```
import pandas as pd
import numpy as np

np.random.seed(1212)

import keras
from keras.models import Model
from keras.layers import *
from keras import optimizers
```

```
df_train = pd.read_csv('train.csv')
df_test = pd.read_csv('test.csv')
```

```
df_train.head()
```

```
label pixel0 pixel1 pixel2 pixel3 pixel4 pixel5 pixel6 pixel7 pixel8 ... pixel774 pixel775 pixel776 pixel777 p
              0
                                                                                        0.0
                                                                                                 0.0
                                                                                                           0.0
                                                                                                                    0.0
              0
                                            0
                                                    0
                                                            0
                                                                   0
                                                                                        0.0
                                                                                                 0.0
                                                                                                           0.0
                                                                                                                    0.0
1
                                     0
                                                                           0
                                                            0
                                                                                        0.0
                                                                                                 0.0
                                                                                                           0.0
                                                                                                                    0.0
              0
                     0
                             0
                                     0
                                            0
                                                    0
                                                            0
                                                                   0
                                                                                        0.0
                                                                                                 0.0
                                                                                                           0.0
                                                                                                                    0.0
                                                            0
                                                                                        0.0
                                                                                                 0.0
                                                                                                           0.0
                                                                                                                    0.0
```

5 rows × 785 columns

```
df_features = df_train.iloc[:, 1:785]
df_label = df_train.iloc[:, 0]

X_test = df_test.iloc[:, 0:784]

print(X_test.shape)
print(X_train.shape)
print(X_cv.shape)
```

```
(12638, 784)
(7336, 784)
(1834, 784)
```

```
from sklearn.model_selection import train_test_split
       X train, X cv, y train, y cv = train test split(df features, df label,
                                                            test size = 0.2,
                                                            random_state = 1212)
       X_train = X_train.to_numpy().reshape(7336, 784)
       X \text{ cv} = X \text{ cv.to numpy().reshape(1834, 784)}
       X_test = X_test.to_numpy().reshape(12638, 784)
       print((min(X_train[1]), max(X_train[1])))
       (0.0, 254.0)
X_train = X_train.astype('float32'); X_cv= X_cv.astype('float32'); X_test = X_test.astype('float32')
X_train /= 255; X_cv /= 255; X_test /= 255
# Convert labels to One Hot Encoded
num_digits = 10
y train = keras.utils.to categorical(y train, num digits)
y_cv = keras.utils.to_categorical(y_cv, num_digits)
print(y_train[0])
print(y_train[3])
       [0. 1. 0. 0. 0. 0. 0. 0. 0. 0.]
       [0. 0. 1. 0. 0. 0. 0. 0. 0. 0.]
       n input = 784
       n_hidden_1 = 300
       n hidden 2 = 100
       n_hidden_3 = 100
       n \text{ hidden } 4 = 200
       num_digits = 10
       Inp = Input(shape=(784,))
       x = Dense(n_hidden_1, activation='relu', name = "Hidden_Layer_1")(Inp)
       x = Dense(n_hidden_2, activation='relu', name = "Hidden_Layer_2")(x)
       x = Dense(n_hidden_3, activation='relu', name = "Hidden_Layer_3")(x)
       x = Dense(n_hidden_4, activation='relu', name = "Hidden_Layer_4")(x)
```

output = Dense(num_digits, activation='softmax', name = "Output_Layer")(x)

```
model = Model(Inp, output)
model.summary()
```

Model: "model"

Layer (type)	Output Shape	Param #
input_1 (InputLayer)	[(None, 784)]	0
Hidden_Layer_1 (Dense)	(None, 300)	235500
Hidden_Layer_2 (Dense)	(None, 100)	30100
Hidden_Layer_3 (Dense)	(None, 100)	10100
Hidden_Layer_4 (Dense)	(None, 200)	20200
Output_Layer (Dense)	(None, 10)	2010

Total params: 297,910 Trainable params: 297,910 Non-trainable params: 0

```
Epoch 1/20
74/74 - 1s - loss: nan - accuracy: 0.1010 - val_loss: nan - val_accuracy: 0.0911 - 1s/epoch - 20ms/step
Epoch 2/20
74/74 - 0s - loss: nan - accuracy: 0.1022 - val loss: nan - val accuracy: 0.0911 - 489ms/epoch - 7ms/step
Epoch 3/20
74/74 - 0s - loss: nan - accuracy: 0.1022 - val loss: nan - val accuracy: 0.0911 - 463ms/epoch - 6ms/step
Epoch 4/20
74/74 - 0s - loss: nan - accuracy: 0.1022 - val loss: nan - val accuracy: 0.0911 - 461ms/epoch - 6ms/step
Epoch 5/20
74/74 - 1s - loss: nan - accuracy: 0.1022 - val loss: nan - val accuracy: 0.0911 - 507ms/epoch - 7ms/step
Epoch 6/20
74/74 - 1s - loss: nan - accuracy: 0.1022 - val loss: nan - val accuracy: 0.0911 - 564ms/epoch - 8ms/step
Epoch 7/20
74/74 - 0s - loss: nan - accuracy: 0.1022 - val loss: nan - val accuracy: 0.0911 - 489ms/epoch - 7ms/step
Epoch 8/20
74/74 - 0s - loss: nan - accuracy: 0.1022 - val_loss: nan - val_accuracy: 0.0911 - 498ms/epoch - 7ms/step
Epoch 9/20
74/74 - 1s - loss: nan - accuracy: 0.1022 - val_loss: nan - val_accuracy: 0.0911 - 506ms/epoch - 7ms/step
Epoch 10/20
74/74 - 0s - loss: nan - accuracy: 0.1022 - val_loss: nan - val_accuracy: 0.0911 - 477ms/epoch - 6ms/step
Epoch 11/20
74/74 - 1s - loss: nan - accuracy: 0.1022 - val loss: nan - val accuracy: 0.0911 - 591ms/epoch - 8ms/step
Epoch 12/20
74/74 - 0s - loss: nan - accuracy: 0.1022 - val_loss: nan - val_accuracy: 0.0911 - 453ms/epoch - 6ms/step
Epoch 13/20
74/74 - 0s - loss: nan - accuracy: 0.1022 - val loss: nan - val accuracy: 0.0911 - 491ms/epoch - 7ms/step
Epoch 14/20
74/74 - 1s - loss: nan - accuracy: 0.1022 - val_loss: nan - val_accuracy: 0.0911 - 601ms/epoch - 8ms/step
Epoch 15/20
74/74 - 1s - loss: nan - accuracy: 0.1022 - val loss: nan - val accuracy: 0.0911 - 803ms/epoch - 11ms/step
Epoch 16/20
74/74 - 1s - loss: nan - accuracy: 0.1022 - val loss: nan - val accuracy: 0.0911 - 836ms/epoch - 11ms/step
Epoch 17/20
74/74 - 1s - loss: nan - accuracy: 0.1022 - val_loss: nan - val_accuracy: 0.0911 - 755ms/epoch - 10ms/step
Epoch 18/20
74/74 - 0s - loss: nan - accuracy: 0.1022 - val_loss: nan - val_accuracy: 0.0911 - 499ms/epoch - 7ms/step
Epoch 19/20
74/74 - 0s - loss: nan - accuracy: 0.1022 - val_loss: nan - val_accuracy: 0.0911 - 474ms/epoch - 6ms/step
Epoch 20/20
74/74 - 0s - loss: nan - accuracy: 0.1022 - val_loss: nan - val_accuracy: 0.0911 - 471ms/epoch - 6ms/step
```

/usr/local/lib/python3.10/dist-packages/keras/optimizers/legacy/adam.py:117: UserWarning: The `lr` argument is deprecated, use super().__init__(name, **kwargs)

```
history2 = model2.fit(X_train, y_train,

batch_size = batch_size,

epochs = training_epochs,

verbose = 2,

validation_data=(X_cv, y_cv))
```

```
Epoch 1/20
74/74 - 2s - loss: nan - accuracy: 0.6366 - val loss: nan - val accuracy: 0.0911 - 2s/epoch - 24ms/step
Epoch 2/20
74/74 - 1s - loss: nan - accuracy: 0.1022 - val loss: nan - val accuracy: 0.0911 - 560ms/epoch - 8ms/step
Epoch 3/20
74/74 - 1s - loss: nan - accuracy: 0.1022 - val loss: nan - val accuracy: 0.0911 - 593ms/epoch - 8ms/step
Epoch 4/20
74/74 - 1s - loss: nan - accuracy: 0.1022 - val_loss: nan - val_accuracy: 0.0911 - 591ms/epoch - 8ms/step
Epoch 5/20
74/74 - 1s - loss: nan - accuracy: 0.1022 - val_loss: nan - val_accuracy: 0.0911 - 577ms/epoch - 8ms/step
Epoch 6/20
74/74 - 1s - loss: nan - accuracy: 0.1022 - val_loss: nan - val_accuracy: 0.0911 - 864ms/epoch - 12ms/step
Epoch 7/20
74/74 - 1s - loss: nan - accuracy: 0.1022 - val_loss: nan - val_accuracy: 0.0911 - 975ms/epoch - 13ms/step
Epoch 8/20
74/74 - 1s - loss: nan - accuracy: 0.1022 - val_loss: nan - val_accuracy: 0.0911 - 1s/epoch - 14ms/step
Epoch 9/20
74/74 - 1s - loss: nan - accuracy: 0.1022 - val_loss: nan - val_accuracy: 0.0911 - 597ms/epoch - 8ms/step
Epoch 10/20
74/74 - 1s - loss: nan - accuracy: 0.1022 - val_loss: nan - val_accuracy: 0.0911 - 573ms/epoch - 8ms/step
Epoch 11/20
74/74 - 1s - loss: nan - accuracy: 0.1022 - val loss: nan - val accuracy: 0.0911 - 587ms/epoch - 8ms/step
Epoch 12/20
74/74 - 1s - loss: nan - accuracy: 0.1022 - val_loss: nan - val_accuracy: 0.0911 - 567ms/epoch - 8ms/step
Epoch 13/20
74/74 - 1s - loss: nan - accuracy: 0.1022 - val_loss: nan - val_accuracy: 0.0911 - 558ms/epoch - 8ms/step
Epoch 14/20
74/74 - 1s - loss: nan - accuracy: 0.1022 - val_loss: nan - val_accuracy: 0.0911 - 529ms/epoch - 7ms/step
Epoch 15/20
74/74 - 1s - loss: nan - accuracy: 0.1022 - val_loss: nan - val_accuracy: 0.0911 - 574ms/epoch - 8ms/step
Epoch 16/20
74/74 - 1s - loss: nan - accuracy: 0.1022 - val_loss: nan - val_accuracy: 0.0911 - 542ms/epoch - 7ms/step
Epoch 17/20
74/74 - 1s - loss: nan - accuracy: 0.1022 - val_loss: nan - val_accuracy: 0.0911 - 575ms/epoch - 8ms/step
Epoch 18/20
74/74 - 1s - loss: nan - accuracy: 0.1022 - val_loss: nan - val_accuracy: 0.0911 - 573ms/epoch - 8ms/step
Epoch 19/20
74/74 - 1s - loss: nan - accuracy: 0.1022 - val loss: nan - val accuracy: 0.0911 - 544ms/epoch - 7ms/step
Epoch 20/20
74/74 - 1s - loss: nan - accuracy: 0.1022 - val_loss: nan - val_accuracy: 0.0911 - 552ms/epoch - 7ms/step
```

```
Epoch 1/20
74/74 - 3s - loss: nan - accuracy: 0.6411 - val_loss: nan - val_accuracy: 0.0911 - 3s/epoch - 40ms/step
Epoch 2/20
74/74 - 1s - loss: nan - accuracy: 0.1022 - val loss: nan - val accuracy: 0.0911 - 673ms/epoch - 9ms/step
Epoch 3/20
74/74 - 1s - loss: nan - accuracy: 0.1022 - val loss: nan - val accuracy: 0.0911 - 683ms/epoch - 9ms/step
Epoch 4/20
74/74 - 1s - loss: nan - accuracy: 0.1022 - val_loss: nan - val_accuracy: 0.0911 - 806ms/epoch - 11ms/step
Epoch 5/20
74/74 - 1s - loss: nan - accuracy: 0.1022 - val_loss: nan - val_accuracy: 0.0911 - 1s/epoch - 14ms/step
Epoch 6/20
74/74 - 1s - loss: nan - accuracy: 0.1022 - val loss: nan - val accuracy: 0.0911 - 1s/epoch - 15ms/step
Epoch 7/20
74/74 - 1s - loss: nan - accuracy: 0.1022 - val_loss: nan - val_accuracy: 0.0911 - 751ms/epoch - 10ms/step
Epoch 8/20
74/74 - 1s - loss: nan - accuracy: 0.1022 - val_loss: nan - val_accuracy: 0.0911 - 680ms/epoch - 9ms/step
Epoch 9/20
74/74 - 1s - loss: nan - accuracy: 0.1022 - val_loss: nan - val_accuracy: 0.0911 - 767ms/epoch - 10ms/step
Epoch 10/20
74/74 - 1s - loss: nan - accuracy: 0.1022 - val loss: nan - val accuracy: 0.0911 - 725ms/epoch - 10ms/step
Epoch 11/20
74/74 - 1s - loss: nan - accuracy: 0.1022 - val loss: nan - val accuracy: 0.0911 - 685ms/epoch - 9ms/step
```

```
Epoch 12/20
74/74 - 1s - loss: nan - accuracy: 0.1022 - val_loss: nan - val_accuracy: 0.0911 - 664ms/epoch - 9ms/step
Epoch 13/20
74/74 - 1s - loss: nan - accuracy: 0.1022 - val loss: nan - val accuracy: 0.0911 - 731ms/epoch - 10ms/step
Epoch 14/20
74/74 - 1s - loss: nan - accuracy: 0.1022 - val_loss: nan - val_accuracy: 0.0911 - 742ms/epoch - 10ms/step
Fnoch 15/20
74/74 - 1s - loss: nan - accuracy: 0.1022 - val loss: nan - val accuracy: 0.0911 - 671ms/epoch - 9ms/step
Epoch 16/20
74/74 - 1s - loss: nan - accuracy: 0.1022 - val_loss: nan - val_accuracy: 0.0911 - 638ms/epoch - 9ms/step
Epoch 17/20
74/74 - 1s - loss: nan - accuracy: 0.1022 - val loss: nan - val accuracy: 0.0911 - 650ms/epoch - 9ms/step
Epoch 18/20
74/74 - 1s - loss: nan - accuracy: 0.1022 - val_loss: nan - val_accuracy: 0.0911 - 714ms/epoch - 10ms/step
Epoch 19/20
74/74 - 1s - loss: nan - accuracy: 0.1022 - val loss: nan - val accuracy: 0.0911 - 660ms/epoch - 9ms/step
Epoch 20/20
74/74 - 1s - loss: nan - accuracy: 0.1022 - val_loss: nan - val_accuracy: 0.0911 - 719ms/epoch - 10ms/step
Inp = Input(shape=(784,))
x = Dense(n_hidden_1, activation='relu', name = "Hidden_Layer_1")(Inp)
x = Dense(n_hidden_2, activation='relu', name = "Hidden_Layer_2")(x)
x = Dense(n hidden 3, activation='relu', name = "Hidden Layer 3")(x)
x = Dense(n hidden 4, activation='relu', name = "Hidden Layer 4")(x)
output = Dense(num_digits, activation='softmax', name = "Output_Layer")(x)
learning rate = 0.5
adam = keras.optimizers.Adam(lr=learning rate)
model2b = Model(Inp, output)
```

```
Epoch 1/20
74/74 [============ ] - 3s 13ms/step - loss: nan - accuracy: 0.5564 - val loss: nan - val accuracy: 0.0911
Epoch 2/20
74/74 [=============] - 1s 10ms/step - loss: nan - accuracy: 0.1022 - val_loss: nan - val_accuracy: 0.0911
Epoch 3/20
Epoch 4/20
74/74 [====
           ======== ] - 1s 10ms/step - loss: nan - accuracy: 0.1022 - val loss: nan - val accuracy: 0.0911
Epoch 5/20
74/74 [=====
         ========== ] - 1s 11ms/step - loss: nan - accuracy: 0.1022 - val loss: nan - val accuracy: 0.0911
Epoch 6/20
Epoch 7/20
74/74 [=================== ] - 1s 11ms/step - loss: nan - accuracy: 0.1022 - val_loss: nan - val_accuracy: 0.0911
Epoch 8/20
74/74 [========================== ] - 1s 10ms/step - loss: nan - accuracy: 0.1022 - val_loss: nan - val_accuracy: 0.0911
Epoch 9/20
74/74 [=====
         ========== ] - 1s 11ms/step - loss: nan - accuracy: 0.1022 - val loss: nan - val accuracy: 0.0911
Epoch 10/20
Epoch 11/20
Epoch 12/20
74/74 [=============] - 1s 16ms/step - loss: nan - accuracy: 0.1022 - val_loss: nan - val_accuracy: 0.0911
Epoch 13/20
Epoch 14/20
Epoch 15/20
74/74 [=====
           ============== ] - 1s 10ms/step - loss: nan - accuracy: 0.1022 - val loss: nan - val accuracy: 0.0911
Epoch 16/20
Epoch 17/20
74/74 [================== ] - 1s 11ms/step - loss: nan - accuracy: 0.1022 - val_loss: nan - val_accuracy: 0.0911
Epoch 18/20
74/74 [============] - 1s 10ms/step - loss: nan - accuracy: 0.1022 - val loss: nan - val accuracy: 0.0911
Epoch 19/20
74/74 [=====
         ==========] - 1s 10ms/step - loss: nan - accuracy: 0.1022 - val_loss: nan - val_accuracy: 0.0911
Epoch 20/20
n input = 784
n hidden 1 = 300
n \text{ hidden } 2 = 100
n \text{ hidden } 3 = 100
n hidden 4 = 100
n \text{ hidden } 5 = 200
num digits = 10
Inp = Input(shape=(784,))
x = Dense(n hidden 1, activation='relu', name = "Hidden Layer 1")(Inp)
x = Dense(n hidden 2, activation='relu', name = "Hidden Layer 2")(x)
x = Dense(n_hidden_3, activation='relu', name = "Hidden_Layer_3")(x)
x = Dense(n hidden 4, activation='relu', name = "Hidden Layer 4")(x)
```

x = Dense(n hidden 5, activation='relu', name = "Hidden Layer 5")(x)

output = Dense(num digits, activation='softmax', name = "Output Layer")(x)

```
model3 = Model(Inp, output)
model3.summary()
```

Model: "model_4"

Layer (type)	Output Shape	Param #
input_5 (InputLayer)	[(None, 784)]	0
Hidden_Layer_1 (Dense)	(None, 300)	235500
Hidden_Layer_2 (Dense)	(None, 100)	30100
Hidden_Layer_3 (Dense)	(None, 100)	10100
Hidden_Layer_4 (Dense)	(None, 100)	10100
Hidden_Layer_5 (Dense)	(None, 200)	20200
Output_Layer (Dense)	(None, 10)	2010

Total params: 308,010 Trainable params: 308,010 Non-trainable params: 0

```
Epoch 1/20
Fnoch 2/20
Epoch 3/20
Epoch 4/20
74/74 [====
       =========] - 1s 11ms/step - loss: nan - accuracy: 0.1022 - val_loss: nan - val_accuracy: 0.0911
Epoch 5/20
Epoch 6/20
Epoch 7/20
Fnoch 8/20
Epoch 9/20
Epoch 10/20
74/74 [=====
        ========] - 1s 11ms/step - loss: nan - accuracy: 0.1022 - val loss: nan - val accuracy: 0.0911
Epoch 11/20
Epoch 12/20
74/74 [==============] - 1s 10ms/step - loss: nan - accuracy: 0.1022 - val_loss: nan - val_accuracy: 0.0911
Epoch 13/20
74/74 [=====
       =============== ] - 1s 11ms/step - loss: nan - accuracy: 0.1022 - val loss: nan - val accuracy: 0.0911
Epoch 14/20
Epoch 15/20
74/74 [=====
      =============== ] - 1s 15ms/step - loss: nan - accuracy: 0.1022 - val_loss: nan - val_accuracy: 0.0911
Epoch 16/20
         ======== ] - 1s 17ms/step - loss: nan - accuracy: 0.1022 - val loss: nan - val accuracy: 0.0911
74/74 [=====
Epoch 17/20
74/74 [===========] - 1s 13ms/step - loss: nan - accuracy: 0.1022 - val_loss: nan - val_accuracy: 0.0911
Epoch 18/20
Epoch 19/20
Epoch 20/20
n input = 784
n \text{ hidden } 1 = 300
n \text{ hidden } 2 = 100
n \text{ hidden } 3 = 100
n \text{ hidden } 4 = 200
num_digits = 10
Inp = Input(shape=(784,))
x = Dense(n hidden 1, activation='relu', name = "Hidden Layer 1")(Inp)
x = Dropout(0.3)(x)
x = Dense(n hidden 2, activation='relu', name = "Hidden Layer 2")(x)
x = Dropout(0.3)(x)
x = Dense(n_hidden_3, activation='relu', name = "Hidden_Layer_3")(x)
x = Dropout(0.3)(x)
x = Dense(n_hidden_4, activation='relu', name = "Hidden_Layer_4")(x)
```

output = Dense(num_digits, activation='softmax', name = "Output_Layer")(x)

model4 = Model(Inp, output) model4.summary()

Model: "model 5"

Layer (type)	Output Shape	Param #
input_6 (InputLayer)	[(None, 784)]	0
Hidden_Layer_1 (Dense)	(None, 300)	235500
dropout (Dropout)	(None, 300)	0
Hidden_Layer_2 (Dense)	(None, 100)	30100
dropout_1 (Dropout)	(None, 100)	0
Hidden_Layer_3 (Dense)	(None, 100)	10100
dropout_2 (Dropout)	(None, 100)	0
Hidden_Layer_4 (Dense)	(None, 200)	20200
Output_Layer (Dense)	(None, 10)	2010
1		

Total params: 297,910 Trainable params: 297,910 Non-trainable params: 0

```
Epoch 1/20
74/74 [====
     Epoch 2/20
    74/74 [======
Epoch 3/20
74/74 [=====
    Epoch 4/20
Epoch 5/20
74/74 [=====
    =============== | - 1s 11ms/step - loss: nan - accuracy: 0.1022 - val loss: nan - val accuracy: 0.0911
Epoch 6/20
Epoch 7/20
74/74 [====
     Epoch 8/20
Epoch 9/20
74/74 [=============] - 1s 12ms/step - loss: nan - accuracy: 0.1022 - val_loss: nan - val_accuracy: 0.0911
Epoch 10/20
74/74 [=============] - 1s 14ms/step - loss: nan - accuracy: 0.1022 - val loss: nan - val accuracy: 0.0911
Fnoch 11/20
74/74 [===========] - 1s 17ms/step - loss: nan - accuracy: 0.1022 - val_loss: nan - val_accuracy: 0.0911
Epoch 12/20
Epoch 13/20
74/74 [=============] - 1s 11ms/step - loss: nan - accuracy: 0.1022 - val_loss: nan - val_accuracy: 0.0911
Epoch 14/20
Epoch 15/20
Epoch 16/20
Epoch 17/20
Epoch 18/20
Epoch 19/20
Epoch 20/20
```

```
test_pred = pd.DataFrame(model4.predict(X_test, batch_size=200))
test_pred = pd.DataFrame(test_pred.idxmax(axis = 1))
test_pred.index.name = 'ImageId'
test_pred = test_pred.rename(columns = {0: 'Label'}).reset_index()
test_pred['ImageId'] = test_pred['ImageId'] + 1
test_pred.head()
```

ImageId Label 0 1 NaN 1 2 NaN 2 3 NaN 3 4 NaN 4 5 NaN