

Pre-Covid Forecasting

Library

```
library(fpp3)

## Warning: package 'fpp3' was built under R version 4.0.5

## -- Attaching packages ----- fpp3 0.4.0 --

## v tibble      3.1.4      v tsibble      1.0.1
## v dplyr       1.0.7      v tsibbledata 0.3.0
## v tidyr       1.1.4      v feasts      0.2.2
## v lubridate   1.7.10     v fable       0.3.1
## v ggplot2     3.3.5

## Warning: package 'tibble' was built under R version 4.0.5

## Warning: package 'dplyr' was built under R version 4.0.5

## Warning: package 'tidyr' was built under R version 4.0.5

## Warning: package 'lubridate' was built under R version 4.0.5

## Warning: package 'ggplot2' was built under R version 4.0.5

## Warning: package 'tsibble' was built under R version 4.0.5

## Warning: package 'tsibbledata' was built under R version 4.0.5

## Warning: package 'feasts' was built under R version 4.0.5

## Warning: package 'fabletools' was built under R version 4.0.5

## Warning: package 'fable' was built under R version 4.0.5

## -- Conflicts ----- fpp3_conflicts --
## x lubridate::date()      masks base::date()
## x dplyr::filter()        masks stats::filter()
## x tsibble::intersect()   masks base::intersect()
## x tsibble::interval()   masks lubridate::interval()
## x dplyr::lag()           masks stats::lag()
## x tsibble::setdiff()     masks base::setdiff()
## x tsibble::union()       masks base::union()
```

```
library(TTR)
```

```
## Warning: package 'TTR' was built under R version 4.0.5
```

```
library(ggplot2)
library(tsibble)
library(tsibbledata)
library(dplyr)
library(forecast)
```

```
## Warning: package 'forecast' was built under R version 4.0.5
```

```
## Registered S3 method overwritten by 'quantmod':
##   method      from
##   as.zoo.data.frame zoo
```

```
library(fpp)
```

```
## Warning: package 'fpp' was built under R version 4.0.5
```

```
## Loading required package: fma
```

```
## Warning: package 'fma' was built under R version 4.0.5
```

```
## Loading required package: expsmooth
```

```
## Warning: package 'expsmooth' was built under R version 4.0.5
```

```
## Loading required package: lmtest
```

```
## Warning: package 'lmtest' was built under R version 4.0.5
```

```
## Loading required package: zoo
```

```
## Warning: package 'zoo' was built under R version 4.0.5
```

```
##
## Attaching package: 'zoo'
```

```
## The following object is masked from 'package:tsibble':
##
##   index
```

```
## The following objects are masked from 'package:base':
##
##   as.Date, as.Date.numeric
```

```
## Loading required package: tseries
```

```
## Warning: package 'tseries' was built under R version 4.0.5
```

```
##
```

```
## Attaching package: 'fpp'
```

```
## The following object is masked from 'package:fpp3':
```

```
##
```

```
##      insurance
```

```
library(fpp2)
```

```
## Warning: package 'fpp2' was built under R version 4.0.5
```

```
##
```

```
## Attaching package: 'fpp2'
```

```
## The following objects are masked from 'package:fpp':
```

```
##
```

```
##      ausair, ausbeer, austa, austourists, debitcards, departures,
```

```
##      elecequip, euretail, guinearice, oil, sunspotarea, usmelec
```

```
## The following object is masked from 'package:fpp3':
```

```
##
```

```
##      insurance
```

```
library(bsts)
```

```
## Warning: package 'bsts' was built under R version 4.0.5
```

```
## Loading required package: BoomSpikeSlab
```

```
## Warning: package 'BoomSpikeSlab' was built under R version 4.0.5
```

```
## Loading required package: Boom
```

```
## Warning: package 'Boom' was built under R version 4.0.5
```

```
## Loading required package: MASS
```

```
##
```

```
## Attaching package: 'MASS'
```

```
## The following objects are masked from 'package:fma':
```

```
##
```

```
##      cement, housing, petrol
```

```
## The following object is masked from 'package:dplyr':
```

```
##
```

```
##      select
```

```
##
## Attaching package: 'Boom'

## The following object is masked from 'package:stats':
##
##      rWishart

##
## Attaching package: 'BoomSpikeSlab'

## The following object is masked from 'package:stats':
##
##      knots

## Loading required package: xts

## Warning: package 'xts' was built under R version 4.0.5

##
## Attaching package: 'xts'

## The following objects are masked from 'package:dplyr':
##
##      first, last

##
## Attaching package: 'bsts'

## The following object is masked from 'package:BoomSpikeSlab':
##
##      SuggestBurn
```

```
library(prophet)
```

```
## Warning: package 'prophet' was built under R version 4.0.5

## Loading required package: Rcpp

## Warning: package 'Rcpp' was built under R version 4.0.5

## Loading required package: rlang

## Warning: package 'rlang' was built under R version 4.0.5
```

```
library(repr)
```

```
## Warning: package 'repr' was built under R version 4.0.5
```

```
library(readxl)
```

```
## Warning: package 'readxl' was built under R version 4.0.5
```

```
Tng_Ctr_Hour <- read_excel("C:/Users/prach/Desktop/Rutgers/BF/Project/Tng_Ctr_Hour.xlsx")
View(Tng_Ctr_Hour)
summary(Tng_Ctr_Hour)
```

```
##      Year      Quarter      Month      Device_Hrs
## Length:81    Length:81    Length:81    Min.   : 222.8
## Class :character Class :character Class :character 1st Qu.: 899.0
## Mode  :character Mode  :character Mode  :character Median :1008.0
##                                     Mean  : 990.1
##                                     3rd Qu.:1101.7
##                                     Max.   :1519.9
## DH_Prev_Year  DH_YoY_Change  DH_YoY_Ch_Per  Total_Inst_Hrs
## Length:81    Length:81    Length:81    Min.   : 504.6
## Class :character Class :character Class :character 1st Qu.:1937.3
## Mode  :character Mode  :character Mode  :character Median :2203.2
##                                     Mean  :2165.7
##                                     3rd Qu.:2446.8
##                                     Max.   :3084.1
## Total_Inst_Hrs_Prev_Year Inst_Hrs_YoY_Change Total_Inst_Hrs_YoY_Change_Per2
## Length:81    Length:81    Length:81
## Class :character Class :character Class :character
## Mode  :character Mode  :character Mode  :character
##
##
##
```

Converting Data Frame to Time Series

Converting the Dataset into training and testing set.

```
df_Tng = Tng_Ctr_Hour[,c(4)]
df_Tng
```

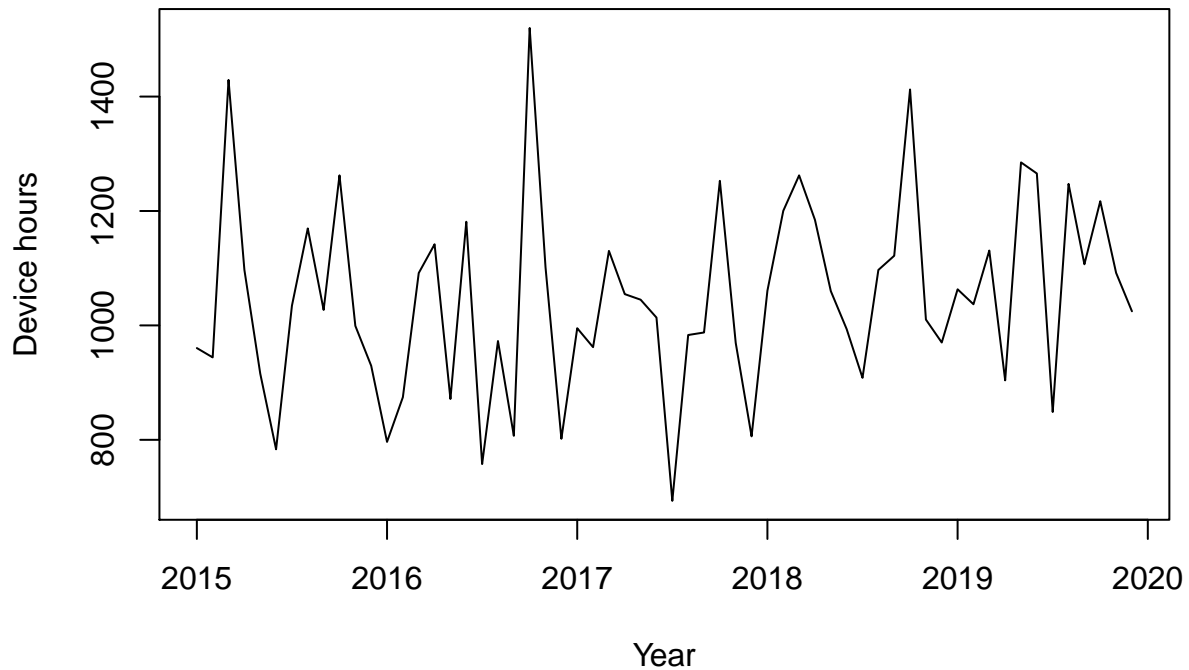
```
## # A tibble: 81 x 1
##   Device_Hrs
##   <dbl>
## 1    960.
## 2    944.
## 3   1429.
## 4   1097
## 5    916.
## 6    783.
## 7   1035.
## 8   1170.
## 9   1027.
## 10  1262.
## # ... with 71 more rows
```

```
train_tng = ts(data = df_Tng,frequency = 12,start = c(2015, 1),end = c(2019,12))
train_tng
```

```
##           Jan      Feb      Mar      Apr      May      Jun      Jul      Aug      Sep
## 2015  960.42  944.08 1429.12 1097.00  915.85  783.45 1034.52 1169.50 1027.08
## 2016  796.42  874.55 1091.55 1141.84  871.36 1181.21  757.59  972.73  807.02
## 2017  995.09  962.00 1130.24 1054.71 1044.95 1013.73  693.33  983.25  987.64
## 2018 1060.57 1200.25 1262.25 1184.45 1059.92  993.55  908.37 1096.93 1121.75
## 2019 1063.13 1036.95 1130.87  903.97 1284.95 1265.56  848.64 1247.40 1106.84
##           Oct      Nov      Dec
## 2015 1262.32  999.25  929.42
## 2016 1519.92 1101.67  801.83
## 2017 1252.69  969.31  806.10
## 2018 1412.47 1010.25  970.12
## 2019 1217.08 1091.84 1024.67
```

Plotting the time series

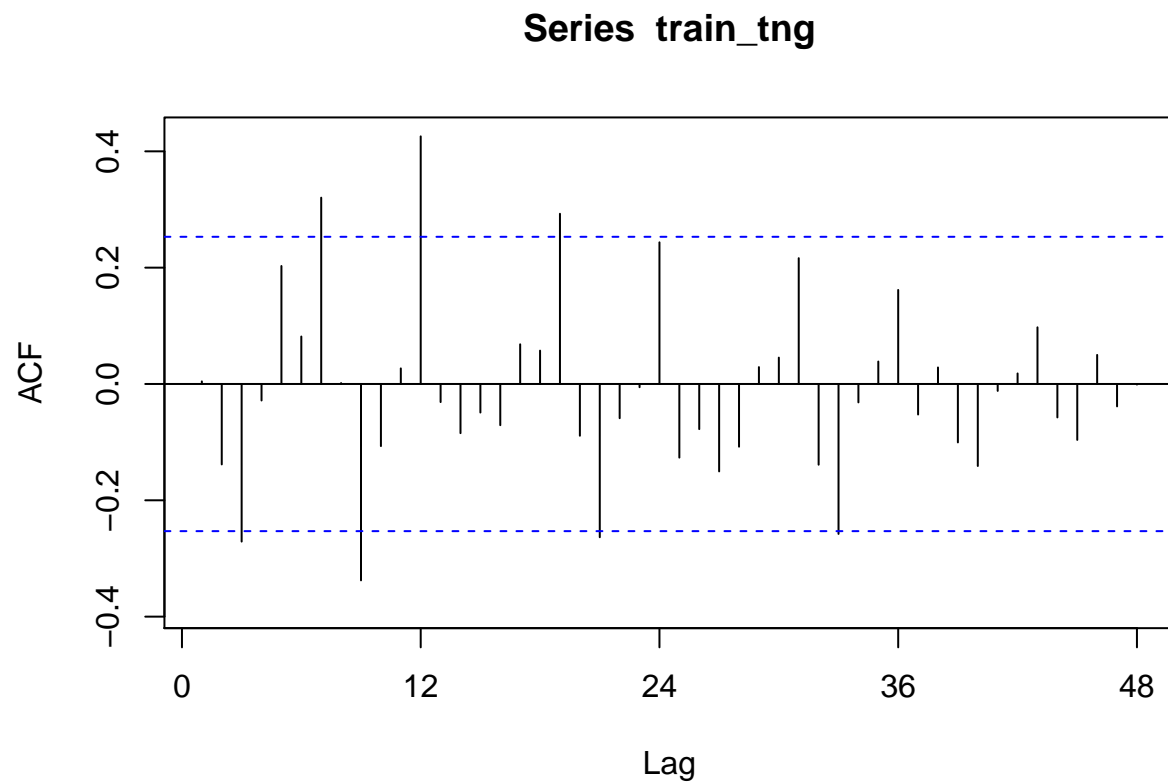
```
plot(train_tng,xlab = "Year", ylab = "Device hours")
```



We can notice in the plot that there is seasonality and device hours are its peak mostly in the third quarter of every year.

Acf

```
Acf(train_tng, lag = 48)
```

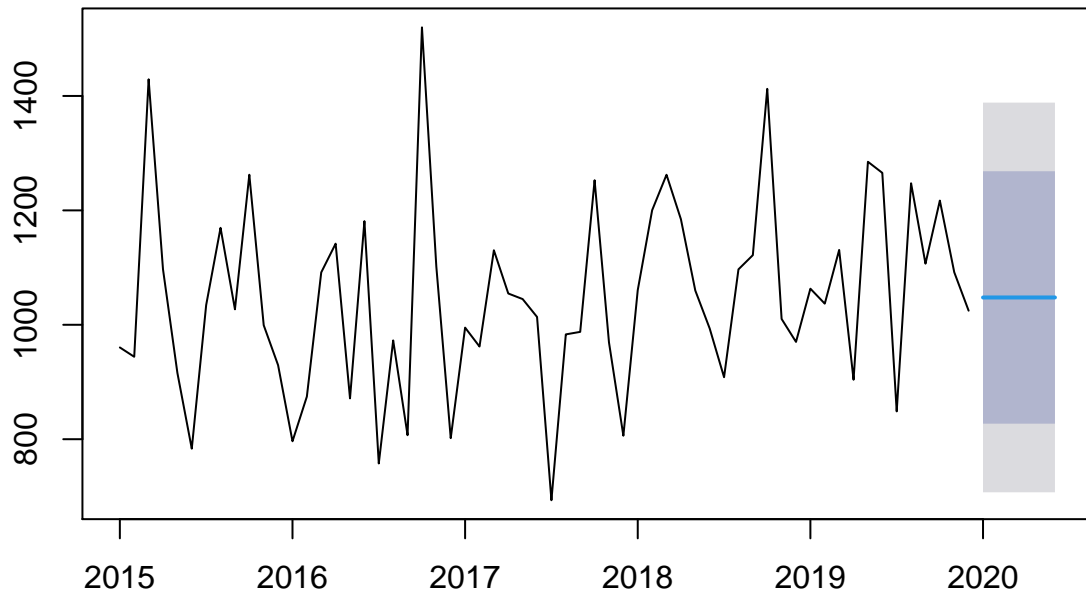


```
## Forecasting Methods
```

Mean Forecast

```
mean_forecast = meanf(train_tng, h=6)  
plot(mean_forecast)
```

Forecasts from Mean



```
summary(mean_forecast)
```

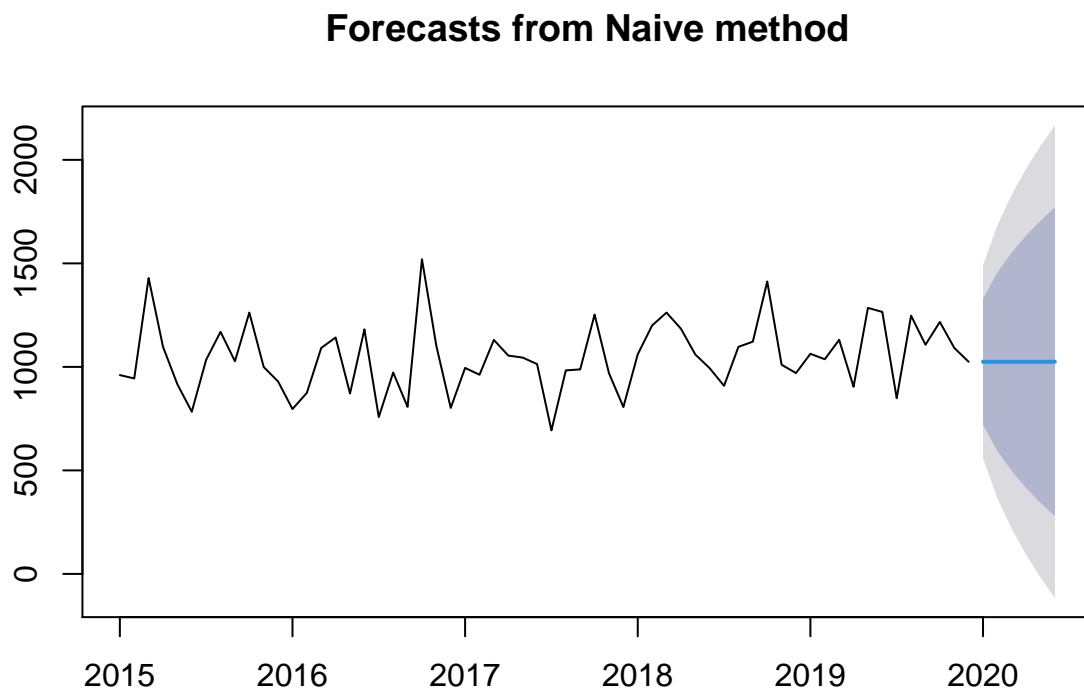
```
##
## Forecast method: Mean
##
## Model Information:
## $mu
## [1] 1047.759
##
## $mu.se
## [1] 21.79203
##
## $sd
## [1] 168.8003
##
## $bootstrap
## [1] FALSE
##
## $call
## meanf(y = train_tng, h = 6)
##
## attr("class")
## [1] "meanf"
##
## Error measures:
```



```
##           ME      RMSE      MAE      MPE      MAPE      MASE
## Training set 5.494447e-14 167.3878 130.0262 -2.590342 12.81213 0.9299448
##           ACF1
## Training set 0.004503158
##
## Forecasts:
##      Point Forecast      Lo 80      Hi 80      Lo 95      Hi 95
## Jan 2020      1047.759 827.1667 1268.351 707.1869 1388.33
## Feb 2020      1047.759 827.1667 1268.351 707.1869 1388.33
## Mar 2020      1047.759 827.1667 1268.351 707.1869 1388.33
## Apr 2020      1047.759 827.1667 1268.351 707.1869 1388.33
## May 2020      1047.759 827.1667 1268.351 707.1869 1388.33
## Jun 2020      1047.759 827.1667 1268.351 707.1869 1388.33
```

Naive Forecast

```
naive_forecast <- naive(train_tng,6)
plot(naive_forecast)
```



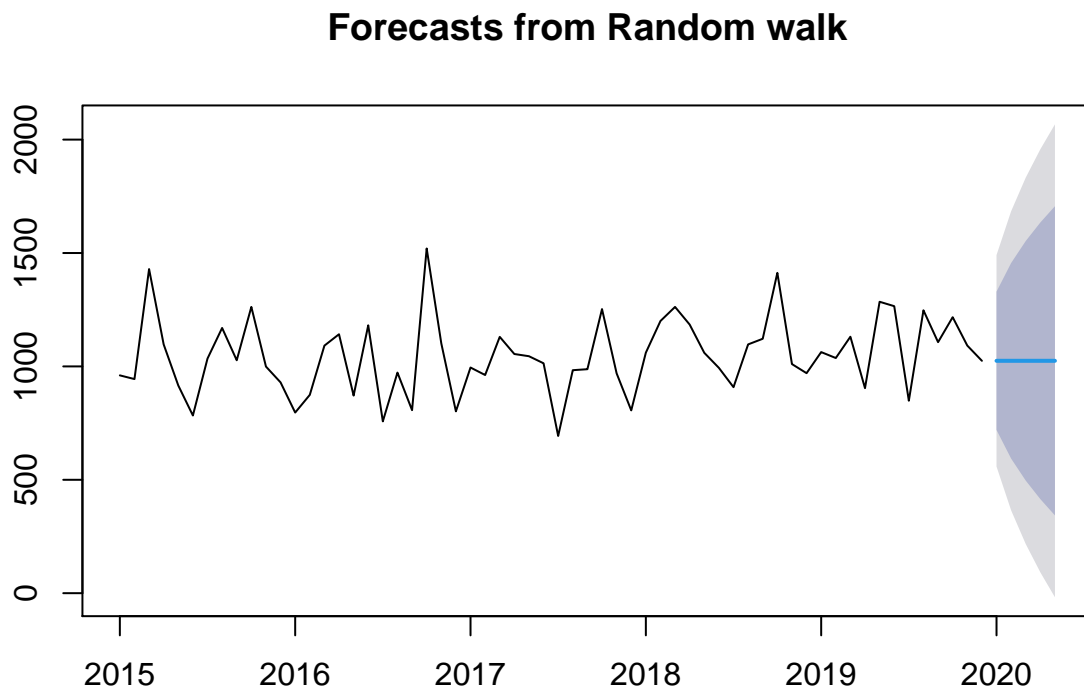
```
summary(naive_forecast)
```

```
##
## Forecast method: Naive method
```

```
##
## Model Information:
## Call: naive(y = train_tng, h = 6)
##
## Residual sd: 237.8911
##
## Error measures:
##           ME      RMSE      MAE      MPE      MAPE      MASE      ACF1
## Training set 1.088983 237.8911 190.3571 -2.425052 18.37449 1.36143 -0.4293306
##
## Forecasts:
##           Point Forecast      Lo 80      Hi 80      Lo 95      Hi 95
## Jan 2020           1024.67 719.8003 1329.540 558.41209 1490.928
## Feb 2020           1024.67 593.5192 1455.821 365.28174 1684.058
## Mar 2020           1024.67 496.6203 1552.720 217.08761 1832.252
## Apr 2020           1024.67 414.9307 1634.409  92.15418 1957.186
## May 2020           1024.67 342.9607 1706.379 -17.91439 2067.254
## Jun 2020           1024.67 277.8949 1771.445 -117.42397 2166.764
```

Random Walk Forecast

```
rwf_forecast = rwf(train_tng,5)
plot(rwf_forecast)
```



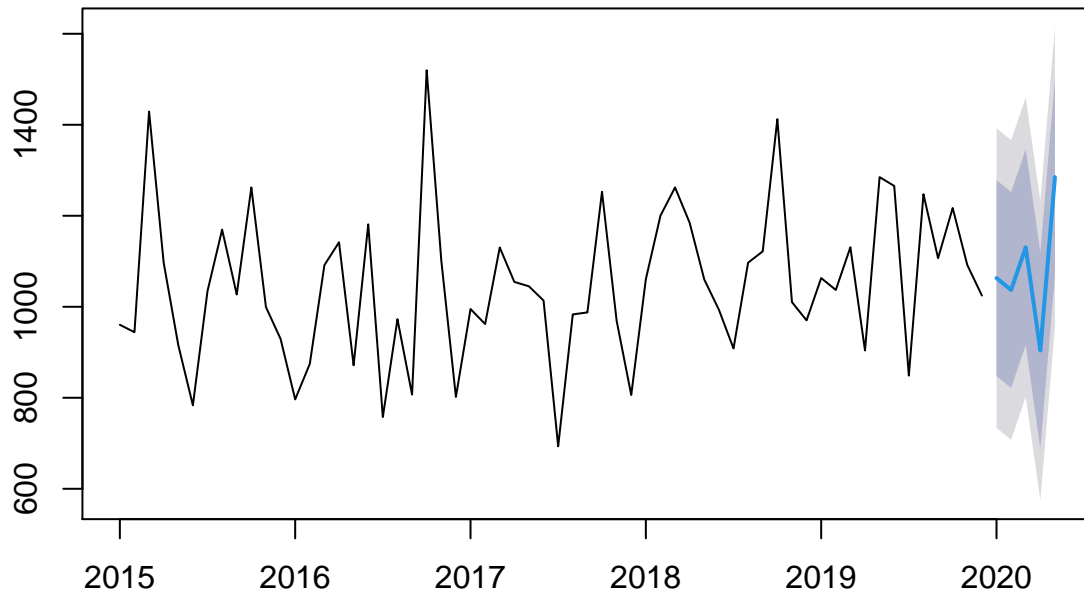
```
summary(rwf_forecast)
```

```
##
## Forecast method: Random walk
##
## Model Information:
## Call: rwf(y = train_tng, h = 5)
##
## Residual sd: 237.8911
##
## Error measures:
##           ME      RMSE      MAE      MPE      MAPE      MASE      ACF1
## Training set 1.088983 237.8911 190.3571 -2.425052 18.37449 1.36143 -0.4293306
##
## Forecasts:
##      Point Forecast    Lo 80    Hi 80    Lo 95    Hi 95
## Jan 2020      1024.67 719.8003 1329.540 558.41209 1490.928
## Feb 2020      1024.67 593.5192 1455.821 365.28174 1684.058
## Mar 2020      1024.67 496.6203 1552.720 217.08761 1832.252
## Apr 2020      1024.67 414.9307 1634.409  92.15418 1957.186
## May 2020      1024.67 342.9607 1706.379 -17.91439 2067.254
```

Seasonal Naive Forecast

```
snaive_forecast = snaive(train_tng,5)
plot(snaive_forecast)
```

Forecasts from Seasonal naive method

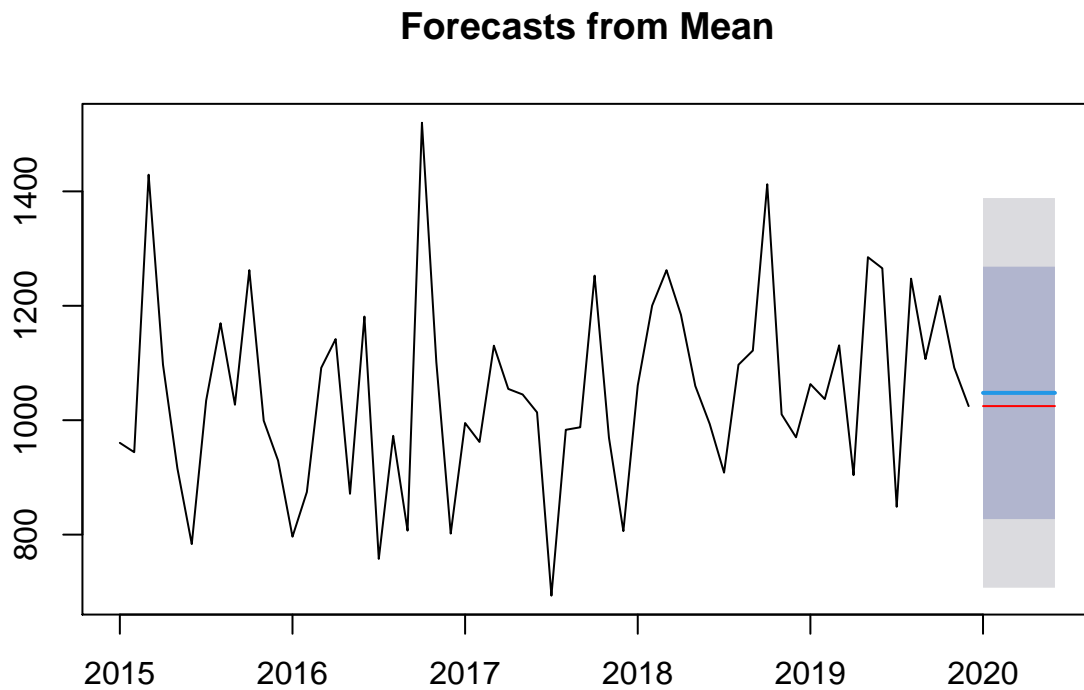


```
summary(snaive_forecast)
```

```
##
## Forecast method: Seasonal naive method
##
## Model Information:
## Call: snaive(y = train_tng, h = 5)
##
## Residual sd: 167.9362
##
## Error measures:
##           ME      RMSE      MAE      MPE      MAPE  MASE      ACF1
## Training set 13.95604 167.9362 139.8215 0.1167369 13.38504    1 0.02684331
##
## Forecasts:
##           Point Forecast      Lo 80      Hi 80      Lo 95      Hi 95
## Jan 2020          1063.13  847.9111 1278.349  733.9811 1392.279
## Feb 2020          1036.95  821.7311 1252.169  707.8011 1366.099
## Mar 2020          1130.87  915.6511 1346.089  801.7211 1460.019
## Apr 2020           903.97  688.7511 1119.189  574.8211 1233.119
## May 2020          1284.95 1069.7311 1500.169  955.8011 1614.099
```

Plotting mean and naive forecasting together

```
plot(mean_forecast)
lines(naive_forecast$mean,col="red")
```



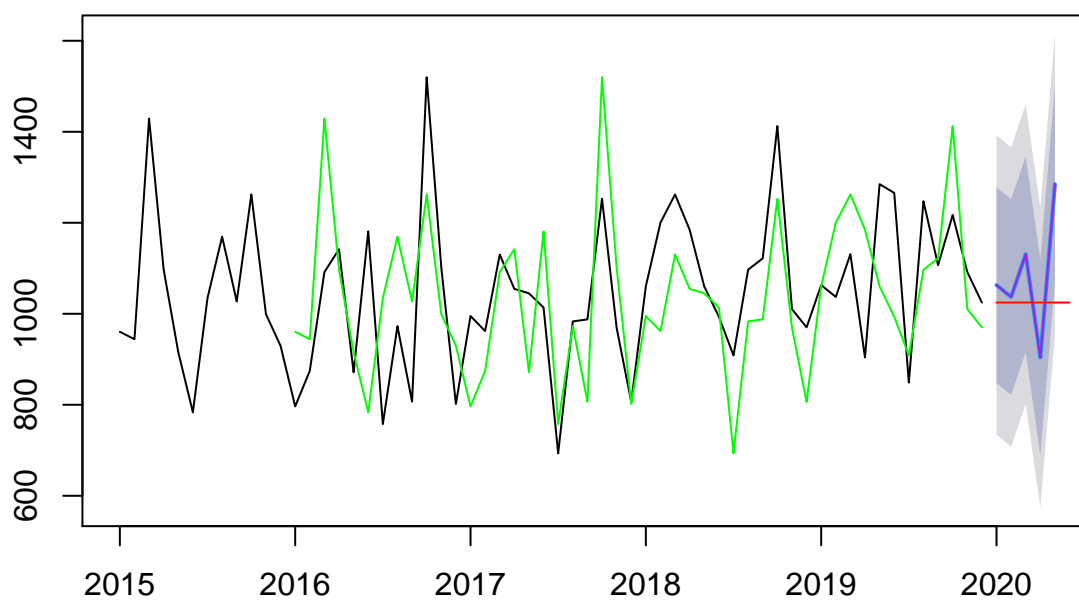
```
attributes(naive_forecast)
```

```
## $names
## [1] "method"      "model"      "lambda"     "x"          "fitted"     "residuals"
## [7] "series"      "mean"       "level"      "lower"      "upper"
##
## $class
## [1] "forecast"
```

Plotting other attributes

```
plot(snaive_forecast)
lines(rwf_forecast$mean,col="yellow")
lines(snaive_forecast$mean,col="purple")
lines(snaive_forecast$fitted, col = "green")
lines(naive_forecast$mean,col="red")
```

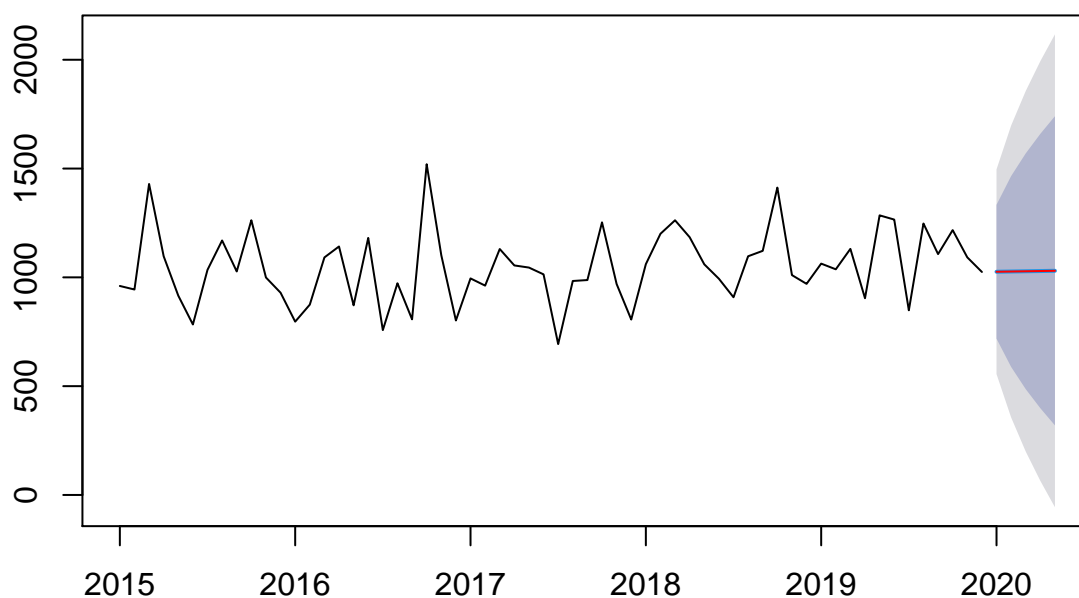
Forecasts from Seasonal naive method



Drift with RWF

```
rwf_drift = rwf(train_tng,5,drift = TRUE)
plot(rwf_drift)
lines(rwf_drift$mean, col = "red")
```

Forecasts from Random walk with drift

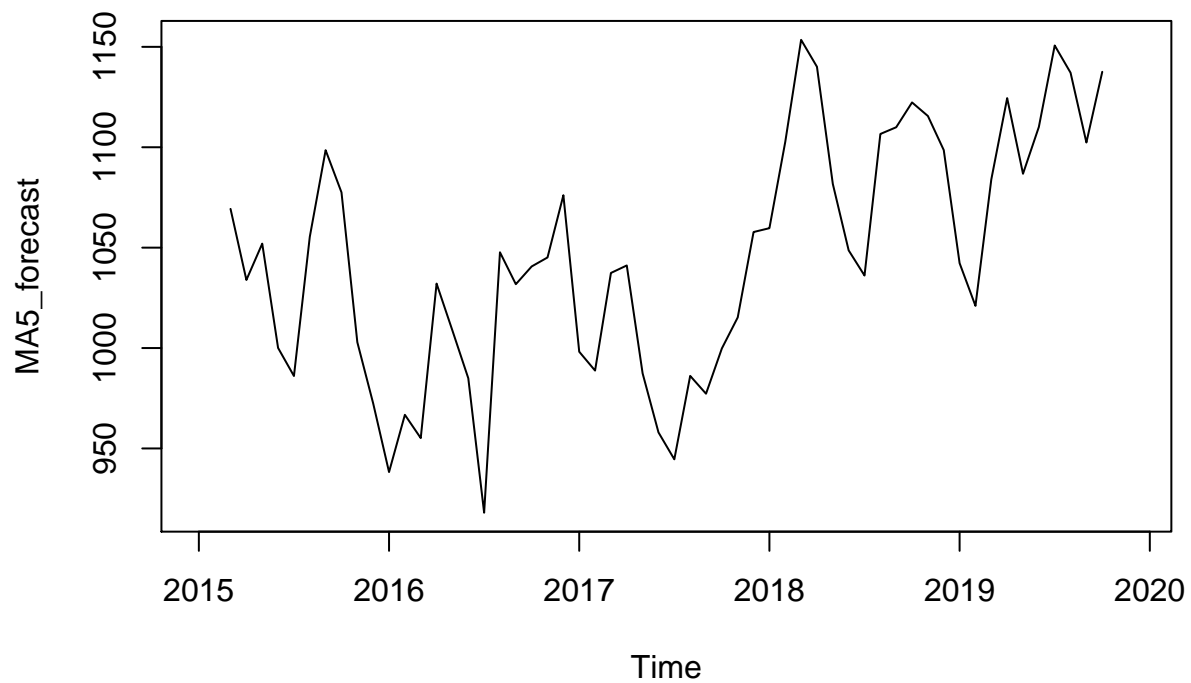


```
summary(rwf_drift)
```

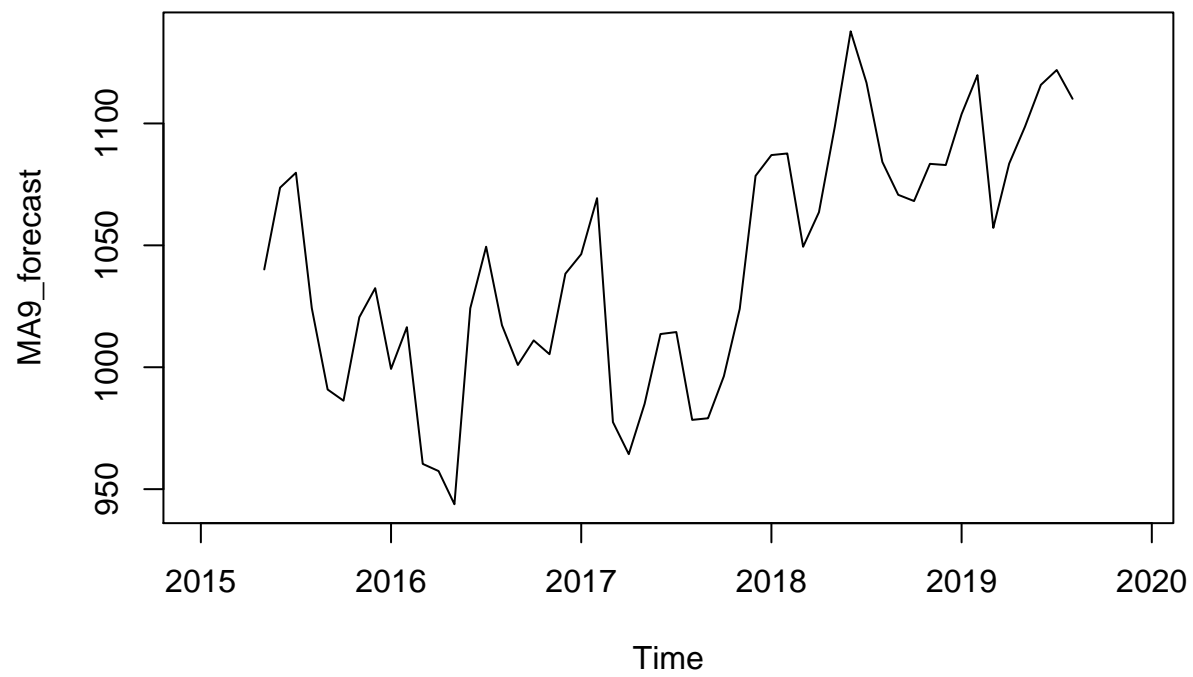
```
##
## Forecast method: Random walk with drift
##
## Model Information:
## Call: rwf(y = train_tng, h = 5, drift = TRUE)
##
## Drift: 1.089 (se 31.2363)
## Residual sd: 239.9306
##
## Error measures:
##           ME      RMSE      MAE      MPE      MAPE      MASE
## Training set 1.348733e-14 237.8886 190.4863 -2.531564 18.39682 1.362354
##           ACF1
## Training set -0.4293306
##
## Forecasts:
##      Point Forecast      Lo 80      Hi 80      Lo 95      Hi 95
## Jan 2020      1025.759 718.2756 1333.242 555.50371 1496.014
## Feb 2020      1026.848 588.3311 1465.365 356.19432 1697.502
## Mar 2020      1027.937 486.4086 1569.465 199.74079 1856.133
## Apr 2020      1029.026 398.6182 1659.434  64.90057 1993.151
## May 2020      1030.115 319.6364 1740.593 -56.46818 2116.698
```

Moving Average Forecast

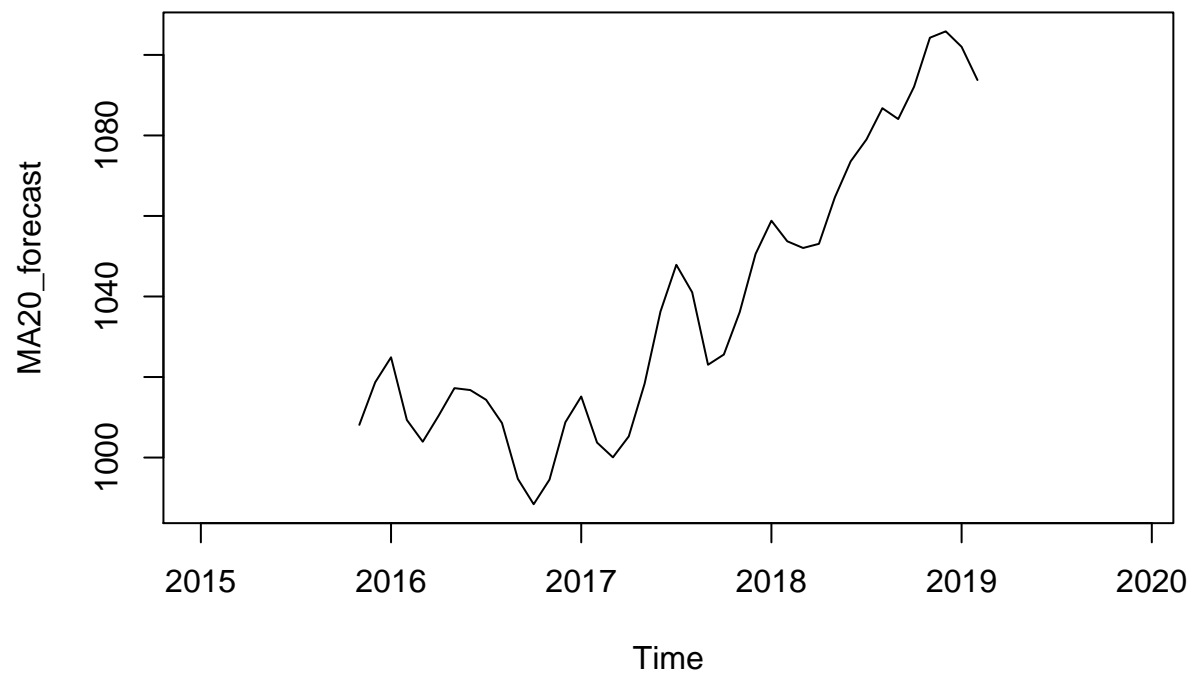
```
MA5_forecast <- ma(train_tng,order=5)
MA9_forecast <- ma(train_tng,order=9)
MA20_forecast <- ma(train_tng,order=20)
plot(MA5_forecast)
```



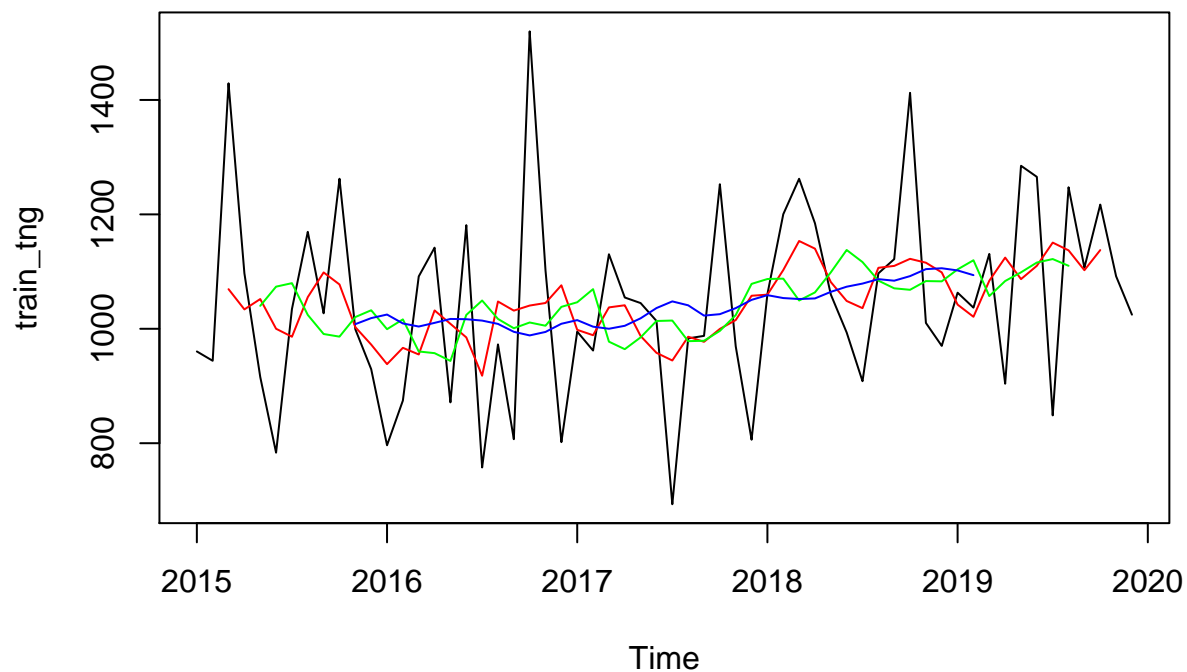
```
plot(MA9_forecast)
```

```
plot(MA20_forecast)
```



```
plot(train_tng)
lines(MA5_forecast, col = "Red")
lines(MA9_forecast, col = "Green")
lines(MA20_forecast, col = "Blue")
```



```
summary(MA5_forecast)
```

```
##      Min. 1st Qu.  Median    Mean 3rd Qu.    Max.     NA's
##    918.0   999.4  1043.7  1045.7  1098.5  1153.5         4
```

As we increase the order, the graph becomes smoother and randomness in the data is decreased.

ETS

```
ets(train_tng)
```

```
## ETS(M,N,M)
##
## Call:
## ets(y = train_tng)
##
## Smoothing parameters:
##   alpha = 0.0576
##   gamma = 1e-04
##
## Initial states:
```

```
##      l = 1047.4318
##      s = 0.8577 0.9689 1.2739 0.9471 1.0336 0.8229
##          1.0137 1.0033 1.0204 1.1643 0.9529 0.9413
##
##      sigma: 0.1274
##
##      AIC      AICc      BIC
## 845.0223 855.9314 876.4374
```

Holt Winters

```
HoltWinters(train_tng)
```

```
## Holt-Winters exponential smoothing with trend and additive seasonal component.
##
## Call:
## HoltWinters(x = train_tng)
##
## Smoothing parameters:
##   alpha: 0.03242971
##   beta : 0.2550264
##   gamma: 0.5409953
##
## Coefficients:
##           [,1]
## a    1098.083982
## b         4.106445
## s1        5.752170
## s2       26.587256
## s3      131.000958
## s4     -13.303193
## s5      126.573215
## s6      121.179458
## s7     -195.078411
## s8      112.683879
## s9        24.150535
## s10     233.999789
## s11      -2.426057
## s12     -91.113979
```

SSE without trend and without seasonality

```
HoltWinters(train_tng,beta=FALSE,gamma=FALSE)
```

```
## Holt-Winters exponential smoothing without trend and without seasonal component.
##
## Call:
## HoltWinters(x = train_tng, beta = FALSE, gamma = FALSE)
##
```

```
## Smoothing parameters:
## alpha: 0.05955483
## beta : FALSE
## gamma: FALSE
##
## Coefficients:
##      [,1]
## a 1078.308
```

```
hw_forecast_level = HoltWinters(train_tng,beta=FALSE,gamma=FALSE)
hw_forecast_level
```

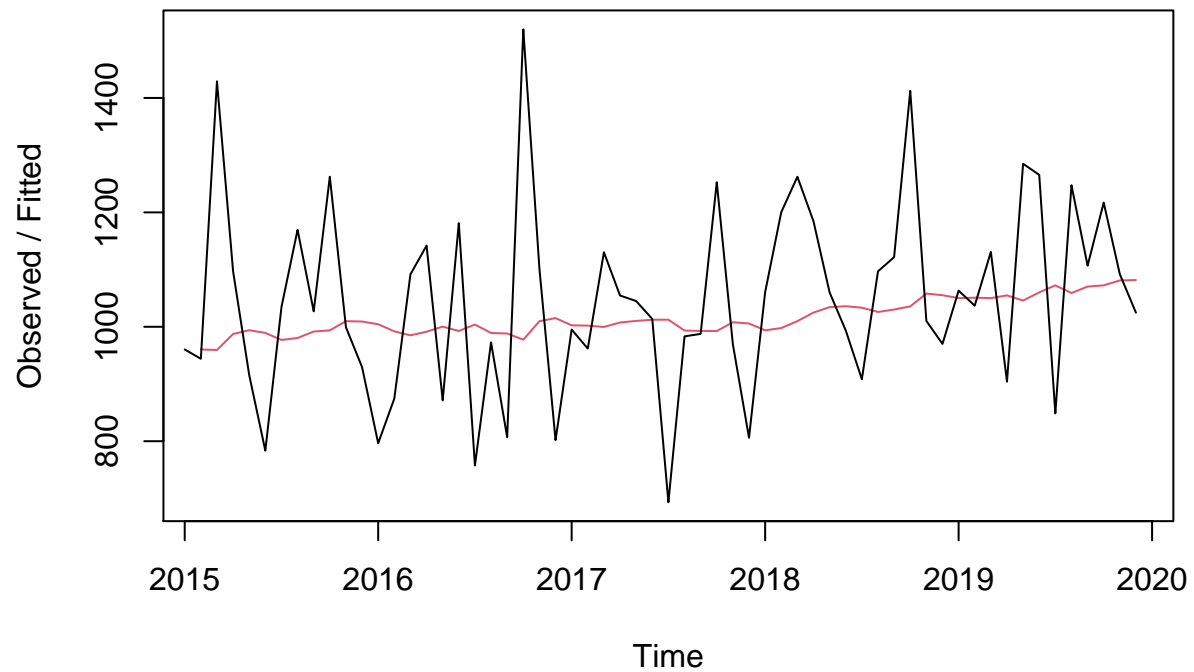
```
## Holt-Winters exponential smoothing without trend and without seasonal component.
##
## Call:
## HoltWinters(x = train_tng, beta = FALSE, gamma = FALSE)
##
## Smoothing parameters:
## alpha: 0.05955483
## beta : FALSE
## gamma: FALSE
##
## Coefficients:
##      [,1]
## a 1078.308
```

```
attributes(hw_forecast_level)
```

```
## $names
## [1] "fitted"      "x"           "alpha"       "beta"        "gamma"
## [6] "coefficients" "seasonal"    "SSE"         "call"
##
## $class
## [1] "HoltWinters"
```

```
plot(hw_forecast_level)
```

Holt-Winters filtering



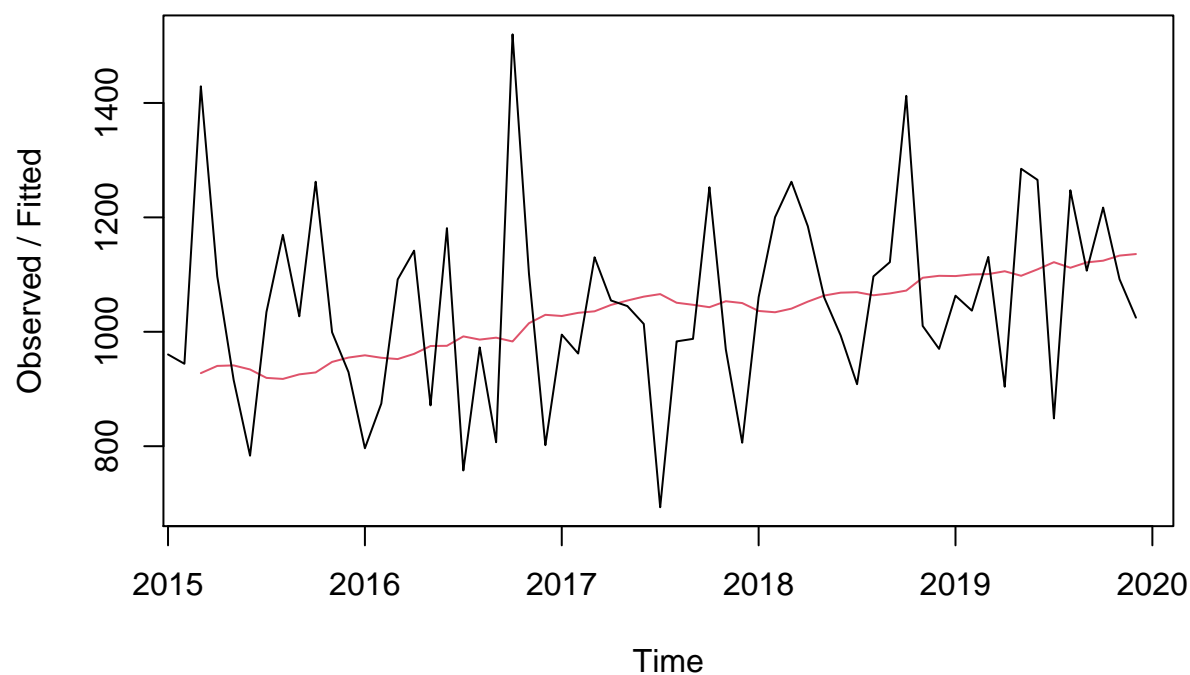
```
hw_forecast_level$SSE
```

```
## [1] 1776425
```

SSE with Trend but no Seasonlaity

```
hw_forecast_trend = HoltWinters(train_tng,gamma=FALSE)  
plot(hw_forecast_trend)
```

Holt-Winters filtering



```
hw_forecast_trend
```

```
## Holt-Winters exponential smoothing with trend and without seasonal component.
##
## Call:
## HoltWinters(x = train_tng, gamma = FALSE)
##
## Smoothing parameters:
##   alpha: 0.04146809
##   beta : 0.3933152
##   gamma: FALSE
##
## Coefficients:
##           [,1]
## a 1131.268702
## b   2.580617
```

```
hw_forecast_trend$SSE #Check the residual error magnitude
```

```
## [1] 1841394
```

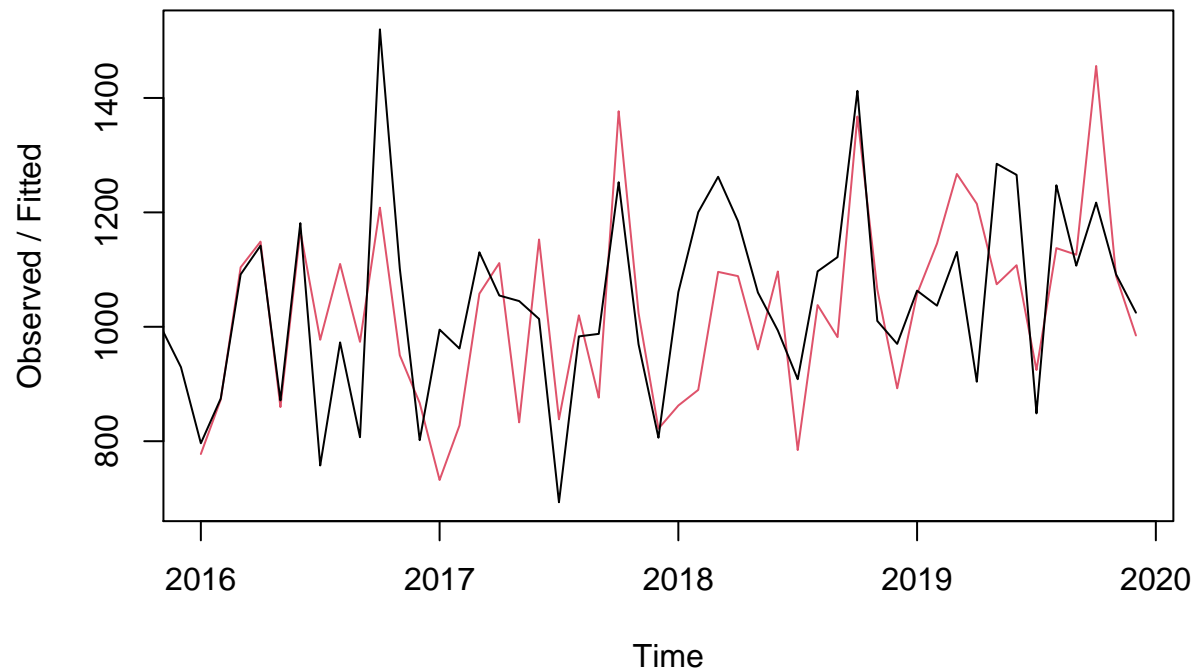
SSE with trend and seasonality

```
hw_forecast_season = HoltWinters(train_tng)
hw_forecast_season
```

```
## Holt-Winters exponential smoothing with trend and additive seasonal component.
##
## Call:
## HoltWinters(x = train_tng)
##
## Smoothing parameters:
##   alpha: 0.03242971
##   beta : 0.2550264
##   gamma: 0.5409953
##
## Coefficients:
##              [,1]
## a    1098.083982
## b         4.106445
## s1      5.752170
## s2     26.587256
## s3    131.000958
## s4   -13.303193
## s5    126.573215
## s6    121.179458
## s7   -195.078411
## s8    112.683879
## s9     24.150535
## s10   233.999789
## s11    -2.426057
## s12   -91.113979
```

```
plot(hw_forecast_season)
```


Holt-Winters filtering



```
hw_forecast_season$SSE
```

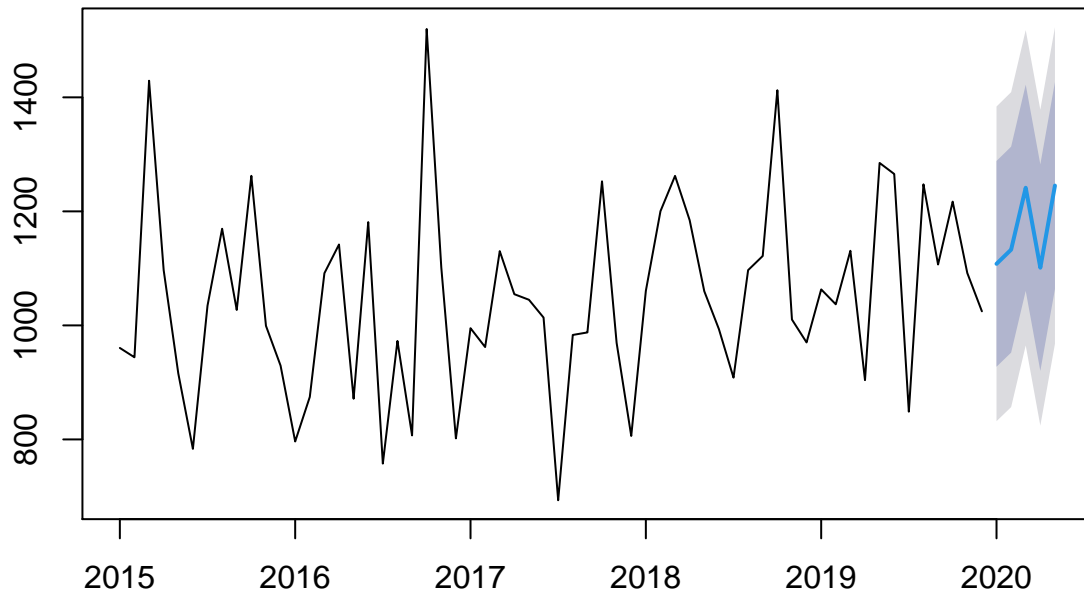
```
## [1] 949245.4
```

```
hw_forecast_all = forecast(hw_forecast_season,h =5)  
hw_forecast_all
```

```
##          Point Forecast      Lo 80      Hi 80      Lo 95      Hi 95  
## Jan 2020      1107.943  927.5032 1288.382  831.9843 1383.901  
## Feb 2020      1132.884  952.2953 1313.473  856.6974 1409.071  
## Mar 2020      1241.404 1060.5994 1422.209  964.8871 1517.921  
## Apr 2020      1101.207  920.1069 1282.306  824.2386 1378.175  
## May 2020      1245.189 1063.7044 1426.674  967.6320 1522.747
```

```
plot(hw_forecast_all)
```

Forecasts from HoltWinters



```
accuracy(hw_forecast_all)
```

```
##               ME      RMSE      MAE      MPE      MAPE      MASE      ACF1
## Training set 19.10421 140.627 111.9195 0.8341924 10.74567 0.8004457 0.1613357
```

SSE of HoltWinters with Trend and Seasonality is smaller than the SSE of Holtwinter without trend, without seasonality and SSE of Holtwinters with Trend and without seasonality.

Ets

```
ets(train_tng)
```

```
## ETS(M,N,M)
##
## Call:
## ets(y = train_tng)
##
## Smoothing parameters:
##   alpha = 0.0576
##   gamma = 1e-04
##
```

```
## Initial states:
## l = 1047.4318
## s = 0.8577 0.9689 1.2739 0.9471 1.0336 0.8229
##      1.0137 1.0033 1.0204 1.1643 0.9529 0.9413
##
## sigma: 0.1274
##
##      AIC      AICc      BIC
## 845.0223 855.9314 876.4374
```

```
ets_forecast = ets(train_tng)
attributes(ets)
```

```
## NULL
```

```
attributes(ets_forecast)
```

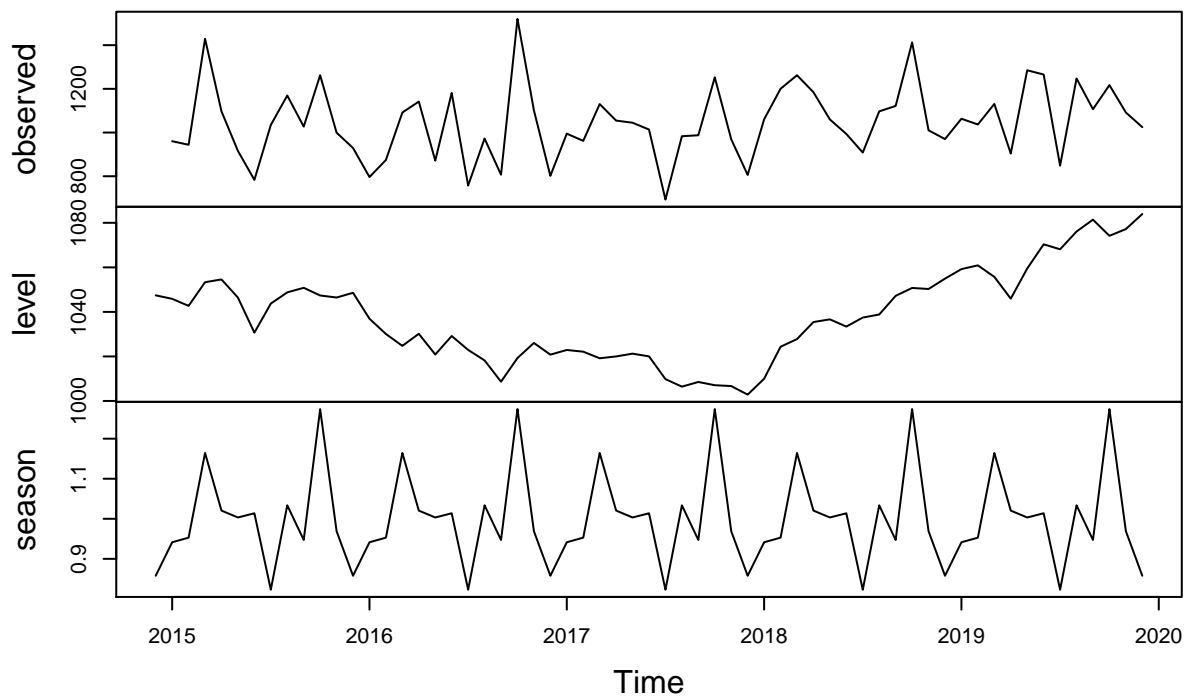
```
## $names
## [1] "loglik"      "aic"         "bic"         "aicc"        "mse"
## [6] "amse"        "fit"         "residuals"   "fitted"      "states"
## [11] "par"         "m"           "method"      "series"      "components"
## [16] "call"        "initstate"   "sigma2"      "x"
##
## $class
## [1] "ets"
```

```
ets_forecast$mse
```

```
## [1] 13415.89
```

```
plot(ets_forecast)
```

Decomposition by ETS(M,N,M) method



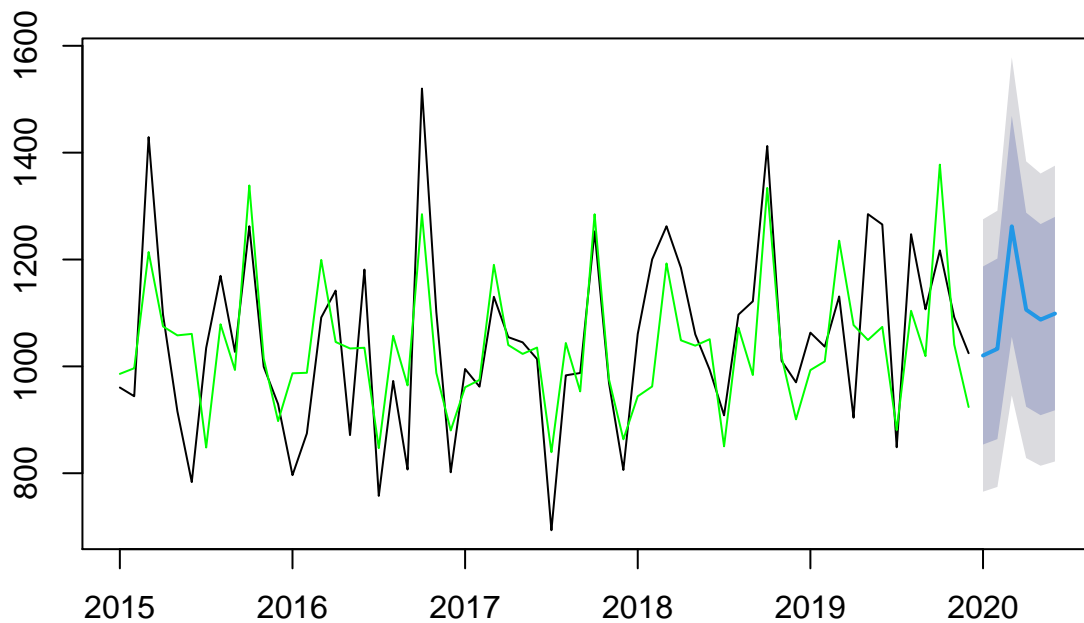
Forecast with Ets

```
forecast.ets(ets_forecast, h=6)
```

##	Point Forecast	Lo 80	Hi 80	Lo 95	Hi 95
## Jan 2020	1020.365	853.7138	1187.016	765.4940	1275.236
## Feb 2020	1032.863	863.8867	1201.839	774.4362	1291.289
## Mar 2020	1262.057	1055.2391	1468.876	945.7561	1578.359
## Apr 2020	1106.075	924.5152	1287.634	828.4033	1383.746
## May 2020	1087.494	908.6867	1266.301	814.0321	1360.955
## Jun 2020	1098.813	917.8453	1279.781	822.0466	1375.580

```
forecast_ets = forecast.ets(ets_forecast, h=6)
plot(forecast_ets)
lines(forecast_ets$fitted, col="green")
```

Forecasts from ETS(M,N,M)



```
accuracy(forecast_ets)
```

```
##                               ME    RMSE    MAE    MPE    MAPE    MASE    ACF1
## Training set 10.47703 115.827 93.97734 -0.2245269 9.112492 0.6721239 0.04408278
```

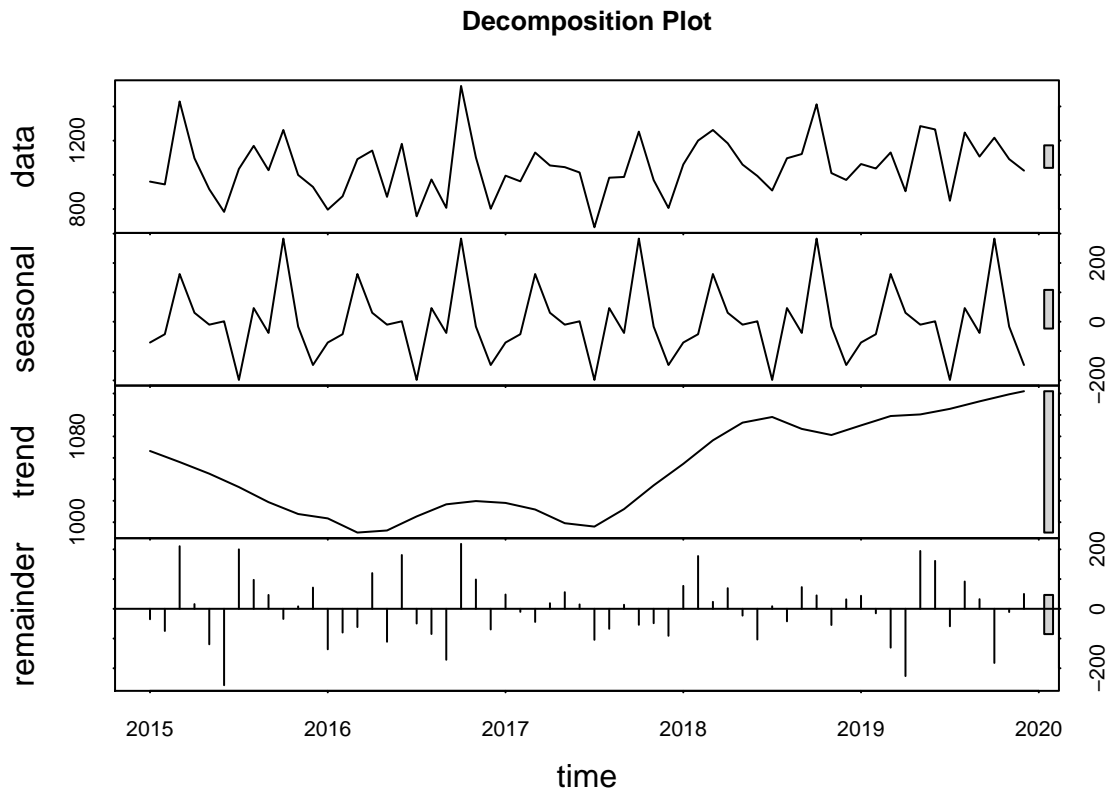
Decomposition

```
stl_decomp = stl(train_tng, s.window = "periodic")
stl_decomp
```

```
## Call:
## stl(x = train_tng, s.window = "periodic")
##
## Components
##      seasonal      trend  remainder
## Jan 2015 -70.915777 1066.4205 -35.084739
## Feb 2015 -42.611463 1061.2528 -74.561376
## Mar 2015 162.492749 1056.0852 210.542088
## Apr 2015  30.504883 1050.6743  15.820826
## May 2015 -10.059213 1045.2634 -119.354208
## Jun 2015   1.393934 1039.0208 -256.964697
## Jul 2015 -198.257090 1032.7781 199.998984
## Aug 2015  46.454532 1025.7504  97.295063
```

## Sep 2015	-38.201779	1018.7227	46.559073
## Oct 2015	283.244350	1013.1913	-34.115634
## Nov 2015	-16.571712	1007.6599	8.161849
## Dec 2015	-147.473465	1005.6070	71.286507
## Jan 2016	-70.915777	1003.5541	-136.218277
## Feb 2016	-42.611463	996.9635	-79.802043
## Mar 2016	162.492749	990.3730	-61.315707
## Apr 2016	30.504883	991.3423	119.992841
## May 2016	-10.059213	992.3116	-110.892381
## Jun 2016	1.393934	998.8536	180.962509
## Jul 2016	-198.257090	1005.3955	-49.548430
## Aug 2016	46.454532	1011.0417	-84.766246
## Sep 2016	-38.201779	1016.6879	-171.466130
## Oct 2016	283.244350	1018.2038	218.471859
## Nov 2016	-16.571712	1019.7197	98.522038
## Dec 2016	-147.473465	1018.8521	-69.548663
## Jan 2017	-70.915777	1017.9846	48.021194
## Feb 2017	-42.611463	1014.9185	-10.307084
## Mar 2017	162.492749	1011.8525	-44.105260
## Apr 2017	30.504883	1005.4660	18.739121
## May 2017	-10.059213	999.0795	55.929732
## Jun 2017	1.393934	997.5038	14.832273
## Jul 2017	-198.257090	995.9281	-104.341015
## Aug 2017	46.454532	1004.0896	-67.294128
## Sep 2017	-38.201779	1012.2511	13.590691
## Oct 2017	283.244350	1023.3028	-53.857162
## Nov 2017	-16.571712	1034.3545	-48.472825
## Dec 2017	-147.473465	1044.3906	-90.817098
## Jan 2018	-70.915777	1054.4266	77.059186
## Feb 2018	-42.611463	1065.3955	177.465993
## Mar 2018	162.492749	1076.3643	23.392902
## Apr 2018	30.504883	1084.6045	69.340655
## May 2018	-10.059213	1092.8446	-22.865363
## Jun 2018	1.393934	1095.4737	-103.317629
## Jul 2018	-198.257090	1098.1028	8.524276
## Aug 2018	46.454532	1092.5451	-42.069635
## Sep 2018	-38.201779	1086.9874	72.964385
## Oct 2018	283.244350	1084.1472	45.078464
## Nov 2018	-16.571712	1081.3070	-54.485268
## Dec 2018	-147.473465	1085.7953	31.798174
## Jan 2019	-70.915777	1090.2836	43.762173
## Feb 2019	-42.611463	1094.6359	-15.074463
## Mar 2019	162.492749	1098.9882	-130.610997
## Apr 2019	30.504883	1099.7370	-226.271912
## May 2019	-10.059213	1100.4858	194.523402
## Jun 2019	1.393934	1103.0818	161.084246
## Jul 2019	-198.257090	1105.6778	-58.780740
## Aug 2019	46.454532	1109.1747	91.770742
## Sep 2019	-38.201779	1112.6716	32.370157
## Oct 2019	283.244350	1115.9599	-182.124262
## Nov 2019	-16.571712	1119.2482	-10.836491
## Dec 2019	-147.473465	1122.1292	50.014278

```
plot(stl_decomp, main="Decomposition Plot")
```



```
attributes(stl_decomp)
```

```
## $names
## [1] "time.series" "weights"      "call"      "win"      "deg"
## [6] "jump"        "inner"      "outer"
##
## $class
## [1] "stl"
```

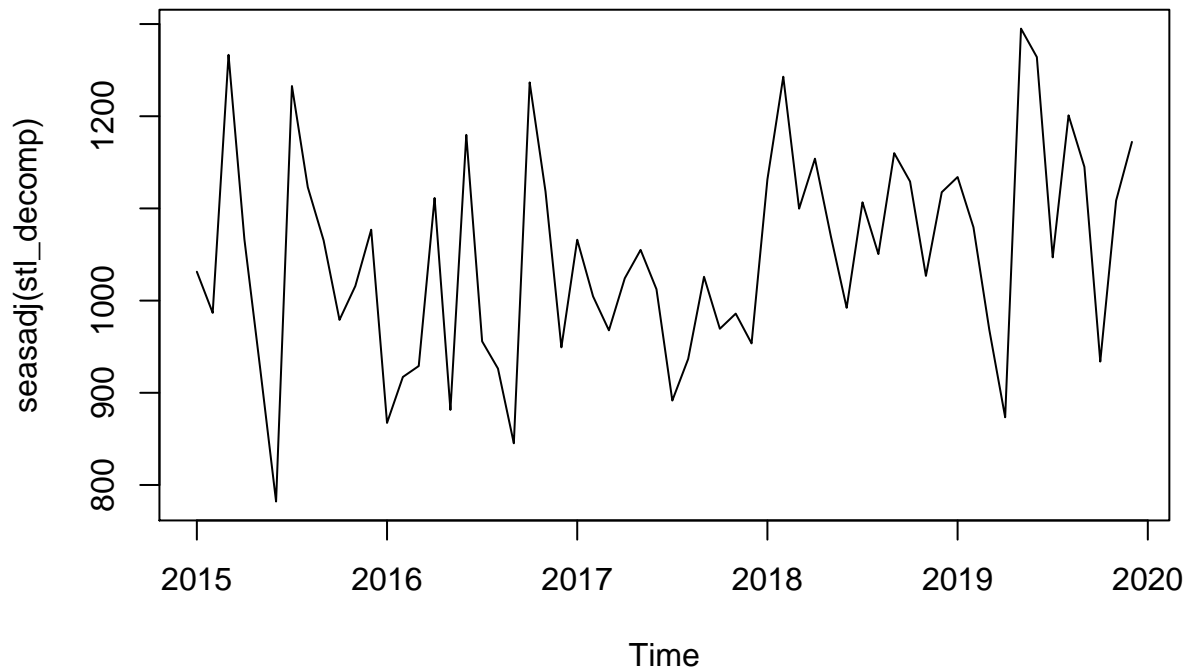
Seasonal Adjustment

```
seasadj(stl_decomp)
```

```
##           Jan           Feb           Mar           Apr           May           Jun           Jul
## 2015 1031.3358  986.6915 1266.6273 1066.4951  925.9092  782.0561 1232.7771
## 2016  867.3358  917.1615  929.0573 1111.3351  881.4192 1179.8161  955.8471
## 2017 1066.0058 1004.6115  967.7473 1024.2051 1055.0092 1012.3361  891.5871
## 2018 1131.4858 1242.8615 1099.7573 1153.9451 1069.9792  992.1561 1106.6271
## 2019 1134.0458 1079.5615  968.3773  873.4651 1295.0092 1264.1661 1046.8971
##           Aug           Sep           Oct           Nov           Dec
```

```
## 2015 1123.0455 1065.2818 979.0757 1015.8217 1076.8935
## 2016 926.2755 845.2218 1236.6757 1118.2417 949.3035
## 2017 936.7955 1025.8418 969.4457 985.8817 953.5735
## 2018 1050.4755 1159.9518 1129.2257 1026.8217 1117.5935
## 2019 1200.9455 1145.0418 933.8357 1108.4117 1172.1435
```

```
plot(seasadj(stl_decomp))
```



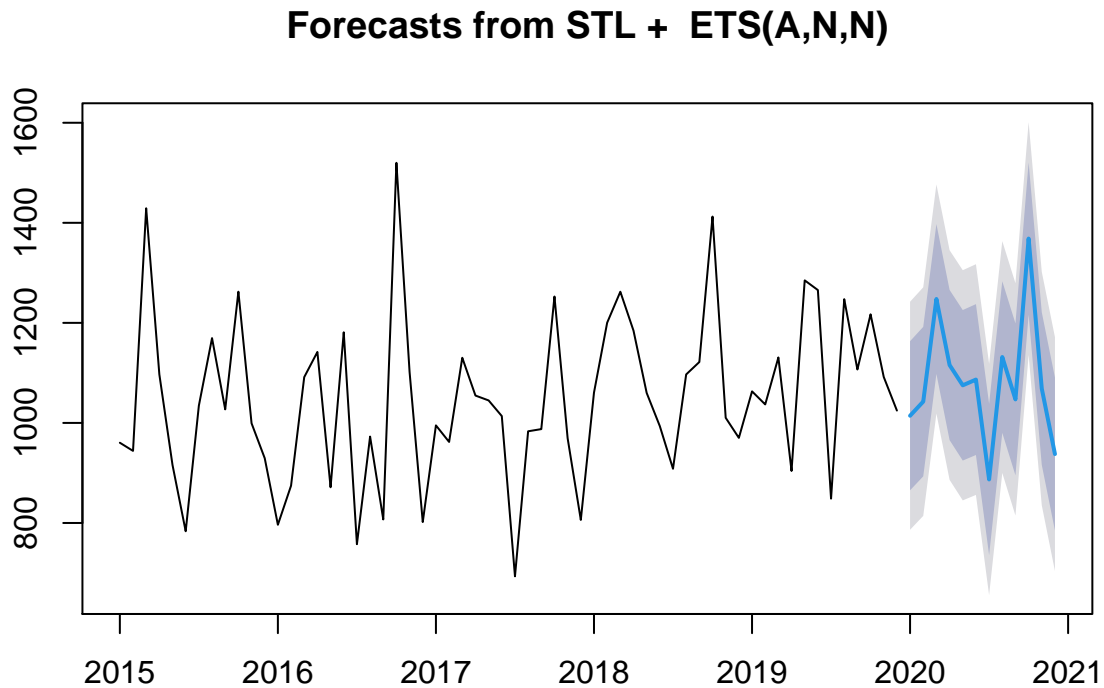
Default Period Forecast

```
f_stl = forecast(stl_decomp,h = 12)
f_stl
```

##	Point Forecast	Lo 80	Hi 80	Lo 95	Hi 95
## Jan 2020	1014.3270	865.2967	1163.357	786.4049	1242.249
## Feb 2020	1042.6313	893.2525	1192.010	814.1762	1271.086
## Mar 2020	1247.7355	1098.0091	1397.462	1018.7487	1476.722
## Apr 2020	1115.7477	965.6743	1265.821	886.2303	1345.265
## May 2020	1075.1836	924.7641	1225.603	845.1369	1305.230
## Jun 2020	1086.6367	935.8720	1237.401	856.0619	1317.211
## Jul 2020	886.9857	735.8764	1038.095	655.8840	1118.087
## Aug 2020	1131.6973	980.2443	1283.150	900.0699	1363.325
## Sep 2020	1047.0410	895.2451	1198.837	814.8891	1279.193


```
## Oct 2020      1368.4871 1216.3490 1520.625 1135.8120 1601.162
## Nov 2020      1068.6711  916.1915 1221.151  835.4738 1301.868
## Dec 2020       937.7693  784.9491 1090.589  704.0510 1171.488
```

```
plot(f_stl)
```



```
accuracy(f_stl)
```

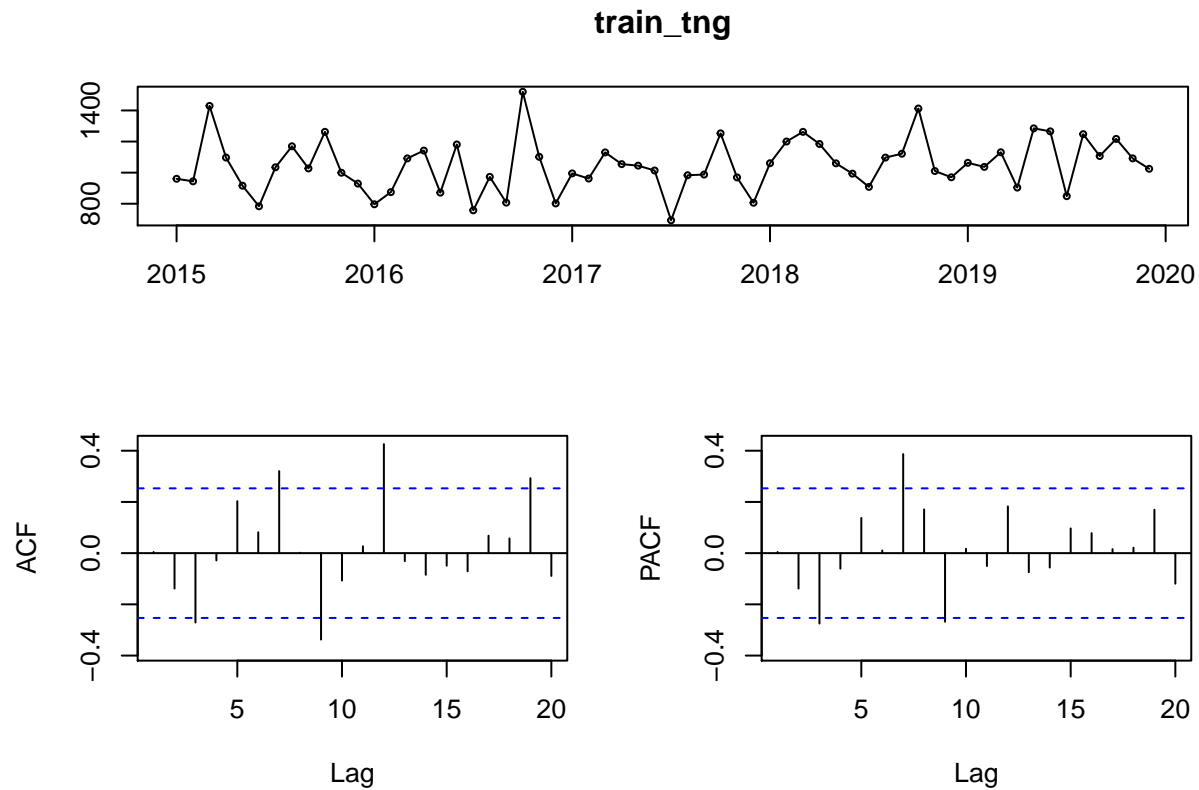
```
##              ME      RMSE      MAE      MPE      MAPE      MASE      ACF1
## Training set 13.38141 114.3344 91.29621 0.1050379 8.793197 0.6529485 0.02342607
```

Accuracy is improved for stl decomp as MAPE is slightly lower compared to other forecasts.

```
ndiffs(train_tng)
```

```
## [1] 0
```

```
tsdisplay(train_tng)
```



```
auto_fit = auto.arima(train_tng,trace = TRUE, stepwise = FALSE)
```

```
##
## ARIMA(0,0,0)          with zero mean      : 1008.383
## ARIMA(0,0,0)          with non-zero mean  : 788.9207
## ARIMA(0,0,0)(0,0,1)[12] with zero mean    : Inf
## ARIMA(0,0,0)(0,0,1)[12] with non-zero mean : 779.2159
## ARIMA(0,0,0)(1,0,0)[12] with zero mean    : Inf
## ARIMA(0,0,0)(1,0,0)[12] with non-zero mean : 776.3417
## ARIMA(0,0,0)(1,0,1)[12] with zero mean    : Inf
## ARIMA(0,0,0)(1,0,1)[12] with non-zero mean : 777.4751
## ARIMA(0,0,1)          with zero mean      : 952.3381
## ARIMA(0,0,1)          with non-zero mean  : 791.1371
## ARIMA(0,0,1)(0,0,1)[12] with zero mean    : Inf
## ARIMA(0,0,1)(0,0,1)[12] with non-zero mean : 781.4647
## ARIMA(0,0,1)(1,0,0)[12] with zero mean    : Inf
## ARIMA(0,0,1)(1,0,0)[12] with non-zero mean : 778.6208
## ARIMA(0,0,1)(1,0,1)[12] with zero mean    : Inf
## ARIMA(0,0,1)(1,0,1)[12] with non-zero mean : 779.7131
## ARIMA(0,0,2)          with zero mean      : 907.2159
## ARIMA(0,0,2)          with non-zero mean  : 791.9724
## ARIMA(0,0,2)(0,0,1)[12] with zero mean    : Inf
## ARIMA(0,0,2)(0,0,1)[12] with non-zero mean : 782.9171
## ARIMA(0,0,2)(1,0,0)[12] with zero mean    : Inf
## ARIMA(0,0,2)(1,0,0)[12] with non-zero mean : 780.6271
```

```

## ARIMA(0,0,2)(1,0,1)[12] with zero mean      : Inf
## ARIMA(0,0,2)(1,0,1)[12] with non-zero mean  : 781.8547
## ARIMA(0,0,3) with zero mean                  : 894.2347
## ARIMA(0,0,3) with non-zero mean              : 790.644
## ARIMA(0,0,3)(0,0,1)[12] with zero mean      : Inf
## ARIMA(0,0,3)(0,0,1)[12] with non-zero mean  : 782.7132
## ARIMA(0,0,3)(1,0,0)[12] with zero mean      : Inf
## ARIMA(0,0,3)(1,0,0)[12] with non-zero mean  : 780.7328
## ARIMA(0,0,3)(1,0,1)[12] with zero mean      : Inf
## ARIMA(0,0,3)(1,0,1)[12] with non-zero mean  : 782.8134
## ARIMA(0,0,4) with zero mean                  : Inf
## ARIMA(0,0,4) with non-zero mean              : 790.0069
## ARIMA(0,0,4)(0,0,1)[12] with zero mean      : 858.5537
## ARIMA(0,0,4)(0,0,1)[12] with non-zero mean  : 784.3248
## ARIMA(0,0,4)(1,0,0)[12] with zero mean      : Inf
## ARIMA(0,0,4)(1,0,0)[12] with non-zero mean  : 782.8422
## ARIMA(0,0,5) with zero mean                  : Inf
## ARIMA(0,0,5) with non-zero mean              : 787.4745
## ARIMA(1,0,0) with zero mean                  : 833.2195
## ARIMA(1,0,0) with non-zero mean              : 791.1376
## ARIMA(1,0,0)(0,0,1)[12] with zero mean      : 824.8455
## ARIMA(1,0,0)(0,0,1)[12] with non-zero mean  : 781.4753
## ARIMA(1,0,0)(1,0,0)[12] with zero mean      : Inf
## ARIMA(1,0,0)(1,0,0)[12] with non-zero mean  : 778.6238
## ARIMA(1,0,0)(1,0,1)[12] with zero mean      : Inf
## ARIMA(1,0,0)(1,0,1)[12] with non-zero mean  : 779.7377
## ARIMA(1,0,1) with zero mean                  : Inf
## ARIMA(1,0,1) with non-zero mean              : 792.5145
## ARIMA(1,0,1)(0,0,1)[12] with zero mean      : Inf
## ARIMA(1,0,1)(0,0,1)[12] with non-zero mean  : 782.803
## ARIMA(1,0,1)(1,0,0)[12] with zero mean      : Inf
## ARIMA(1,0,1)(1,0,0)[12] with non-zero mean  : 780.7184
## ARIMA(1,0,1)(1,0,1)[12] with zero mean      : Inf
## ARIMA(1,0,1)(1,0,1)[12] with non-zero mean  : 782.291
## ARIMA(1,0,2) with zero mean                  : Inf
## ARIMA(1,0,2) with non-zero mean              : 793.6809
## ARIMA(1,0,2)(0,0,1)[12] with zero mean      : Inf
## ARIMA(1,0,2)(0,0,1)[12] with non-zero mean  : 784.6528
## ARIMA(1,0,2)(1,0,0)[12] with zero mean      : Inf
## ARIMA(1,0,2)(1,0,0)[12] with non-zero mean  : 782.5433
## ARIMA(1,0,2)(1,0,1)[12] with zero mean      : Inf
## ARIMA(1,0,2)(1,0,1)[12] with non-zero mean  : 784.137
## ARIMA(1,0,3) with zero mean                  : Inf
## ARIMA(1,0,3) with non-zero mean              : 792.4993
## ARIMA(1,0,3)(0,0,1)[12] with zero mean      : Inf
## ARIMA(1,0,3)(0,0,1)[12] with non-zero mean  : 785.0136
## ARIMA(1,0,3)(1,0,0)[12] with zero mean      : Inf
## ARIMA(1,0,3)(1,0,0)[12] with non-zero mean  : 783.1365
## ARIMA(1,0,4) with zero mean                  : Inf
## ARIMA(1,0,4) with non-zero mean              : 788.8028
## ARIMA(2,0,0) with zero mean                  : 824.0601
## ARIMA(2,0,0) with non-zero mean              : 792.3004
## ARIMA(2,0,0)(0,0,1)[12] with zero mean      : 814.1226
## ARIMA(2,0,0)(0,0,1)[12] with non-zero mean  : 783.2925

```

```

## ARIMA(2,0,0)(1,0,0)[12] with zero mean      : Inf
## ARIMA(2,0,0)(1,0,0)[12] with non-zero mean  : 780.6224
## ARIMA(2,0,0)(1,0,1)[12] with zero mean      : 809.0495
## ARIMA(2,0,0)(1,0,1)[12] with non-zero mean  : 781.6862
## ARIMA(2,0,1) with zero mean                  : Inf
## ARIMA(2,0,1) with non-zero mean             : 792.7482
## ARIMA(2,0,1)(0,0,1)[12] with zero mean      : Inf
## ARIMA(2,0,1)(0,0,1)[12] with non-zero mean  : Inf
## ARIMA(2,0,1)(1,0,0)[12] with zero mean      : Inf
## ARIMA(2,0,1)(1,0,0)[12] with non-zero mean  : 782.2036
## ARIMA(2,0,1)(1,0,1)[12] with zero mean      : Inf
## ARIMA(2,0,1)(1,0,1)[12] with non-zero mean  : 783.8318
## ARIMA(2,0,2) with zero mean                  : Inf
## ARIMA(2,0,2) with non-zero mean             : Inf
## ARIMA(2,0,2)(0,0,1)[12] with zero mean      : Inf
## ARIMA(2,0,2)(0,0,1)[12] with non-zero mean  : 782.2635
## ARIMA(2,0,2)(1,0,0)[12] with zero mean      : Inf
## ARIMA(2,0,2)(1,0,0)[12] with non-zero mean  : Inf
## ARIMA(2,0,3) with zero mean                  : Inf
## ARIMA(2,0,3) with non-zero mean             : 792.2954
## ARIMA(3,0,0) with zero mean                  : Inf
## ARIMA(3,0,0) with non-zero mean             : 789.6905
## ARIMA(3,0,0)(0,0,1)[12] with zero mean      : 813.255
## ARIMA(3,0,0)(0,0,1)[12] with non-zero mean  : 782.134
## ARIMA(3,0,0)(1,0,0)[12] with zero mean      : 808.3923
## ARIMA(3,0,0)(1,0,0)[12] with non-zero mean  : 780.3886
## ARIMA(3,0,0)(1,0,1)[12] with zero mean      : Inf
## ARIMA(3,0,0)(1,0,1)[12] with non-zero mean  : 782.5533
## ARIMA(3,0,1) with zero mean                  : Inf
## ARIMA(3,0,1) with non-zero mean             : 792.0619
## ARIMA(3,0,1)(0,0,1)[12] with zero mean      : Inf
## ARIMA(3,0,1)(0,0,1)[12] with non-zero mean  : 784.5655
## ARIMA(3,0,1)(1,0,0)[12] with zero mean      : Inf
## ARIMA(3,0,1)(1,0,0)[12] with non-zero mean  : 782.9557
## ARIMA(3,0,2) with zero mean                  : Inf
## ARIMA(3,0,2) with non-zero mean             : Inf
## ARIMA(4,0,0) with zero mean                  : Inf
## ARIMA(4,0,0) with non-zero mean             : 791.9508
## ARIMA(4,0,0)(0,0,1)[12] with zero mean      : Inf
## ARIMA(4,0,0)(0,0,1)[12] with non-zero mean  : 784.4907
## ARIMA(4,0,0)(1,0,0)[12] with zero mean      : Inf
## ARIMA(4,0,0)(1,0,0)[12] with non-zero mean  : 782.9545
## ARIMA(4,0,1) with zero mean                  : Inf
## ARIMA(4,0,1) with non-zero mean             : 793.4599
## ARIMA(5,0,0) with zero mean                  : Inf
## ARIMA(5,0,0) with non-zero mean             : 793.1683
##
##
## Best model: ARIMA(0,0,0)(1,0,0)[12] with non-zero mean

```

```
auto_fit
```

```
## Series: train_tng
```

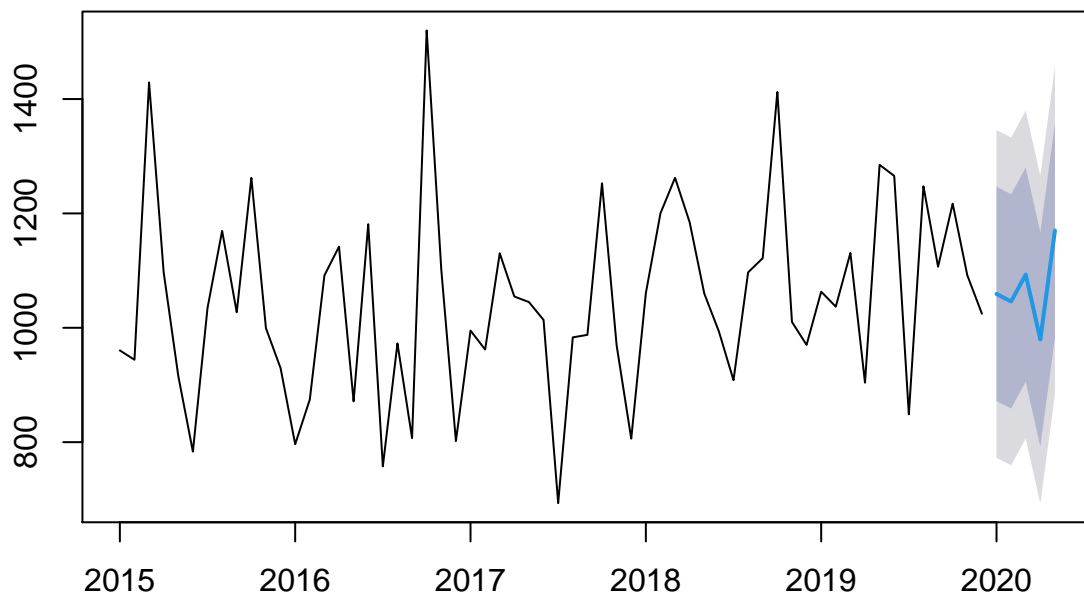
```
## ARIMA(0,0,0)(1,0,0)[12] with non-zero mean
##
## Coefficients:
##          sar1      mean
##          0.5000 1055.231
## s.e.  0.1131    31.467
##
## sigma^2 estimated as 21383:  log likelihood=-384.96
## AIC=775.91   AICc=776.34   BIC=782.2
```

```
forecast_ts = forecast(auto_fit, h=5)
forecast_ts
```

```
##          Point Forecast    Lo 80    Hi 80    Lo 95    Hi 95
## Jan 2020      1059.1806  871.7783 1246.583  772.5735 1345.788
## Feb 2020      1046.0905  858.6882 1233.493  759.4834 1332.698
## Mar 2020      1093.0509  905.6486 1280.453  806.4438 1379.658
## Apr 2020       979.5999  792.1976 1167.002  692.9928 1266.207
## May 2020      1170.0915  982.6892 1357.494  883.4844 1456.699
```

```
plot(forecast_ts)
```

Forecasts from ARIMA(0,0,0)(1,0,0)[12] with non-zero mean



```
summary(forecast_ts)
```

```

##
## Forecast method: ARIMA(0,0,0)(1,0,0)[12] with non-zero mean
##
## Model Information:
## Series: train_tng
## ARIMA(0,0,0)(1,0,0)[12] with non-zero mean
##
## Coefficients:
##          sar1      mean
##          0.5000 1055.231
## s.e.    0.1131   31.467
##
## sigma^2 estimated as 21383:  log likelihood=-384.96
## AIC=775.91   AICc=776.34   BIC=782.2
##
## Error measures:
##              ME      RMSE      MAE      MPE      MAPE      MASE      ACF1
## Training set 1.170595 143.773 113.7024 -1.853976 11.13907 0.8131972 0.01549854
##
## Forecasts:
##      Point Forecast    Lo 80    Hi 80    Lo 95    Hi 95
## Jan 2020      1059.1806 871.7783 1246.583 772.5735 1345.788
## Feb 2020      1046.0905 858.6882 1233.493 759.4834 1332.698
## Mar 2020      1093.0509 905.6486 1280.453 806.4438 1379.658
## Apr 2020       979.5999 792.1976 1167.002 692.9928 1266.207
## May 2020      1170.0915 982.6892 1357.494 883.4844 1456.699

```

Here we can see that the `stl_decomp` forecast has the lowest value of MAPE. Therefore, we consider `stl_decomp` as our forecasting model.