

Assignment 14

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Outline

1 Question

2 Solution

Question

Show that the weighted sample spectrum

$S_c(\omega) = \frac{1}{2T} \left| \int_{-T}^T c(t)x(t)e^{-j\omega t} dt \right|^2$ of process $x(t)$ is the Fourier Transformation of the function

$$R_c(\tau) = \int_{-T+|\tau/2|}^{T-|\tau/2|} c\left(t + \frac{\tau}{2}\right) c\left(t - \frac{\tau}{2}\right) x\left(t + \frac{\tau}{2}\right) x\left(t - \frac{\tau}{2}\right) dt \quad (1)$$

Solution

The Function

$$X_c(\omega) = \int_{-T}^T c(t)x(t)e^{-j\omega t} dt \quad (2)$$

is the Fourier Transformation of the product $c(t)x_T(t)$; where

$$x_T(t) = \begin{cases} 1 & |t| < T \\ 0 & |t| > T \end{cases}$$

Hence , the function $2T.S_T(\omega) = |X_c(\omega)|^2$ is the Fourier Transformation of

$$f(t) = c(t)x_T(t).c(-t)x_T(-t) \quad (3)$$

$$= \int_{-T+|t|/2}^{T-|t|/2} c\left(t + \frac{\tau}{2}\right)c\left(t - \frac{\tau}{2}\right)x\left(t + \frac{\tau}{2}\right)x\left(t - \frac{\tau}{2}\right) dt \quad (4)$$