

Decision Tree Algorithm:

| Outlook | Temperature | Humidity | Windy | Hours played |
|----------|-------------|-------------|-------|--------------|
| Rainy | hot | high | false | 25 |
| Rainy | hot | high | True | 30 |
| Overcast | mild | high | True | 52 |
| Sunny | mild | high | false | 45 |
| Sunny | cool | high Normal | false | 52 |
| Sunny | cool | normal | True | 23 |
| Overcast | cool | normal | True | 43 |
| Rainy | mild | high | false | 35 |
| Rainy | cool | Normal | false | 38 |
| Rainy | mild | Normal | True | 48 |
| Sunny | mild | Normal | false | 46 |
| Overcast | hot | high | false | 44 |
| Overcast | hot | Normal | false | 44 |
| Sunny | mild | high | True | 30 |

Termination criteria: $CV \leq 10\%$ $n \geq 4$

→ standard deviation of hours played: 9.32

calculation of standard deviation of feature columns:-

| outlook | Mean | std. deviation | count(n) |
|----------|-------|----------------|----------|
| Sunny | 39.2 | 10.87 | 5 |
| Rainy | 35.2 | 7.78 | 5 |
| Overcast | 46.25 | 3.49 | 4 |

$$SD(Outlook) = \frac{5}{14} \times 10.87 + \frac{5}{14} \times 7.78 + \frac{4}{14} \times 3.49 = 7.66$$

$$SDR = 1.66$$

| Temperature | Mean | std. deviation | count(n) |
|-------------|-------|----------------|----------|
| hot | 36.25 | 8.95 | 4 |
| cool | 39 | 10.51 | 4 |
| mild | 42.66 | 7.65 | 6 |

$$SD(temp) = \frac{4}{14} \times 8.95 + \frac{4}{14} \times 10.51 + \frac{6}{14} \times 7.65$$

$$= 8.84$$

$$SDR = 0.48$$

| Humidity | Mean | std. deviation | count(n) |
|----------|-------|----------------|----------|
| High | 37.57 | 9.36 | 7 |
| normal | 42 | 8.73 | 6 |

$$SD(Humidity) = \frac{7}{14} \times 9.36 + \frac{6}{14} \times 8.73 = 9.05$$

$$SDR = 0.27$$

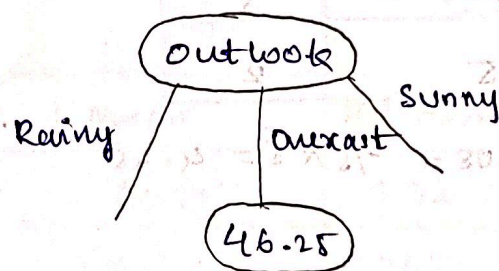
| Windy | Mean | std. deviation | Count (N) |
|-------|-------|----------------|-----------|
| True | 37.66 | 10.59 | 06 |
| false | 41.37 | 7.87 | 08 |

$$SD(windy) = \frac{6}{14} \times 10.59 + \frac{8}{14} \times 7.87 = 9.04$$

$$SDR = 0.28$$

→ outlook becomes root node (high SDR)

→ for outlook overcast $n \leq 4$ and $cvc = 10$, ∴ it will have a leaf node with output as mean of overcast's values i.e. 46.25



For outlook Rainy:-

| Temp. | Humidity | windy | hours played |
|-------|----------|------------|--------------|
| Hot | high | false | 25 |
| hot | high | false True | 30 |
| Mild | high | false | 35 |
| cool | Normal | false | 38 |
| mild | Normal | false | 48 |

$$SD(hours\ played) = 7.78$$

→ calculation of std. deviation to find the next node on Outlook Rainy,

| Temp. | mean. | std. dev | count(n) |
|-------|-------|----------|----------|
| hot | 27.5 | 2.5 | 02 |
| cool | 32 | 0 | 1 |
| mild | 41.5 | 6.5 | 2 |

$$SD(temp) = \frac{2}{5} \times 2.5 + \frac{1}{5} \times 0 + \frac{2}{5} \times 6.5 = 3.6$$

$$SDR = 4.18$$

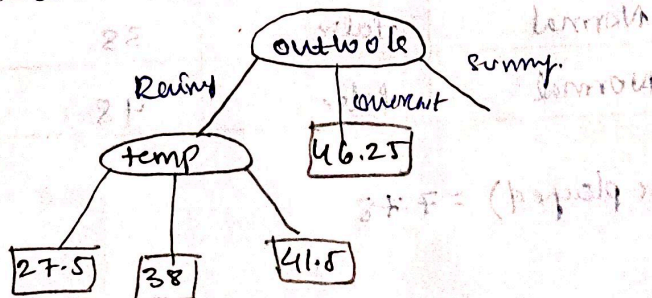
| humidity | Mean | std. deviation | count |
|----------|------|----------------|-------|
| high | 30 | 4.08 | 3 |
| Normal | 43 | 5 | 2 |

$$SD(humidity) = \frac{3}{5} \times 4.08 + \frac{2}{5} \times 5 = 4.45$$

$$SDR (= 3.33)$$

| Windy | mean | std. dev. | count(n) |
|-------|-------|-----------|----------|
| True | 39 | 9 | 2 |
| False | 32.66 | 5.56 | 3 |

→ temp. has highest SDR. it becomes the next node on the Rainy branch of outlook and the leaf node is added with mean value of each attribute.



For outlook sunny:-

| Temp. | humidity | windy | hours played |
|-------|----------|-------|--------------|
| mild | high | false | 45 |
| cool | Normal | false | 52 |
| cool | Normal | True | 23 |
| Mild | Normal | false | 46 |
| Mild | high | True | 30 |

$$SD(\text{hours played}) = 10.87.$$

→ Calculation of std. deviation to find the next node on outlook sunny.

| Temp. | Mean. | Std. deviation | Count |
|-------|-------|----------------|-------|
| mild | 40.33 | 7.32 | 3 |
| cool | 37.5 | 14.5 | 2 |

$$SD(\text{temp}) = 3/5 \times 7.32 + 2/5 \times 14.5 = 10.19$$

$$SDR = 0.68$$

| Humidity | Mean | Std. deviation | Count |
|----------|-------|----------------|-------|
| high | 37.5 | 7.5 | 2 |
| Normal | 40.33 | 12.5 | 3 |

$$SD(\text{humidity}) = 2/5 \times 7.5 + 3/5 \times 12.5 = 10.5$$

$$SDR = 0.37$$

| windy | Mean | std. dev. | Count |
|-------|-------|-----------|-------|
| True | 26.5 | 3.5 | 2 |
| False | 47.67 | 3.09 | 3 |

→ windy has highest SDR. it becomes root node on sunny branch and all the attributes satisfy the termination criteria.

∴ leaf node are added with mean values as o/p.

