{2}{2} \log_2 \frac{2}{2} = 0$
 - Entropy of Mild $\{+1, -1\} = -\frac{1}{2} \log_2 \frac{1}{2} - \frac{1}{2} \log_2 \frac{1}{2} = 1.0$
 - Entropy of Cool $\{+1, -0\} = -\frac{1}{1} \log_2 \frac{1}{1} - \frac{0}{1} \log_2 \frac{0}{1} = 0$
- Information Gain = Entropy(Sunny) - $\frac{2}{5} \text{Ent(H)} - \frac{2}{5} \text{Ent(M)} - \frac{1}{5} \text{Ent(C)}$
 $= 0.57$

Calculate IG of Humidity

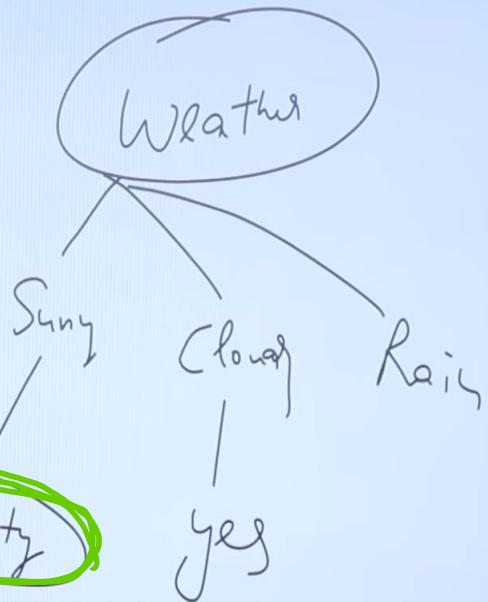
- Step1: Entropy of Sunny $\{+2,-3\} = -\frac{2}{5} \log_2 \frac{2}{5} - \frac{3}{5} \log_2 \frac{3}{5} = 0.97$
- Step2: Entropy of all attributes:
- Entropy of Humid $\{+0,-3\} = -\frac{0}{3} \log_2 \frac{0}{3} - \frac{3}{3} \log_2 \frac{3}{3} = 0$
- Entropy of Normal $\{+2,-0\} = -\frac{2}{2} \log_2 \frac{2}{2} - \frac{0}{2} \log_2 \frac{0}{2} = 0$
- Information Gain= Entropy(Sunny) $- \frac{3}{5} \text{Ent}(H) - \frac{2}{5} \text{Ent}(M)$
 $= 0.97$

Calculate IG of Wind

- Step1: Entropy of Sunny $\{+2,-3\} = -\frac{2}{5} \log_2 \frac{2}{5} - \frac{3}{5} \log_2 \frac{3}{5} = 0.97$
- [Step2: Entropy of all attributes:
- Entropy of Strong $\{+1,-1\} = -\frac{1}{2} \log_2 \frac{1}{2} - \frac{1}{2} \log_2 \frac{1}{2} = 1$
- Entropy of Weak $\{+1,-2\} = -\frac{1}{3} \log_2 \frac{1}{3} - \frac{2}{3} \log_2 \frac{2}{3} = 0.918$
- Information Gain= Entropy(Sunny) $- \frac{2}{5} \text{Ent}(S) - \frac{3}{5} \text{Ent}(W)$
 $= 0.019$

- Gain (S_{sunny} , Temp) = 0.57
- Gain (S_{sunny} , Humidity) = 0.97
- Gain (S_{sunny} , Wind) = 0.019

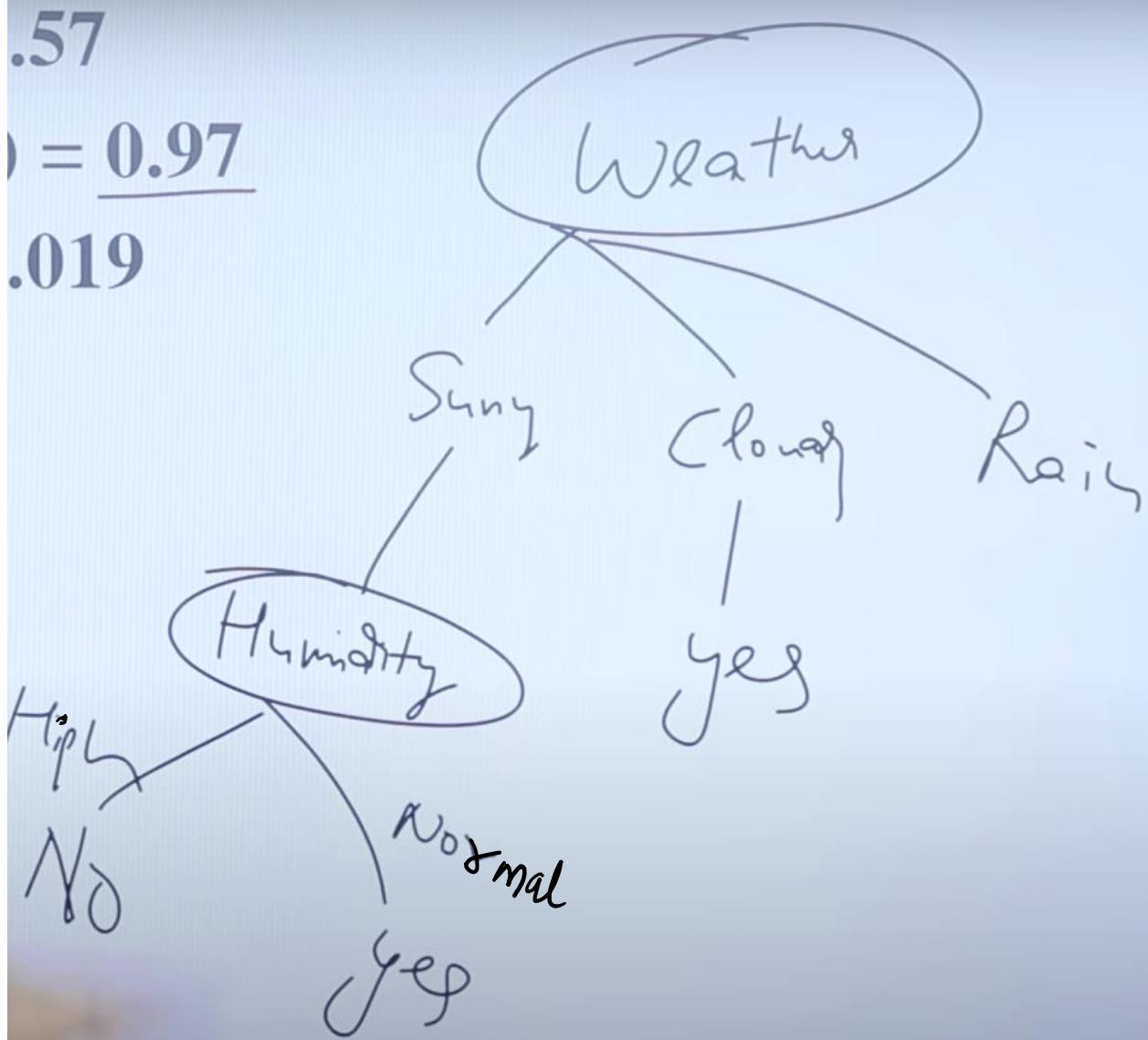
Humidity is selected under 'Sunny'



.57

) = 0.97

.019



Day	Weather	Temperature	Humidity	Wind	Play Football?
Day 4	Rain	Mild	High	Weak	Yes
Day 5	Rain	Cool	Normal	Weak	Yes
Day 6	Rain	Cool	Normal	Strong	No
Day 10	Rain	Mild	Normal	Weak	Yes
	Rain	Mild	High	Strong	No

Calculate IG of Temperature

Step1: Entropy of Rain $\{+3, -2\} = -\frac{3}{5} \log_2 \frac{3}{5} - \frac{2}{5} \log_2 \frac{2}{5} = 0.97$

Step2: Entropy of all attributes:

Entropy of Hot $\{+0, -0\} = -\frac{0}{2} \log_2 \frac{0}{2} - \frac{0}{2} \log_2 \frac{0}{2} = 0$

• Entropy of Mild $\{+2, -1\} = -\frac{2}{3} \log_2 \frac{2}{3} - \frac{1}{3} \log_2 \frac{1}{3} = 0.918$

Entropy of Cool $\{+1, -1\} = -\frac{1}{2} \log_2 \frac{1}{2} - \frac{1}{2} \log_2 \frac{1}{2} = 1.0$

Information Gain = Entropy(Rain) - $\frac{0}{5} \text{Ent(H)} - \frac{3}{5} \text{Ent(M)} - \frac{2}{5} \text{Ent(C)}$

= 0.019

Calculate IG of Humidity

Step1: Entropy of Rain {+3,-2} = $-\frac{3}{5} \log_2 \frac{3}{5} - \frac{2}{5} \log_2 \frac{2}{5} = 0.97$

Step2: Entropy of all attributes:

Entropy of Sough {+1,-1} = $-\frac{1}{2} \log_2 \frac{1}{2} - \frac{1}{2} \log_2 \frac{1}{2} = 1$

Entropy of Normal {+2,-1} = $-\frac{2}{3} \log_2 \frac{2}{3} - \frac{1}{3} \log_2 \frac{1}{3} = 0.918$

Information Gain = Entropy(Rain) - $\frac{2}{5} \text{Ent}(S) - \frac{3}{5} \text{Ent}(W)$
 $= 0.019$

Calculate IG of Wind

Step1: Entropy of Rain {+3,-2} = $-\frac{3}{5} \log_2 \frac{3}{5} - \frac{2}{5} \log_2 \frac{2}{5} = 0.97$

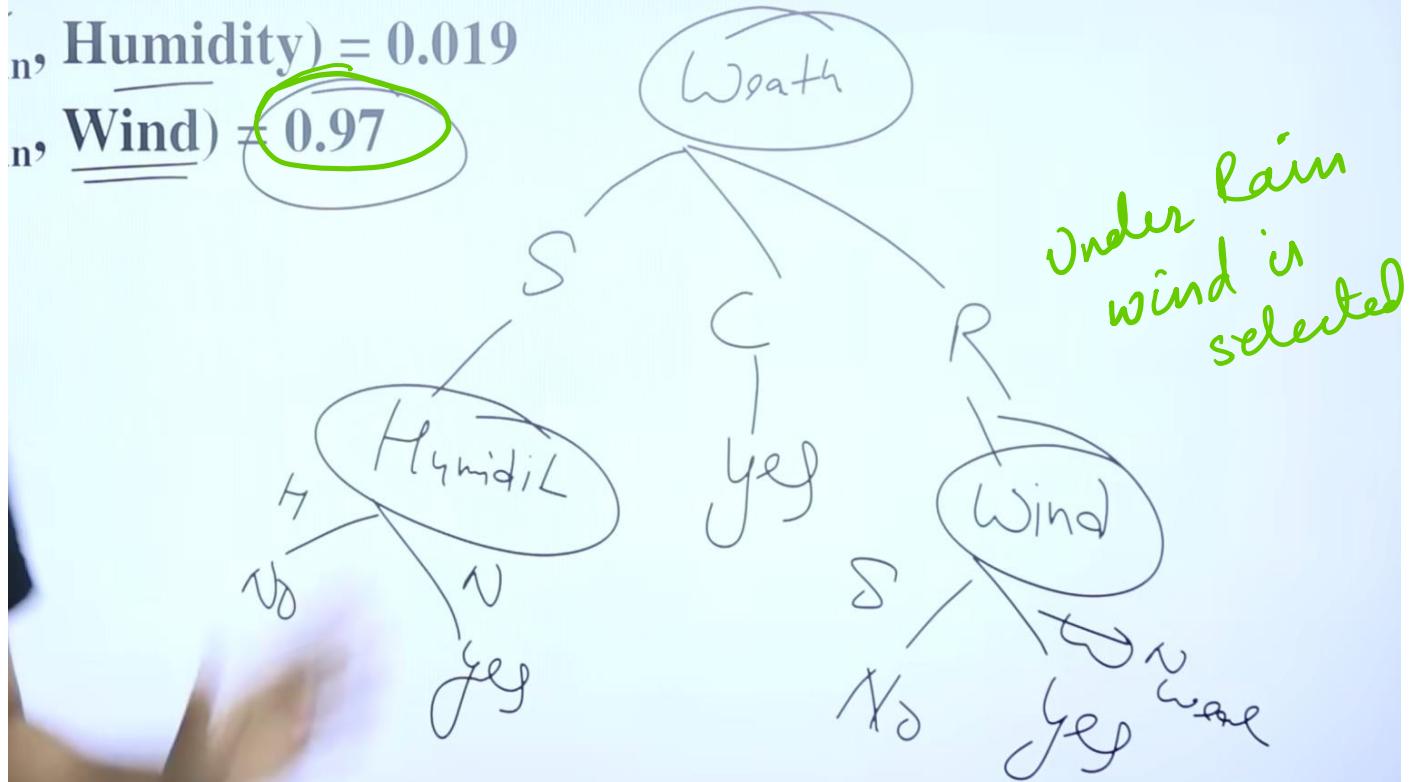
Step2: Entropy of all attributes:

Entropy of Strong {+0,-2} = $-\frac{0}{2} \log_2 \frac{0}{2} - \frac{2}{2} \log_2 \frac{2}{2} = 0$

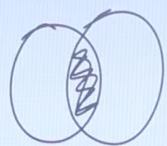
Entropy of Weak {+3,-0} = $-\frac{3}{3} \log_2 \frac{3}{3} - \frac{0}{3} \log_2 \frac{0}{3} = 0$

Information Gain = Entropy(Rain) - $\frac{2}{5} \text{Ent}(S) - \frac{3}{5} \text{Ent}(W)$
 $= 0.97$

$n, \underline{\text{Temp}}) = 0.019$
 $n, \underline{\text{Humidity}}) = 0.019$
 $n, \underline{\text{Wind}}) = 0.97$



Conditional Probability



$$P(E/F) = \frac{P(E \cap F)}{P(F)}$$

Tossing a fair coin three times

$$S = \{\underline{\text{HHH}}, \underline{\text{HHT}}, \underline{\text{HTH}}, \underline{\text{HTT}}, \text{THH}, \text{THT}, \text{TTH}, \text{TTT}\}$$

P(E: at least two Tails appear)

$$\frac{4}{8} = \frac{1}{2}$$

P(F: First coin shows Head) = 1/2

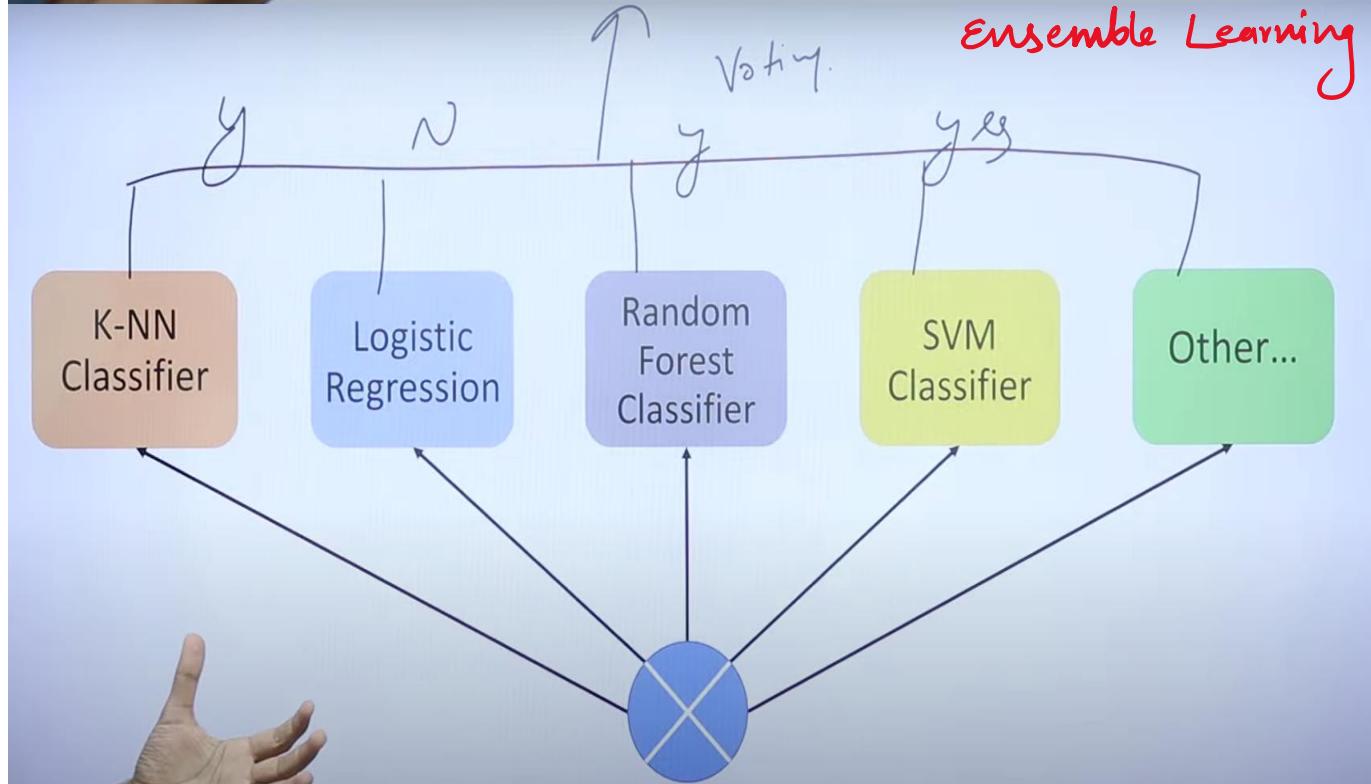
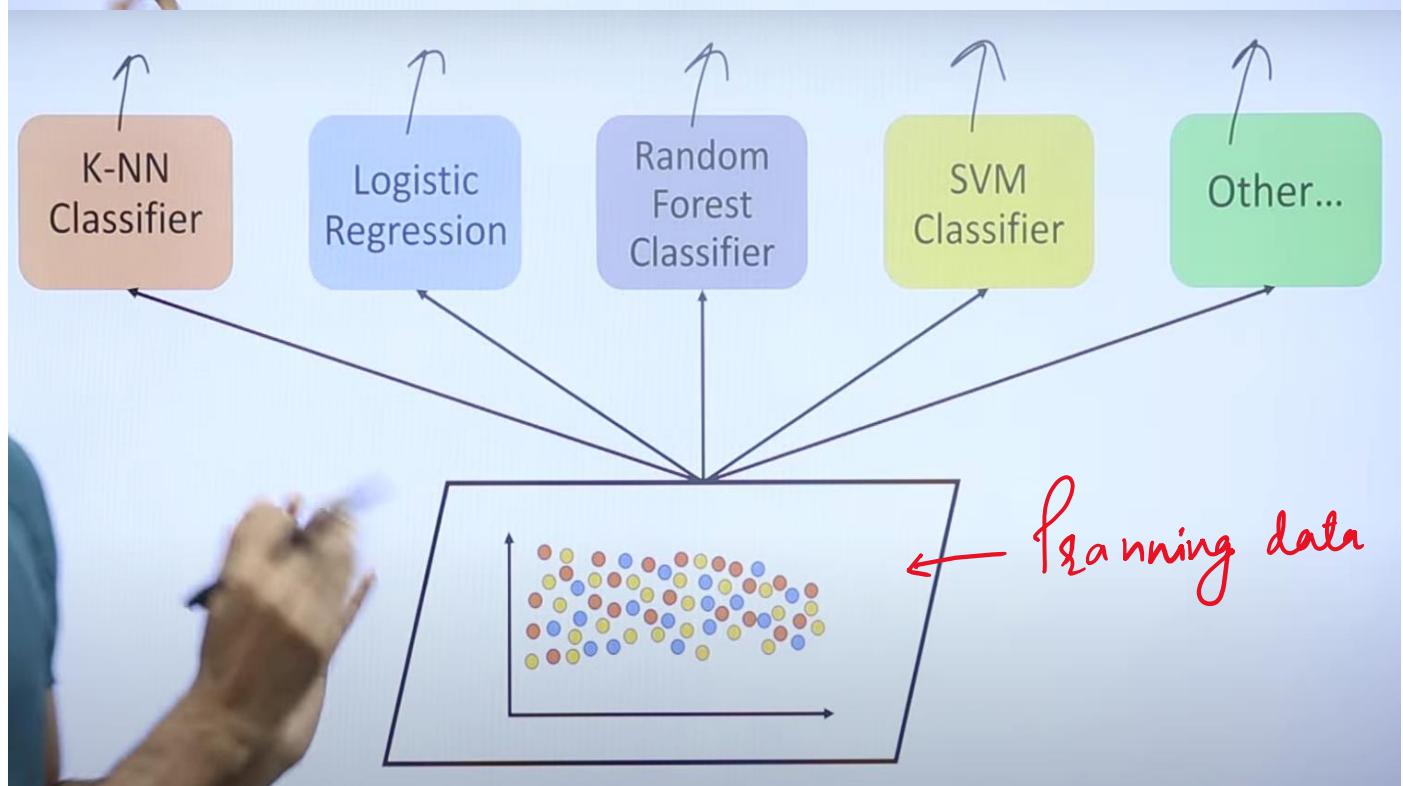
$$\frac{1}{2} = \frac{1}{2}$$

$$\bar{E} \cap \bar{F} =$$

Ensemble Learning

grouping up the different outcomes and predicting the best result

It uses multiple learning algorithms to obtain better predictive performance



Types of Ensemble Learning

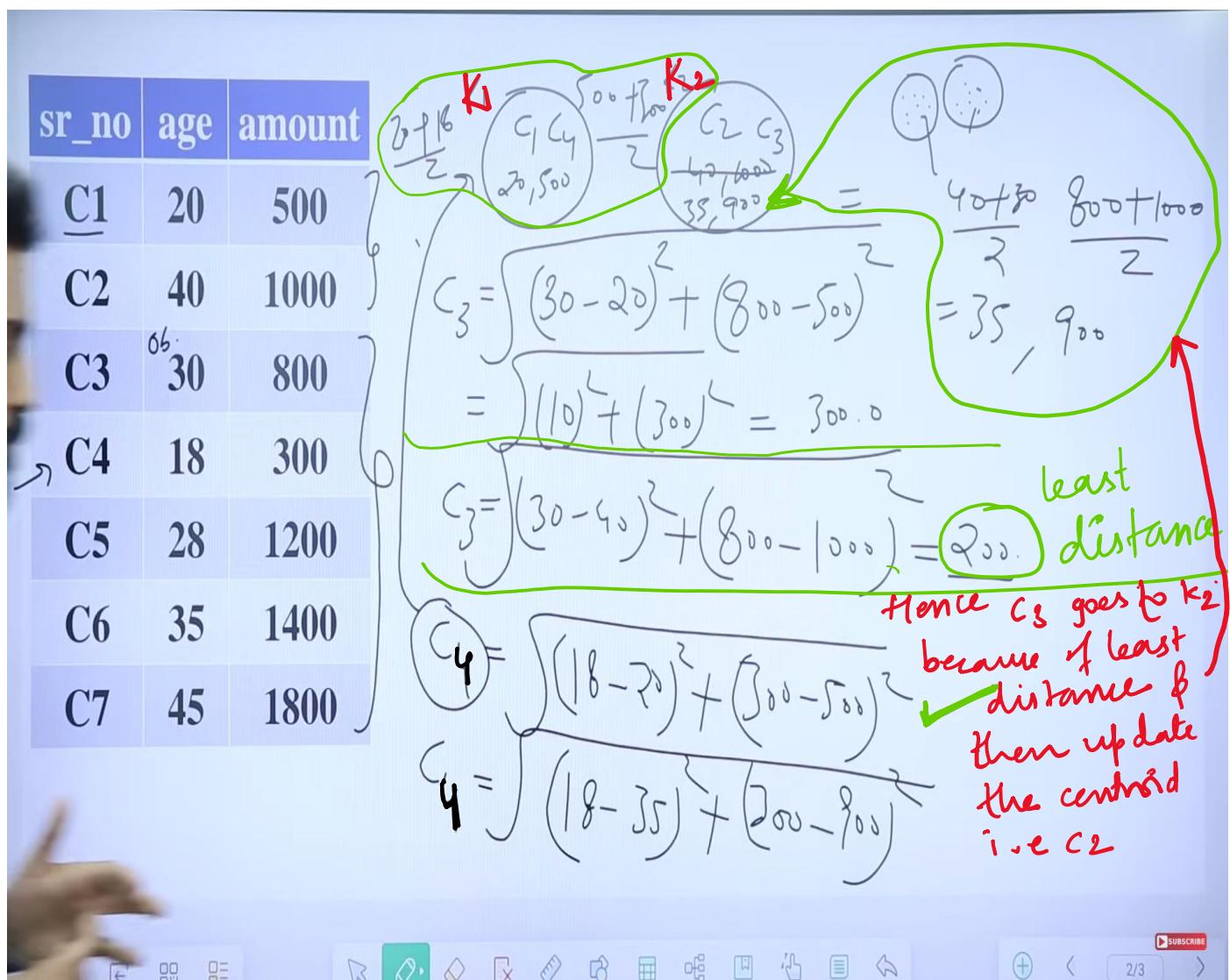
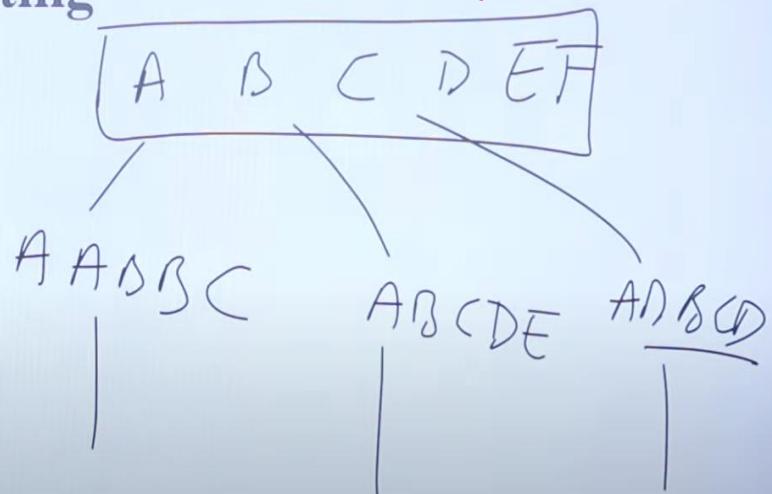
Ensemble Learning uses Random Forest

1. Bootstrap aggregating

2. Boosting

3. Stacking

4. Voting



Hierarchical clustering

Aggregating
↓

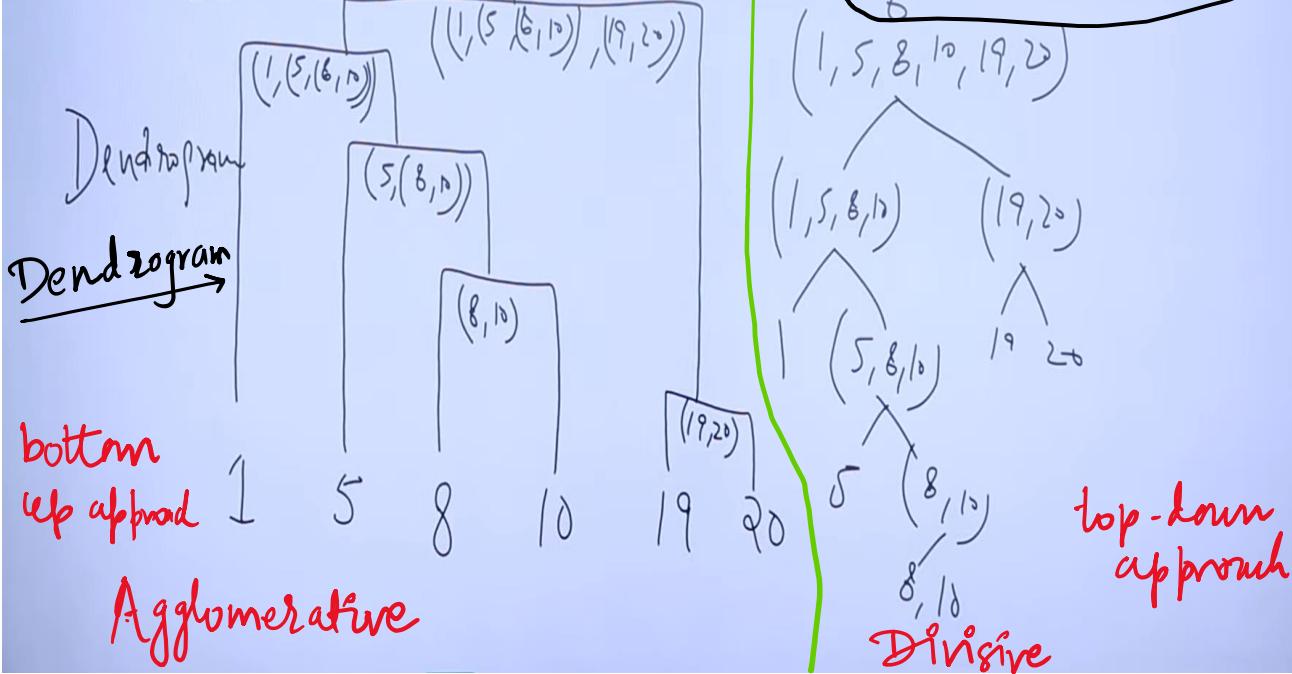
Dividing
↑

- Agglomerative & Divisive

Dendrogram
Dendrogram

bottom
up approach

Agglomerative



Single Linkage Clustering | Agglomerative Clustering | Hierarchical Clustering

Sample no.	X	Y
S ₁	4	3
S ₂	1	4
S ₃	2	1
S ₄	3	8
S ₅	6	9
S ₆	5	1

	S ₁	S ₂	S ₃	S ₄	S ₅	S ₆
S ₁	0	<u>3.16</u>	2.82	5.09	6.32	2.23
S ₂	--	0	<u>3.16</u>	4.47	7.07	5
S ₃	--	--	0	7.07	8.94	3
S ₄	--	--	--	0	<u>3.16</u>	7.28
S ₅	--	--	--	--	0	<u>8.06</u>
S ₆	--	--	--	--	--	0

$$\sqrt{(x_2 - x_1)^2 + (y_2 - y_1)^2}$$



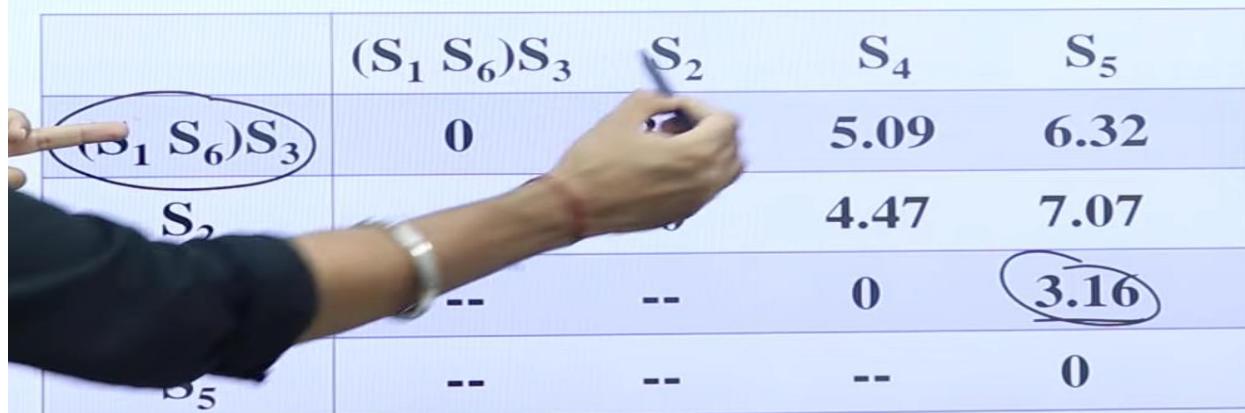
	S_1	S_2	S_3	S_4	S_5	S_6
S_1	0	<u>3.16</u>	2.82	5.09	6.32	2.23
S_2	--	0	<u>3.16</u>	4.47	7.07	5
S_3	--	--	0	7.07	8.94	3
S_4	--	--	--	0	3.16	7.28
S_5	--	--	--	--	0	8.06
S_6	--	--	--	--	--	0

$\hat{y} = \frac{1}{2} (y_2 - y_1)^2 \quad (S_1, S_6)$ Minimum distance

	S_1	S_2	S_3	S_4	S_5	S_6
S_1	0	<u>3.16</u>	2.82	5.09	6.32	2.23
S_2	--	0	<u>3.16</u>	4.47	7.07	5
S_3	--	--	0	7.07	8.94	3
S_4	--	--	--	0	3.16	7.28
S_5	--	--	--	--	0	8.06
S_6	--	--	--	--	--	0

	$(S_1 S_6)$	S_2	S_3	S_4	S_5
$(S_1 S_6)$	0	<u>3.16</u>	<u>2.82</u>	5.09	6.32
S_2	--	0	<u>3.16</u>	4.47	7.07
S_3	--	--	0	7.07	8.94
S_4	--	--	--	0	3.16
S_5	--	--	--	--	0

	$(S_1 S_6)$	S_2	S_3	S_4	S_5
$(S_1 S_6)$	0	3.16	2.82	5.09	6.32
S_2	--	0	3.16	4.47	7.07
S_3	--	--	0	7.07	8.94
S_4	--	--	--	0	3.16
S_5	--	--	--	--	0



	$(S_1 S_6)S_3$	S_2	S_4	S_5
$(S_1 S_6)S_3$	0		5.09	6.32
S_2	--	--	4.47	7.07
S_4	--	--	0	3.16
S_5	--	--	--	0

	$(S_1 S_6)S_3$	S_2	S_4	S_5
$(S_1 S_6)S_3$	0	3.16	5.09	6.32
S_2	--	0	4.47	7.07
S_4	--	--	0	3.16
S_5	--	--	--	0

	$((S_1 S_6)S_3)S_2$	$S_4 S_5$
$((S_1 S_6)S_3)S_2$	0	5.09
$S_4 S_5$	--	0

☰ Complete Linkage
Clustering with Example | Clustering in Unsupervised Learning | ML
🕒 ↗

2
2
6
3

	2	6	9	11	3
2	0	4	7	9	1
6	4	0	3	5	3
9	7	3	0	2	6
11	9	5	2	0	8
3	1	3	6	8	0

minimum distance

$$\begin{aligned} & \sqrt{(x_1 - x_2)^2 + (y_1 - y_2)^2} \\ & \sqrt{(2 - 9)^2} \\ & = \sqrt{(-7)^2} = \sqrt{49} = 7 \\ & \sqrt{(2 - 6)^2} = \sqrt{(-4)^2} = \sqrt{16} = 4 \end{aligned}$$

$d\{(2, 3), 6\} =$

$\text{Max}\{(2, 6), (3, 6)\}$

$(2, 3) / \{6\}$

$= \text{Max}\{(2, 6), (3, 6)\}$

	2	6	9	11	3
2	0	4	7	9	1
6	4	0	3	5	3
9	7	3	0	2	6
11	9	5	2	0	8
3	1	3	6	8	0

	(2, 3)	6	9	11
(2, 3)	0	4	7	9 ✓
6	4	0	3	5
9	7	3	0	2
11	9	5	2	0

$$\begin{aligned} & (2, 3) / \{6\} \\ & = \text{Max}\{(2, 11), (3, 11)\} \\ & = (9, 8) \end{aligned}$$



	(2, 3)	6	9	11
(2, 3)	0	4	7	9
6	4	0	3	5
9	7	3	0	2
11	9	5	2	0

$$\begin{aligned}
 & (9, 11) = 6 \\
 & (9, 6) = 3 \\
 & \text{Max} (9, 6) = 6 \\
 & (11, 6) = 0
 \end{aligned}$$

11, (2, 3)

7, 9
↓

	(2, 3)	6	(9, 11)
(2, 3)	0	4	9
6	4	0	5
(9, 11)	9	5	0

s

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	(2, 3)	6	(9, 11)
(2, 3)	0	4	9
6	4	0	5
(9, 11)	9	5	0

(2, 3), 6 (9, 11)

(2, 3) (9, 11)

9
⑨

	((2, 3), 6)	(9, 11)
((2, 3), 6)	0	9
(9, 11)	9	0

K-medoids clustering

i	x	y
D1	2	3
D2	5	7
D3	8	3
D4	3	5
D5	7	2
D6	6	8
D7	1	4
D8	4	6
D9	9	5
D10	5	4

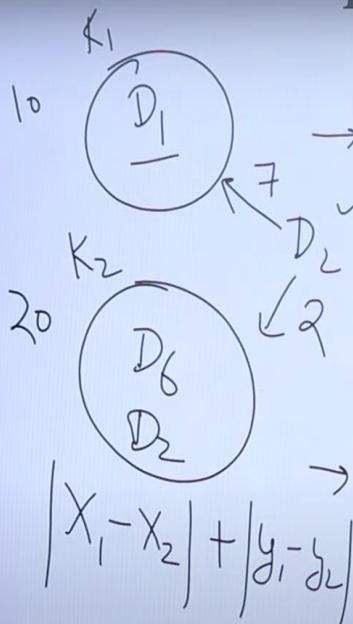
Man Hatton distance formula. It is a very simple formula. What does Man

Selection Write Eraser Clean Ruler Shape Form Mind map Note Move Grid Undo Add Previous Page Next

2/6 SUBSCRIBE

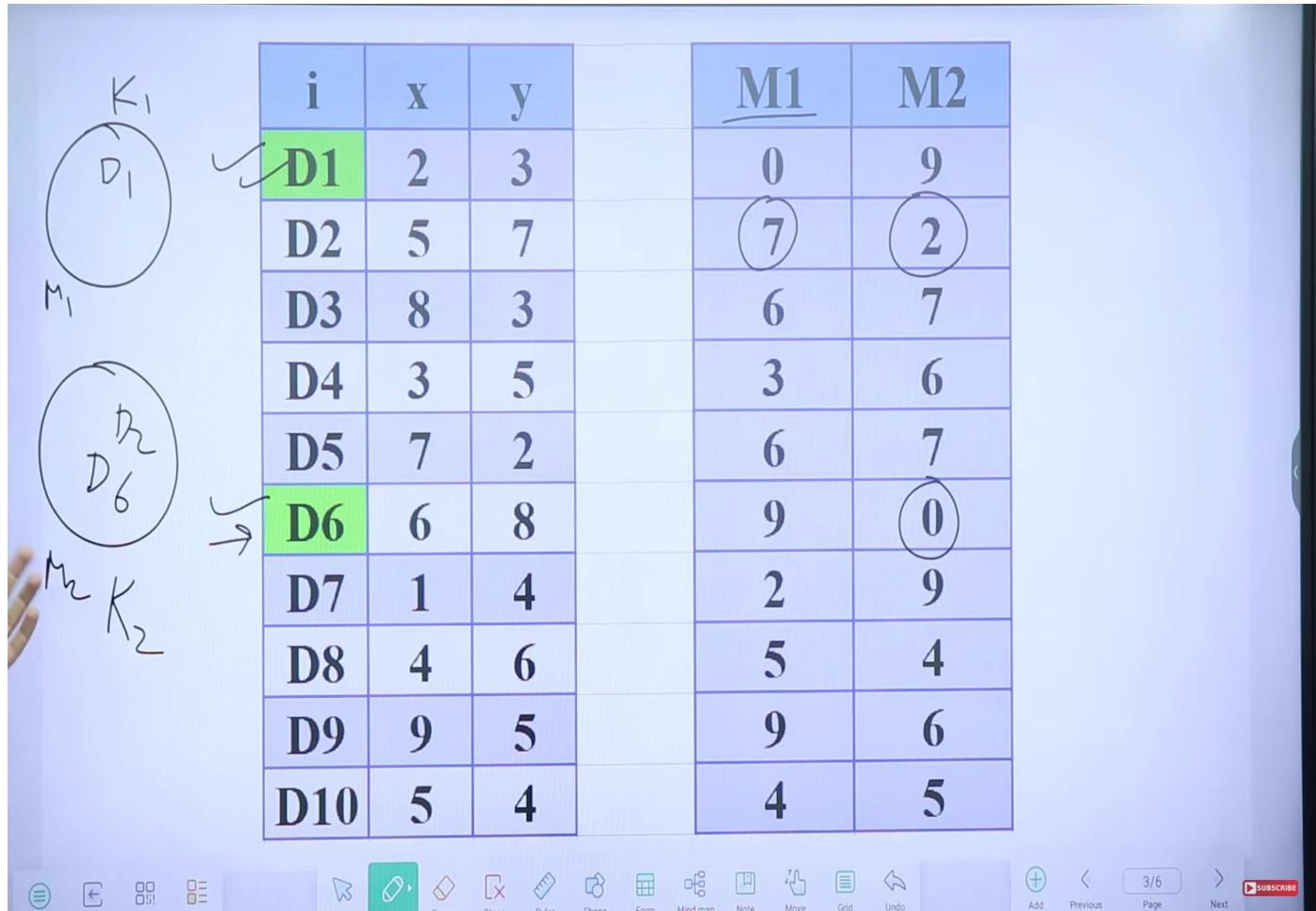
☰ K-medoids Clustering with Numerical Example | Machine Learning

K-medoids clustering



i	x	y
D1	2 ✓	3 ✓
D2 ✓	5 ✓	7
D3	8	3
D4	3	5
D5	7	2
D6	6 ✓	8 ✓
D7	1	4
D8	4	6
D9	9	5
D10	5	4

$$\begin{aligned}
 D_2 &= |x_2 - x_1| + |y_2 - y_1| \\
 &= |5 - 2| + |7 - 3| \\
 &= 3 + 4 = 7 \\
 D_6 &= |x_6 - x_2| + |y_6 - y_2| \\
 &= |6 - 5| + |8 - 7| \\
 &= 1 + 1 = 2
 \end{aligned}$$

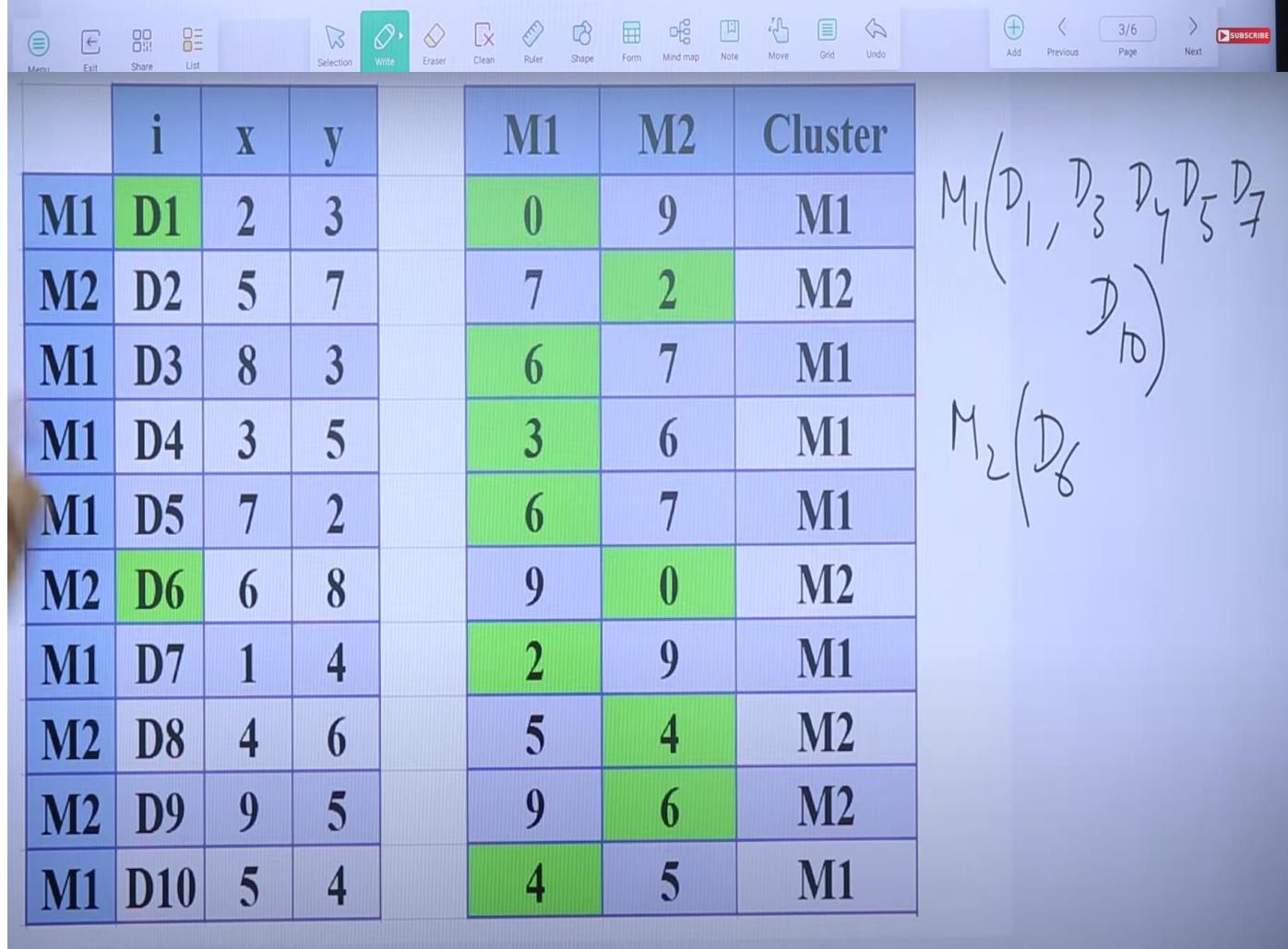


Handwritten notes on the left side of the screen:

- K_1 (top cluster)
- D_1 (point in K_1)
- M_1
- K_2 (bottom cluster)
- D_6 (point in K_2)
- M_2

Two arrows point from the handwritten notes to the first two columns of the table.

i	x	y	<u>M1</u>	M2
D1	2	3	0	9
D2	5	7	(7)	(2)
D3	8	3	6	7
D4	3	5	3	6
D5	7	2	6	7
D6	6	8	9	(0)
D7	1	4	2	9
D8	4	6	5	4
D9	9	5	9	6
D10	5	4	4	5



	i	x	y	M1	M2	Cluster
M1	D1	2	3	0	9	M1
M2	D2	5	7	7	2	M2
M1	D3	8	3	6	7	M1
M1	D4	3	5	3	6	M1
M1	D5	7	2	6	7	M1
M2	D6	6	8	9	0	M2
M1	D7	1	4	2	9	M1
M2	D8	4	6	5	4	M2
M2	D9	9	5	9	6	M2
M1	D10	5	4	4	5	M1

$$M_1(D_1, D_3, D_4, D_5, D_7, D_{10})$$

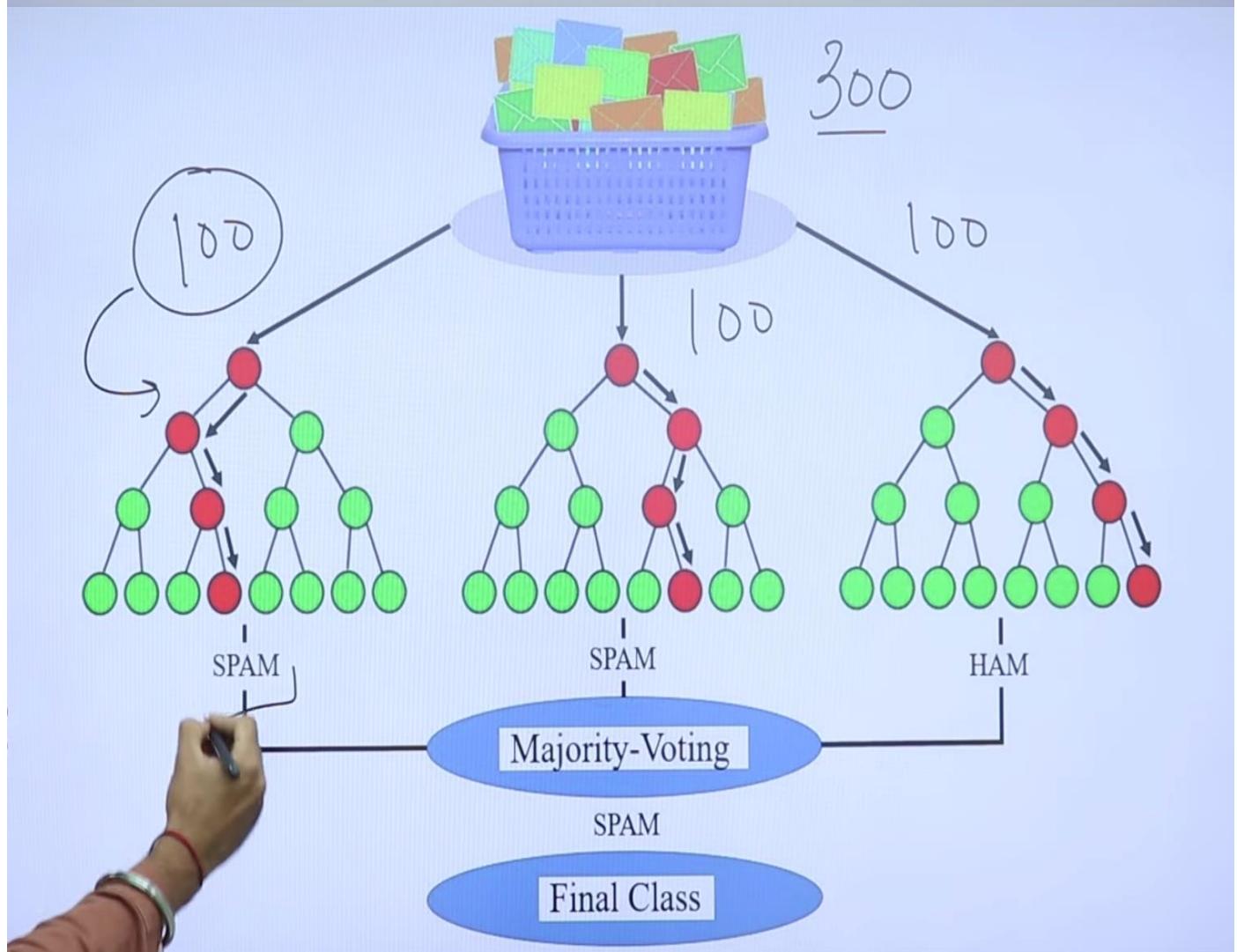
$$M_2(D_6)$$

	i	x	y	M1	M2	Cluster	Total Cost
M1	D1	2	3	0	9	M1	0
M2	D2	5	7	7	2	M2	2
M1	D3	8	3	6	7	M1	6
M1	D4	3	5	3	6	M1	3
M1	D5	7	2	6	7	M1	6
M2	D6	6	8	9	0	M2	0
M1	D7	1	4	2	9	M1	2
M2	D8	4	6	5	4	M2	4
M2	D9	9	5	9	6	M2	6
M1	D10	5	4	4	5	M1	4
							33

	i	x	y	M1	K	Cluster	Total Cost
M1	D1	2	3	0	3	M1	0
K	D2	5	7	7	4	K	4
M1	D3	8	3	6	7	M1	6
K	D4	3	5	3	0	K	0
M1	D5	7	2	6	7	M1	6
K	D6	6	8	9	6	K	6
M1	D7	1	4	2	3	M1	2
K	D8	4	6	5	2	K	2
K	D9	9	5	9	6	K	6
K	D10	5	4	4	3	K	3
							35

Random Forest

- Random forests or random decision forests is an ensemble learning method for classification, regression.
 - Random decision forests correct for decision trees' habit of overfitting to their training set.
 - Step1: Create Bootstrap Dataset from Original data by Randomly choosing data(repetition is allowed).
- Step2: Create Randomized Decision Tree from Bootstrap Dataset.
- Step3: Finally output of the random forest is the class selected by most trees.



Ques. Suppose you have the following dataset with two features (X and Y) and corresponding labels:

$$\begin{aligned} & \sqrt{(x_1 - x_2)^2 + (y_1 - y_2)^2} \\ & \sqrt{(2-6)^2 + (3-7)^2} \\ & = \sqrt{16+16} \\ & \sqrt{32} \end{aligned}$$

Data Point	X	Y	Label
1	2.0	3.0	A
2	3.0	4.0	A
3	5.0	6.0	B
4	7.0	8.0	B
5	10.0	10.0	A

$$\sqrt{(2-6)^2 + (3-7)^2} = \sqrt{32}$$

Now, consider a new data point with $x_1=6.0$ and $y_1=7.0$. Using kNN with $k=3$, predict the label for this new data point.

Ques. Consider a dataset with a single feature (X) and corresponding target values (Y):

Data Point	Input X	Y Target
1	2.0	5.0
2	4.0	8.0
3	6.0	12.0
4	8.0	15.0
5	10.0	20.0

$$\frac{12+15}{2} = \frac{27}{3} = 9$$

$$\sqrt{(6-7)^2 + (8-9)^2} = \sqrt{2}$$

$$\sqrt{(8-7)^2 + (10-9)^2} = \sqrt{2}$$

Now, consider a new data point with $X_1=7.0$. Using kNN with $k=2$, predict the target value (Y) for this new data point.

13.5

Mean

- The mean, or average, is the sum of all values in a dataset divided by the number of values.
- It represents the central point around which the data is distributed.
- Salary Packages in Lakhs

• 2, 3, 4, 5, 8, 9, 32

$$\frac{2+3+4+5+8+9+32}{7}$$

Median

- The median is the middle value of a dataset when it is ordered.

2, 3, 4, 5, 8, 9, 32 3 4

$$\text{Odd} = \frac{7+1}{2} = \frac{8}{2} = 4$$

$$\text{Even} = \frac{5+8}{2}$$

Mode

- The mode is the value that appears most frequently in a dataset.

2, 3, 4, ~~3~~, 5, 7, ~~3~~, 8, 30



Range

- It is a measure of the spread or dispersion of a dataset.
- It is defined as the difference between the maximum and minimum values in a set of observations.

$$2, 3, 4, \cancel{5}, 8, 9, 32$$

↑ ↓
Min Max

$$\text{Max} - \text{Min}$$
$$32 - 2 = 30$$

Standard Deviation vs Variance

How much deviation has occurred from the mean value

- Variance is a measure of the spread or dispersion of a set of data points. It is calculated as the average of the squared differences from the mean.

$$6, 7, 8, \overset{9}{\cancel{9}}, 10, 11, 12 = \frac{6+7+8+9+10+11+12}{7} = 9$$

$$\sigma^2 = \frac{\sum_{i=1}^n (x_i - \bar{x})^2}{n}$$

$$\text{variance} = \sigma^2$$

$$\Rightarrow 9 = \frac{(6-9)^2 + (7-9)^2 + (8-9)^2 + (9-9)^2 + (10-9)^2}{7}$$

$$\sigma^2 = \frac{\sum_{i=1}^n (x_i - \bar{x})^2}{n}$$

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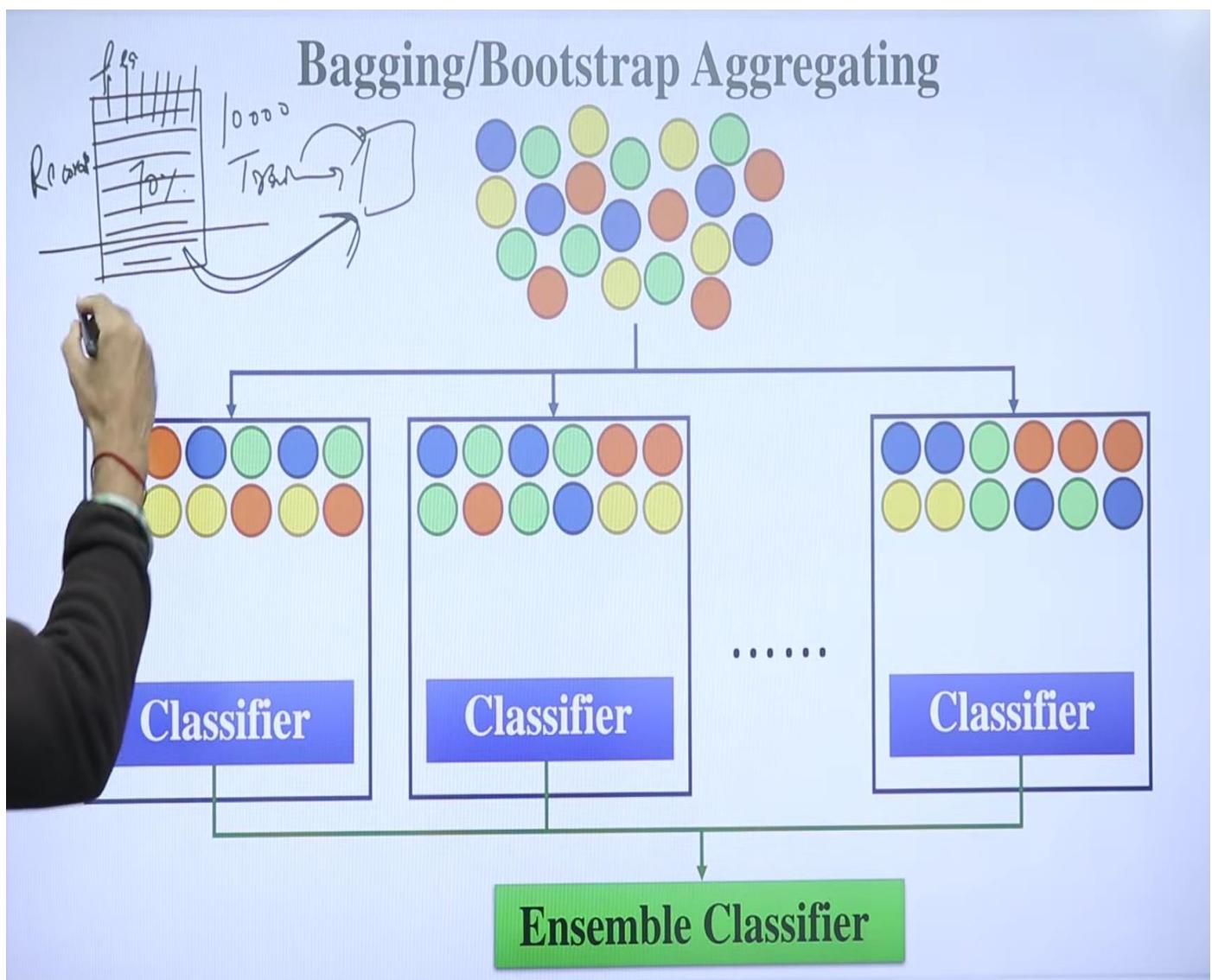
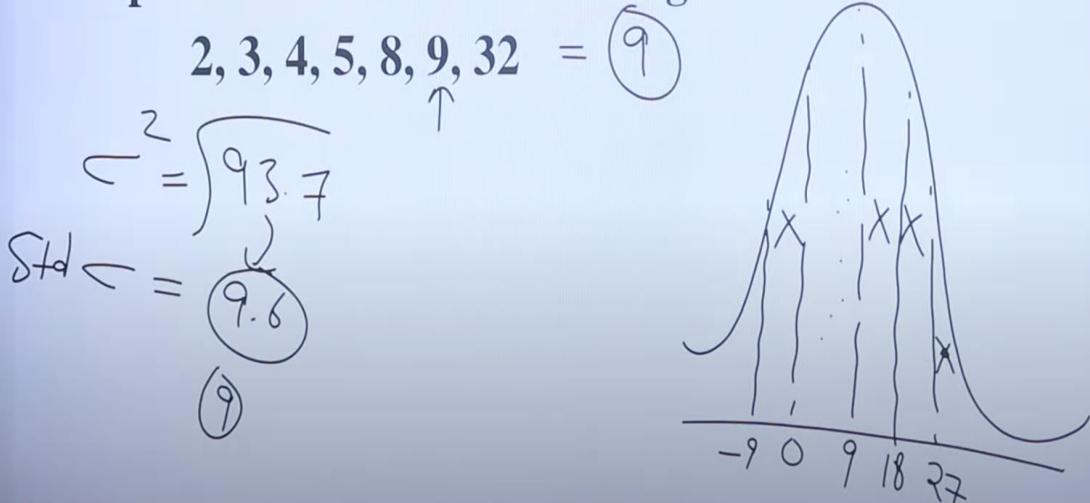
Standard Deviation vs Variance

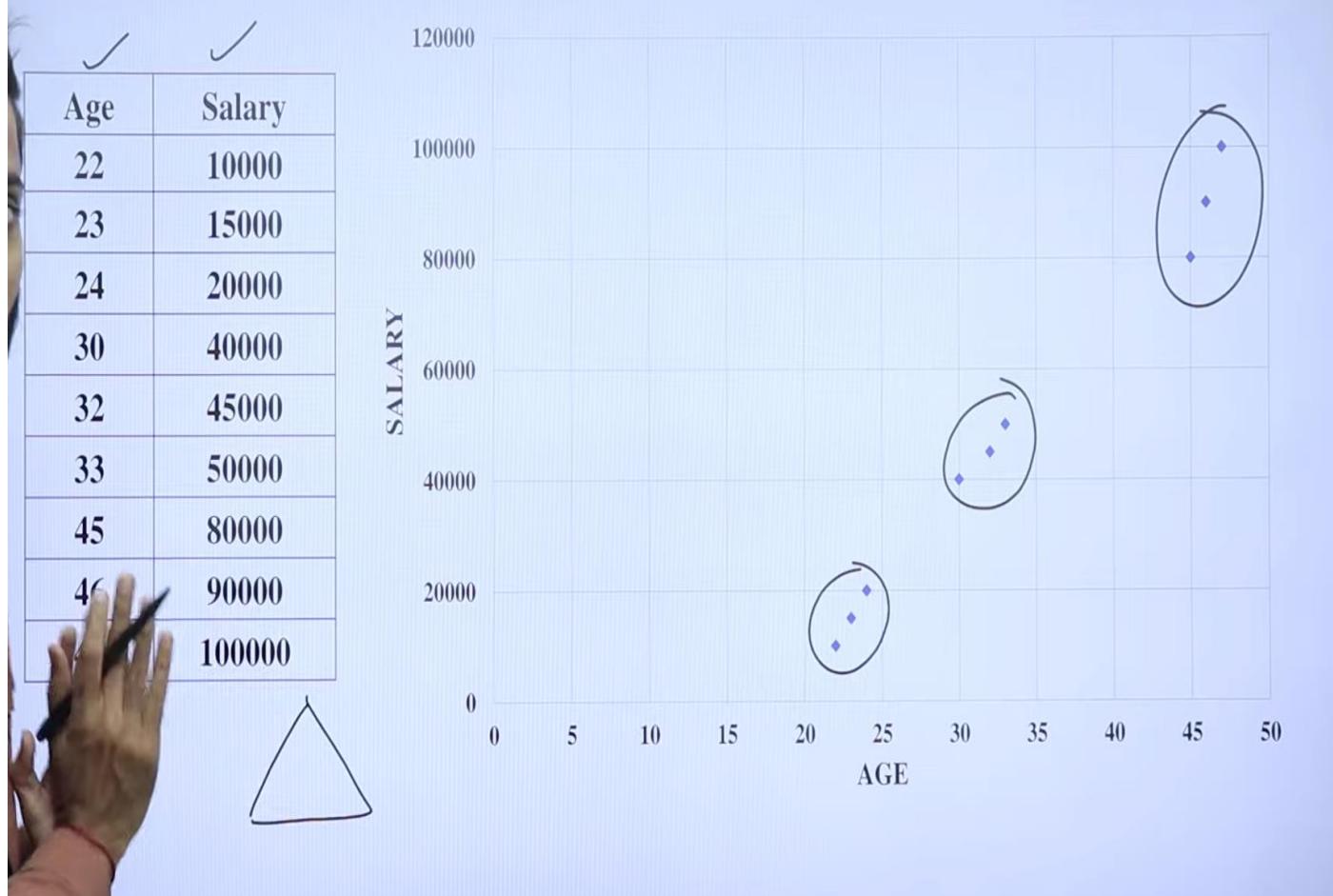
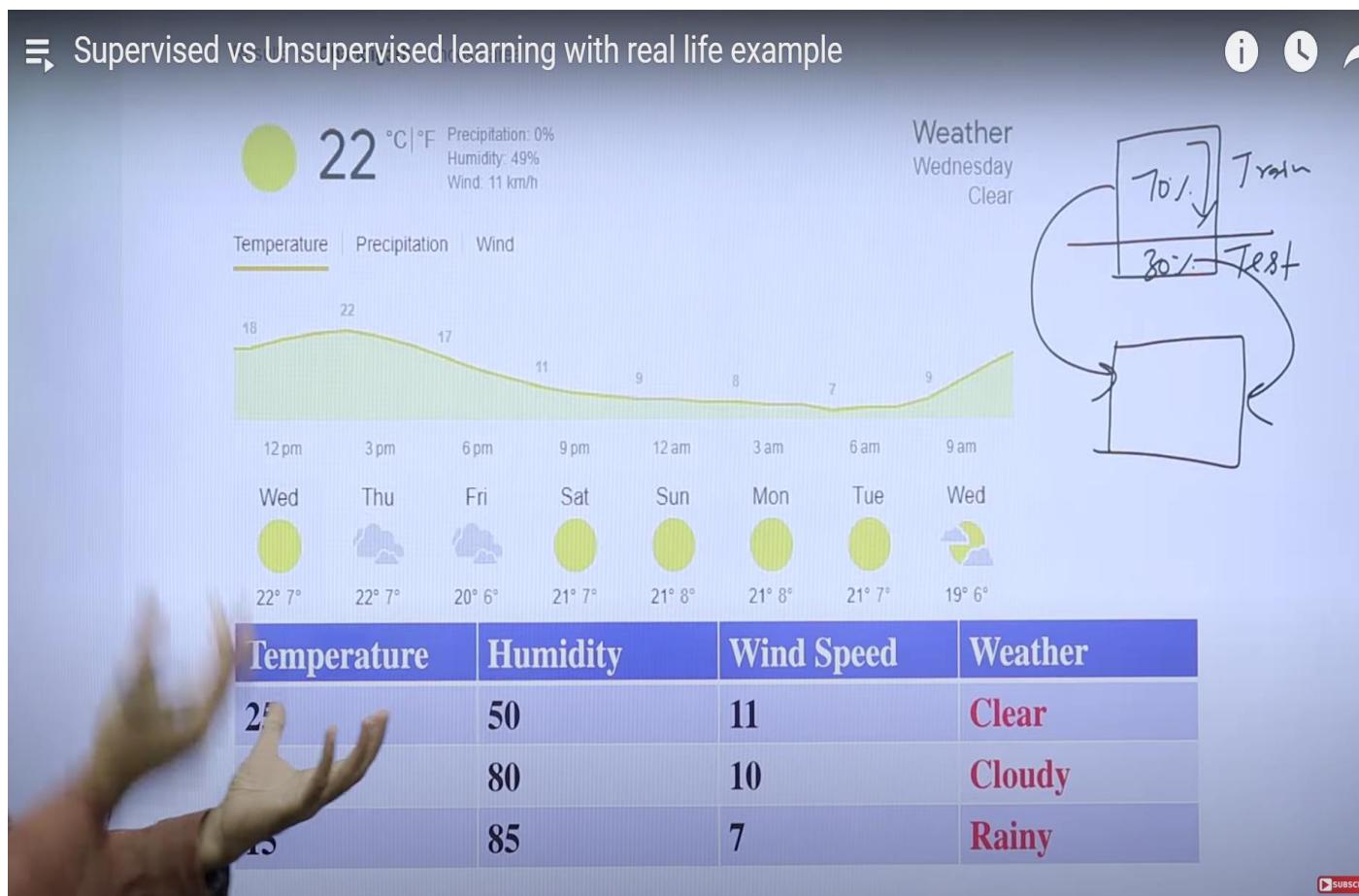
$$\text{Std.} = \sqrt{\sigma^2}$$

- Variance is a measure of the spread or dispersion of a set of data points. It is calculated as the average of the squared differences from the mean.

$$\begin{aligned} \text{Std.} &= \sqrt{\sigma^2} \\ \sigma^2 &= \frac{\sum_{i=1}^n (x_i - \bar{x})^2}{n} \\ &= \frac{(6-9)^2 + (7-9)^2 + (8-9)^2 + (9-9)^2 + (10-9)^2}{7} \\ &= \frac{9}{7} = \sigma^2 = 4 \end{aligned}$$

- A low standard deviation indicates that the values tend to be close to the mean (also called the expected value) of the set, while a high standard deviation indicates that the values are spread out over a wider range.





Supervised Learning		Unsupervised Learning
Classification	Regression	
Logistic Regression	Linear Regression	PCA
Naive Bayes	Ridge Regression	K-mean Clustering
Linear Discriminant Analysis (LDA)	Lasso Regression	Hierarchical Clustering
— Decision Trees		DB Scan Clustering
— Random Forest		
— Support Vector Machines (SVM)		
— k-Nearest Neighbors (KNN)		
Gradient Boosting algorithms		
Neural Networks		

Writing in Python

```

import statistics as stat
data = [2, 3, 4, 5, 8, 9, 32]
meanval = stat.mean(data)
med_val = stat.median(data)
mod_val = stat.mode(data)
var_val = stat.variance(data)
sd_val = stat.stdev(data)

```

$$\text{Range} = \max(\text{Data}) - \min(\text{Data})$$

Step1: Initialize Weights

Step2: Train Weak Learner 1

Step3: Calculate Total Error

Step4: Calculate Weak Learner Weight(α) = $\frac{1}{2} \ln\left(\frac{1 - \text{Total Error}}{\text{Total Error}}\right)$

Step5: Update Instance Weights (NW) = Old weight $\times e^{\alpha}$

Repeat from Step2...

Instance	Feature 1	Feature 2
1	1000	450
2	2000	475
3	3000	545
4	5000	756
5	6000	898

$$\frac{1}{2} \ln\left(\frac{1 - \frac{2}{5}}{\frac{2}{5}}\right) = \frac{3 \times 8}{2} / 1.5$$

$$\begin{aligned} \frac{1}{5} \times e^{-0.20} &= 0.16 \\ 0.16 &\quad 1/5 + 1/5 \\ 1/5 &= 2/5 \\ 1/5 &\rightarrow 1/5 \times e^{0.20} = 0.24 \\ 0.24 & \end{aligned}$$

$$\frac{1}{2} \ln(1.5)$$

Bagging	Boosting	Stacking

Two bags are there containing Red and black balls; first bag has 3 red and 2 black balls, second bag has 2 red and 3 black balls. One ball is drawn randomly. (Find the probability that it is Red ball?)

$$\begin{aligned} B_1 &\left[\begin{matrix} 3R \\ 2B \end{matrix} \right] \quad P(E) = \text{Red} = \frac{P(A) \times P(E/A)}{P(A) + P(B) \times P(E/B)} = \frac{\frac{1}{2} \times \frac{3}{5}}{\frac{1}{2} \times \frac{3}{5} + \frac{1}{2} \times \frac{2}{5}} \\ B_2 &\left[\begin{matrix} 2R \\ 3B \end{matrix} \right] \quad P(B) = \text{Bag 2 choose} = \frac{1}{2} \end{aligned}$$

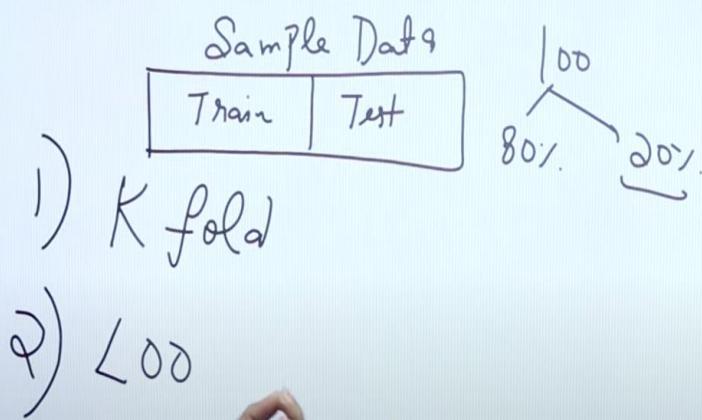
Without any biasing one bag is chosen from that one ball is chosen randomly which was Red. What is probability that it came from the second bag?

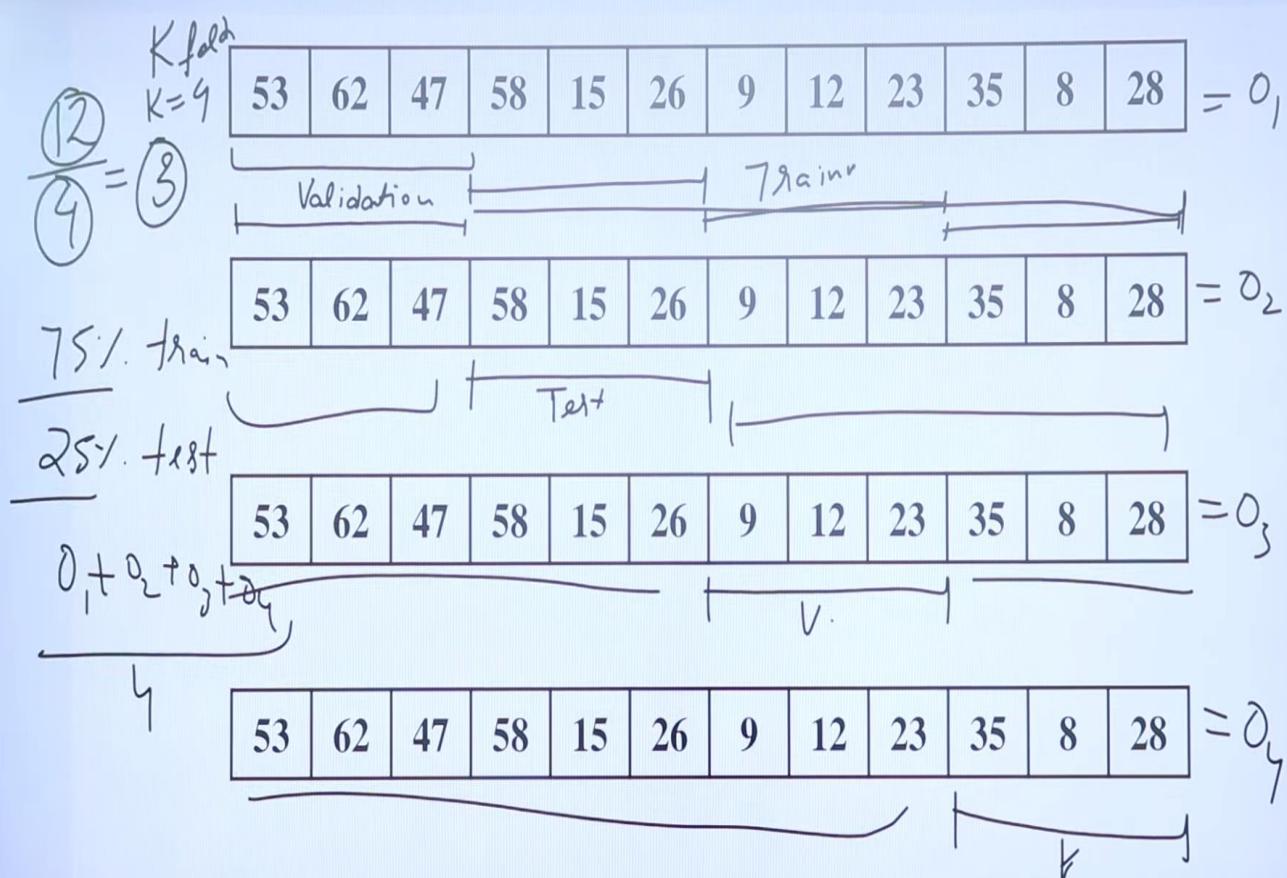
$$P(B/E) = \frac{P(B) \times P(E/B)}{\text{Total}} = \frac{\frac{1}{2} \times \frac{2}{5}}{\frac{1}{2} \times \frac{3}{5} + \frac{1}{2} \times \frac{2}{5}}$$

Cross Validation in Machine Learning with Examples

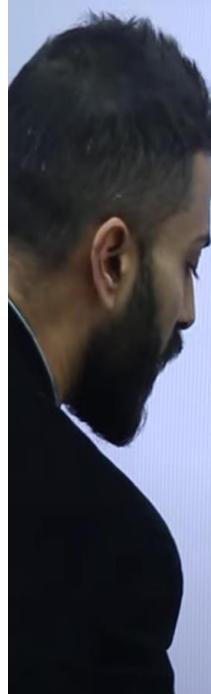


- Cross-validation is a resampling technique
- It helps in estimating how well the model will perform on an independent dataset.

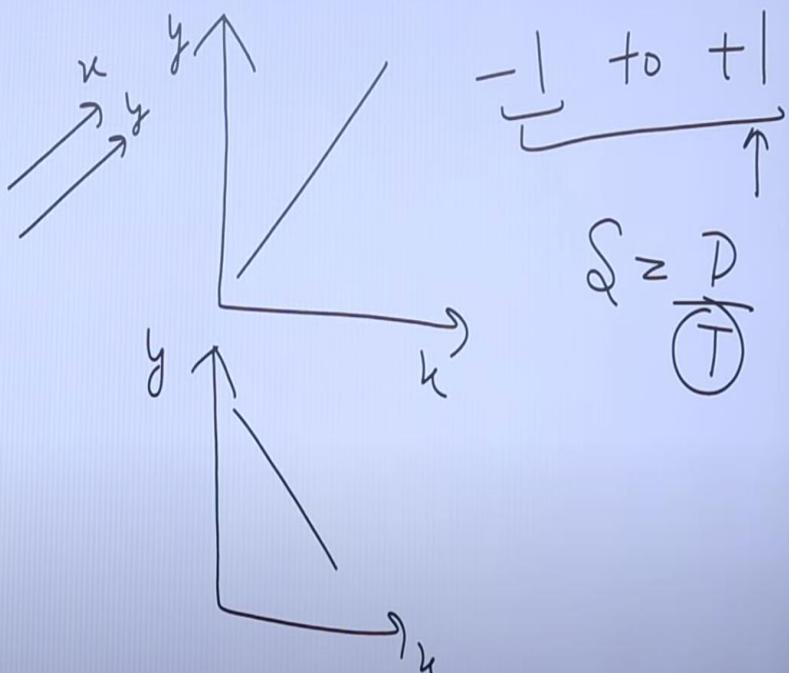




Pearson's Correlation Coefficient | Supervised Learning | Data Science & Machine Learning
The Pearson's correlation coefficient between x and y rounded to the first decimal point for the given data in below table is:



X	Y
-6	6.4
2	4.7
0.2	8
7	2
-4	3.4



$$\rho = \frac{\text{Cov}(X, Y)}{\sqrt{N} \sqrt{S_x^2 + S_y^2}}$$

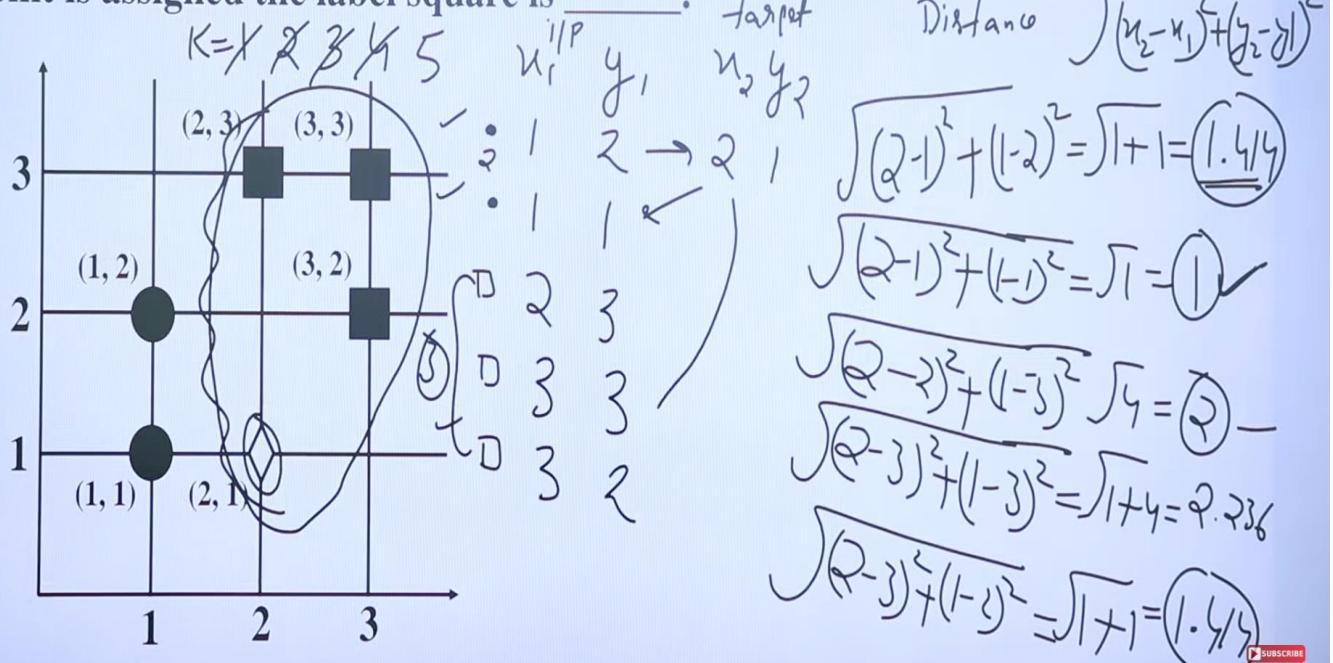
$$\text{Cov}(X, Y) = \frac{1}{n} \sum_{i=1}^n (x_i - \bar{x})(y_i - \bar{y})$$

$$S_x^2 = \frac{1}{n} \sum_{i=1}^n (x_i - \bar{x})^2$$

$$S_y^2 = \frac{1}{n} \sum_{i=1}^n (y_i - \bar{y})^2$$

X	Y	μ_x	μ_y	$x - \mu_x$	$y - \mu_y$	$(x - \mu_x)^*(y - \mu_y)$	$(x - \mu_x)^2$	$(y - \mu_y)^2$
-6	6.4	-0.16	4.9	-5.84	1.5	-8.76	34.1056	2.25
2	4.7			2.16	-0.2	-0.432	4.6656	0.04
0.2	8			0.36	3.1	1.116	0.1296	9.61
7	2			7.16	-2.9	-20.764	51.2656	8.41
-4	3.4			-3.84	-1.5	5.76	14.7456	2.25
						Total = -23.08	Total = 104.91	Total = 22.56
						Avg = -4.6	Avg = 20.98	Avg = 4.5

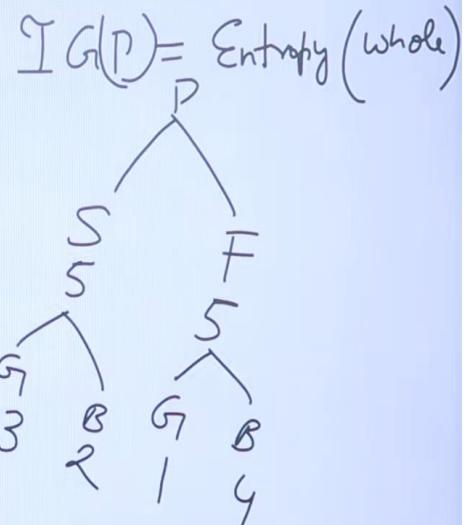
Given the two-dimensional dataset consisting of 5 data points from two classes (circles and squares) and assume that the Euclidean distance is used to measure the distance between two points. The minimum odd value of k in k -nearest neighbor algorithm for which the diamond (\diamond) shaped data point is assigned the label square is _____.



To develop such a model, the computed InformationGain(C, Pitch) with respect to the Target is _____ (rounded off to two decimal places).

Table C

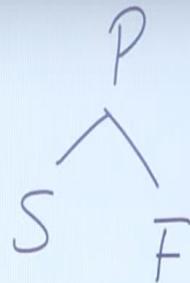
Match Number	Pitch	Format	Winner (Target)
1	- S ✓	T	<u>Green</u> ✓
2	- S	T	Blue
3	F	O	Blue
4	- S	O	Blue
5	F ✓	T	<u>Green</u>
	F	O	Blue
	- S	O	<u>Green</u>
8	F	T	Blue
9	F	O	Blue
10	- S	O	<u>Green</u>



Decision Tree Example | Calculate Entropy, Information Gain | Supervised Learning

- Step 1: Entropy of entire dataset

$$C\{4, 6\} = -\frac{4}{10} \log_2 \frac{4}{10} - \frac{6}{10} \log_2 \frac{6}{10} = 0.97$$



- Step 2: Entropy of all attributes in Pitch:

$$\text{Entropy of } \underline{\text{Spin}(S)} \{3, 2\} = -\frac{3}{5} \log_2 \frac{3}{5} - \frac{2}{5} \log_2 \frac{2}{5} = 0.97$$

$$\text{Entropy of } \underline{\text{Pace}(F)} \{1, 4\} = -\frac{1}{5} \log_2 \frac{1}{5} - \frac{4}{5} \log_2 \frac{4}{5} = 0.72$$

$$\text{Information Gain (C, Pitch)} = \text{Entropy}(C) - \frac{5}{10} \text{Ent}(S) - \frac{5}{10} \text{Ent}(F)$$

$$= 0.97 - 0.485 - 0.360$$

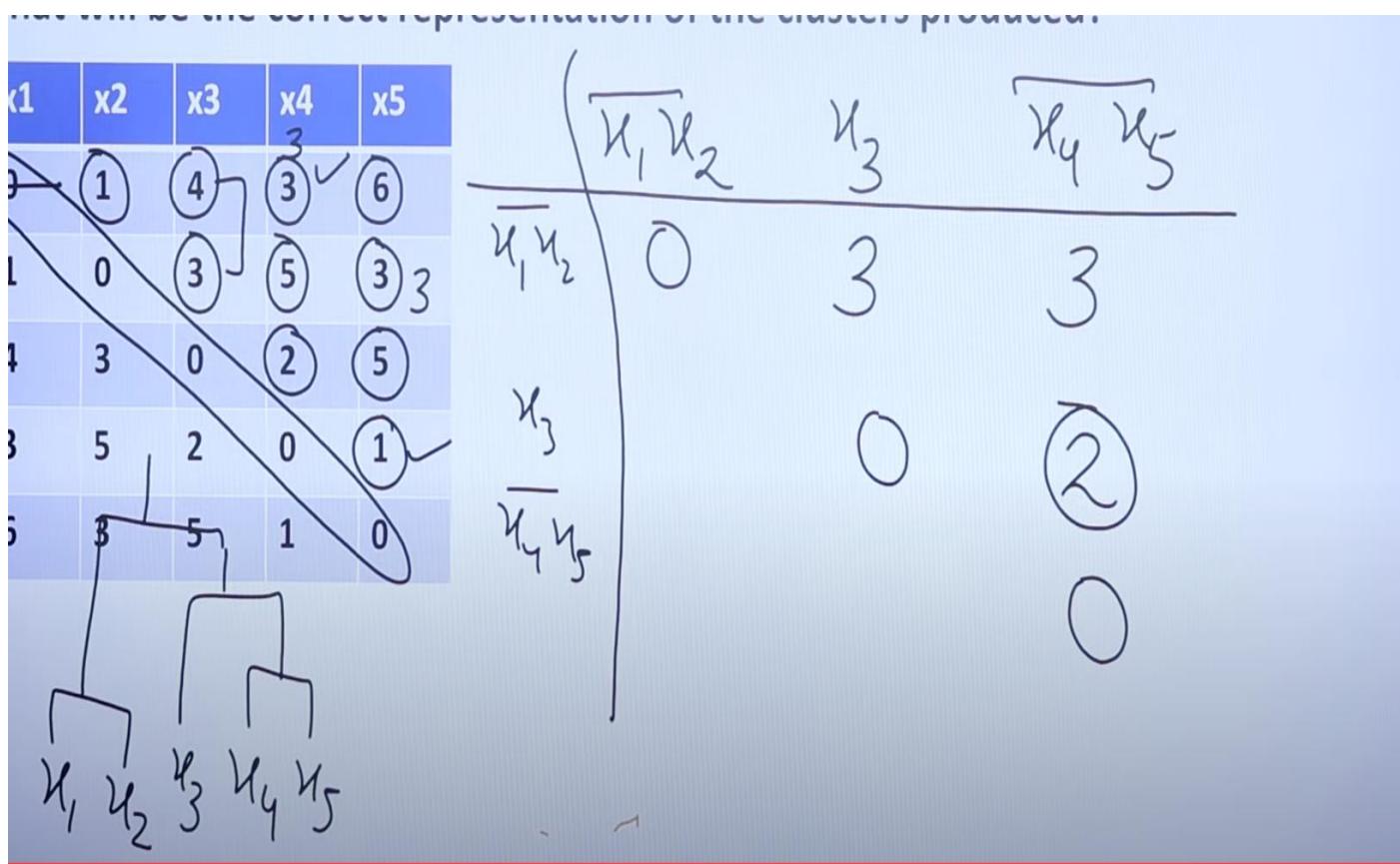
$$= 0.13$$

Single Linkage Clustering Example | Unsupervised Learning | Machine Learning

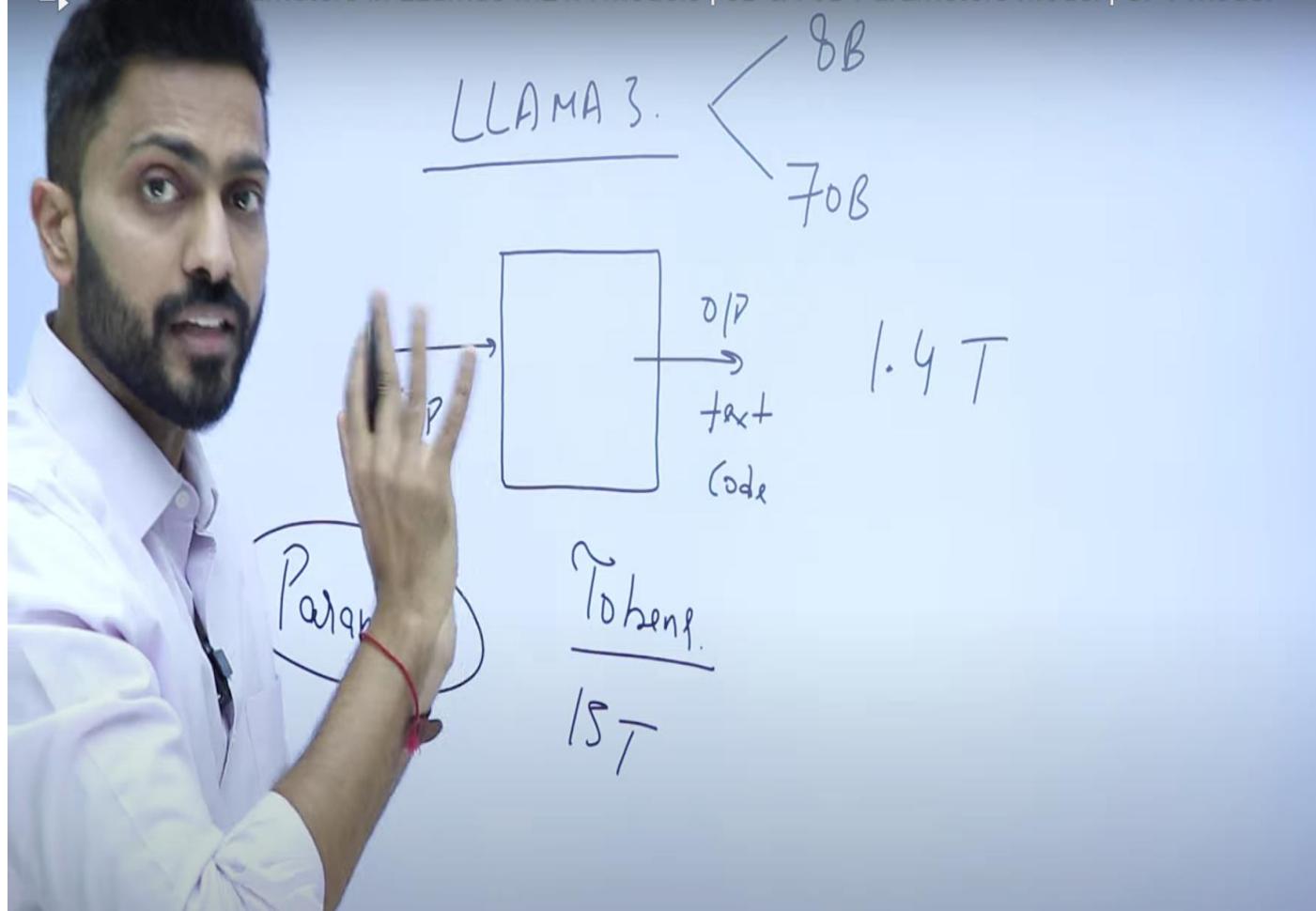


Consider the table below, where the (i, j) th element of the table is the distance between points x_i and x_j . Single linkage clustering is performed on data points, x_1, x_2, x_3, x_4, x_5 . What will be the correct representation of the clusters produced?

	x_1	x_2	x_3	x_4	x_5
x_1	0	1	4	3	6
x_2	1	0	3	5	3
x_3	4	3	0	2	5
x_4	3	5	2	0	1
x_5	6	3	5	1	0



→ Token & Parameters in LLaMA3 META Models | 8B & 70B Parameters Model | GPT model



Token vs Parameters

- Let's say we have a recipe for chocolate chip cookies.
- The ingredients (tokens) might include flour, sugar, butter, eggs, chocolate chips, etc.
- The instructions (parameters) tell us how to mix these ingredients together
- how long to bake the cookies, and at what temperature.
- Adjusting the amount of sugar or the baking time would be like changing the parameters of the recipe.