

1. Question- Analyse the worst-case and best-case Time & space complexity of the following algorithms. (Also add the Reason with it)

1. Linear Search.
2. Binary Search.
3. Bubble Sort.
4. Selection sort.
5. Insertion sort
6. Merge sort.

1. Linear Search:

A. Best Case Time Complexity: $O(1)$

- The best case is when the element being searched for is present at the beginning of the array, requiring only one comparison.

B. Worst Case Time Complexity: $O(n)$

- The worst case is when the element being searched for is present at the end of the array or not present at all, requiring n comparisons.

C. Space Complexity: $O(1)$

- Linear search doesn't require any extra space beyond the input array.

2. Binary Search:

A. Best Case Time Complexity: $O(1)$

- The best case is when the element being searched for is at the middle of the sorted array, requiring only one comparison.

B. Worst Case Time Complexity: $O(\log n)$

- The worst case is when the element being searched for is at either end of the sorted array, requiring $\log n$ comparisons.

C. Space Complexity: $O(1)$

- Binary search doesn't require any extra space beyond the input array.

3. Bubble Sort:

A. Best Case Time Complexity: $O(n)$

- The best case is when the input array is already sorted, requiring only n comparisons and no swaps.

B. Worst Case Time Complexity: $O(n^2)$

- The worst case is when the input array is in reverse order, requiring n^2 comparisons and swaps.

C. Space Complexity: $O(1)$

- Bubble sort sorts the array in place and doesn't require any extra space beyond the input array.

4. Selection Sort:

A. Best Case Time Complexity: $O(n^2)$

- The best case is the same as the worst case since the algorithm always makes n^2 comparisons and swaps.

- B. Worst Case Time Complexity: $O(n^2)$
 - The worst case is when the input array is in reverse order, requiring n^2 comparisons and swaps.
- C. Space Complexity: $O(1)$
 - Selection sort sorts the array in place and doesn't require any extra space beyond the input array.

5. Insertion Sort:

- A. Best Case Time Complexity: $O(n)$
 - The best case is when the input array is already sorted, requiring only n comparisons and no swaps.
- B. Worst Case Time Complexity: $O(n^2)$
 - The worst case is when the input array is in reverse order, requiring n^2 comparisons and swaps.
- C. Space Complexity: $O(1)$
 - Insertion sort sorts the array in place and doesn't require any extra space beyond the input array.

6. Merge Sort:

- A. Best Case Time Complexity: $O(n \log n)$
 - The best case is the same as the worst case since the algorithm always makes $n \log n$ comparisons and requires $n \log n$ space to store the intermediate arrays.
- B. Worst Case Time Complexity: $O(n \log n)$
 - The worst case is when the input array is in reverse order, requiring $n \log n$ comparisons and swaps.
- C. Space Complexity: $O(n)$
 - Merge sort requires extra space to store the intermediate arrays during the merging process. The space complexity is proportional to the size of the input array.