

* Red-Black Tree

A red black is a self balancing binary search tree where each node has an extra color bit
Black / Red

Properties

- Every node is either Red or black
- The root is always Black.
- All leaves are Black.
- Red node cannot have a red parent / no two red nodes can be adjacent.
- Every path from a node to its descendant leaves must have same no of black nodes

Step I :- Insert new node with color red.

Step II

Case 1 :- Node is Root recolor it to black.

Case 2 :- Red red violation

• If new node parent is red

Case 2.1 Uncle is red.

→ Recolor parent & uncle to black & grandparent to red. Repeat fixup process from grandparent

Case 2.2 Uncle is black / null.

→ Perform rotation to balance the tree
→ Recolor nodes accordingly

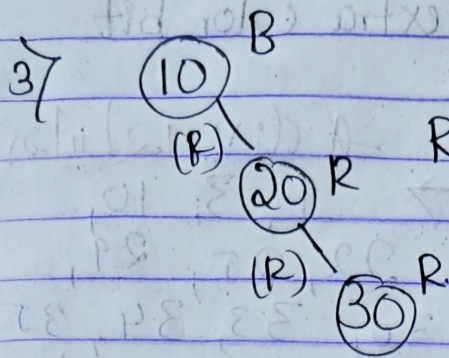
Eg 10, 20, 30, 15, 25, 5, 12, 35, 40, 32, 50

Three basic operations :- Recolor

Rotation.

Rotation followed by Recolor

1) $(10) R \Rightarrow (10) B$ 2) $(10) B$
 $(20) R$

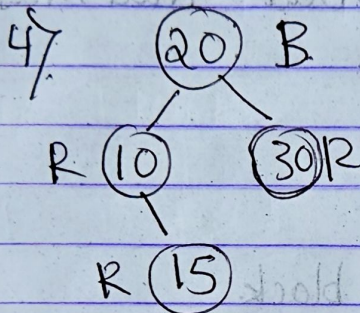
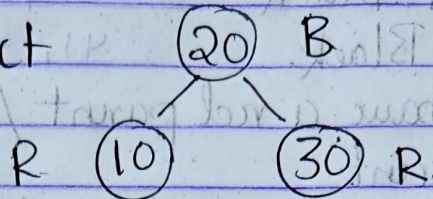


Red-Red conflict

Uncle of 30

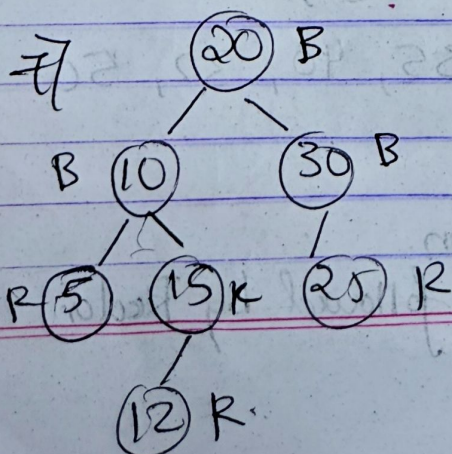
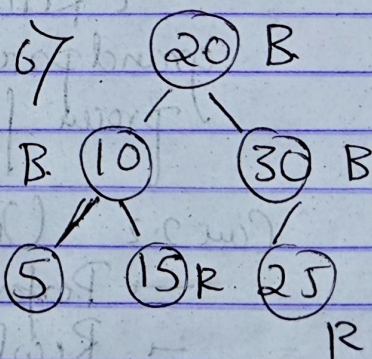
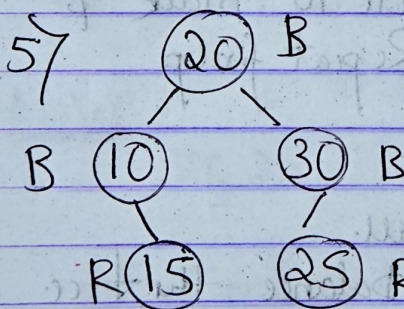
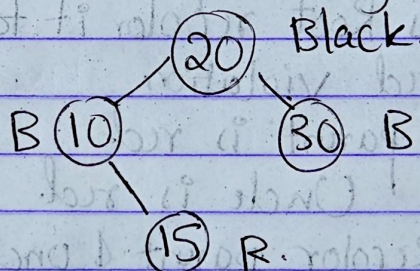
no uncle.
 parent so
 rotation

\rightarrow RR conflict

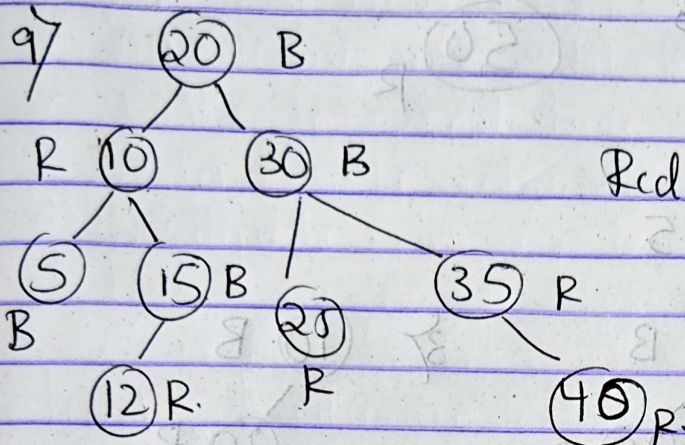
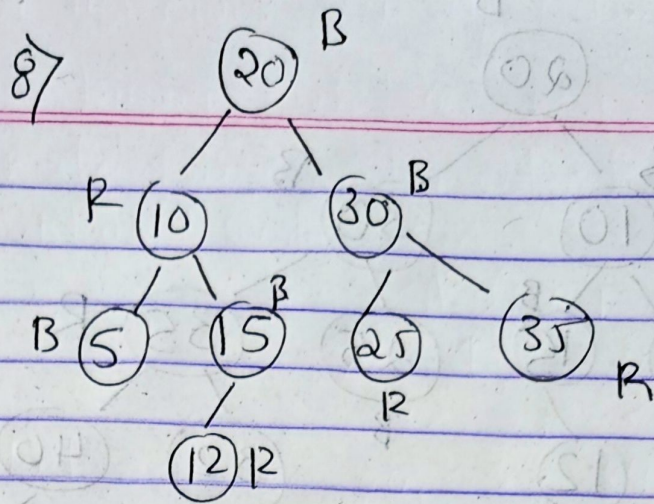
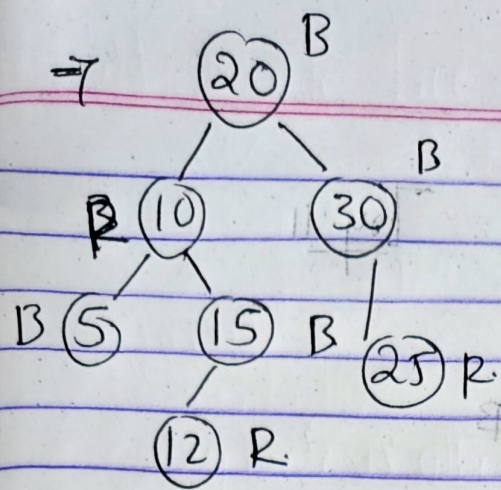


Uncle of 15 is 30 & it is Red color
 - color parent, Uncle \rightarrow black
 \rightarrow grandparent - red

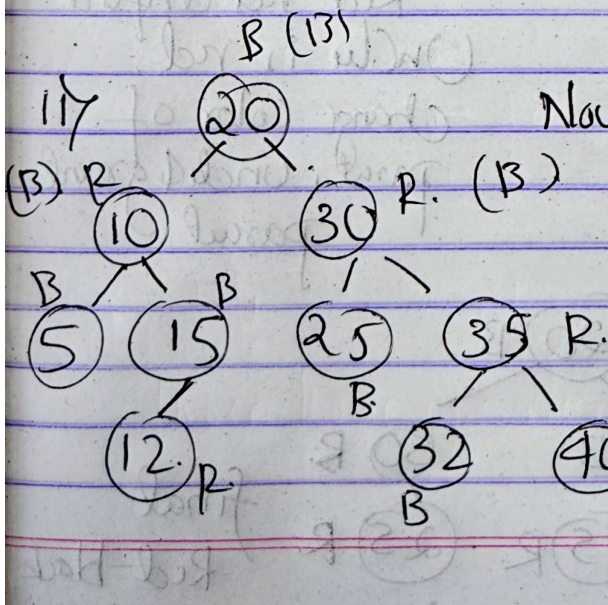
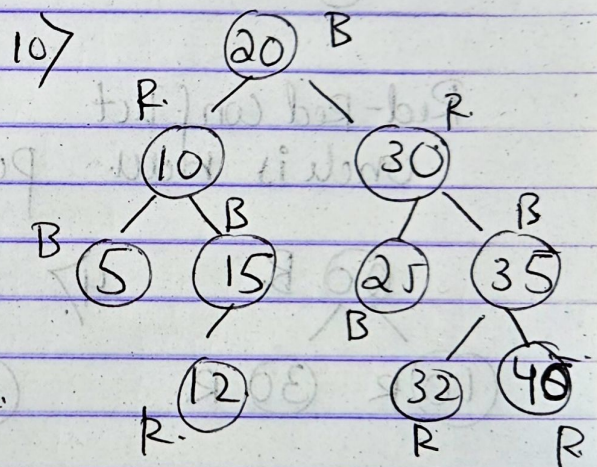
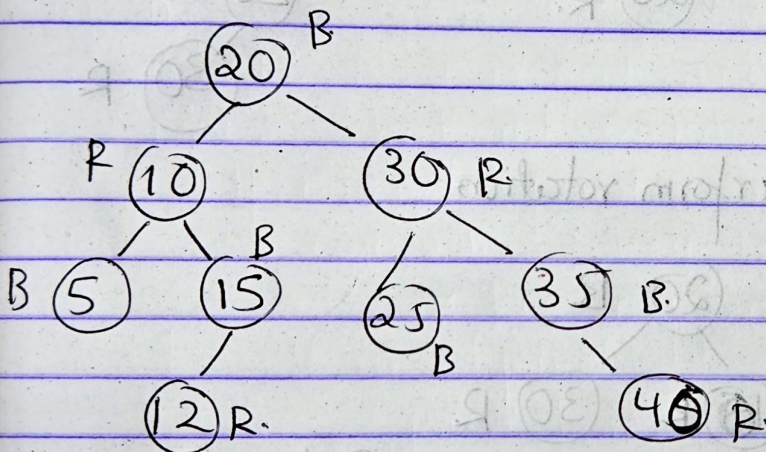
\Rightarrow



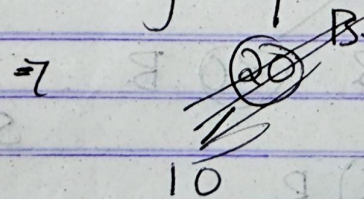
Red-Red conflict
 Uncle is red.

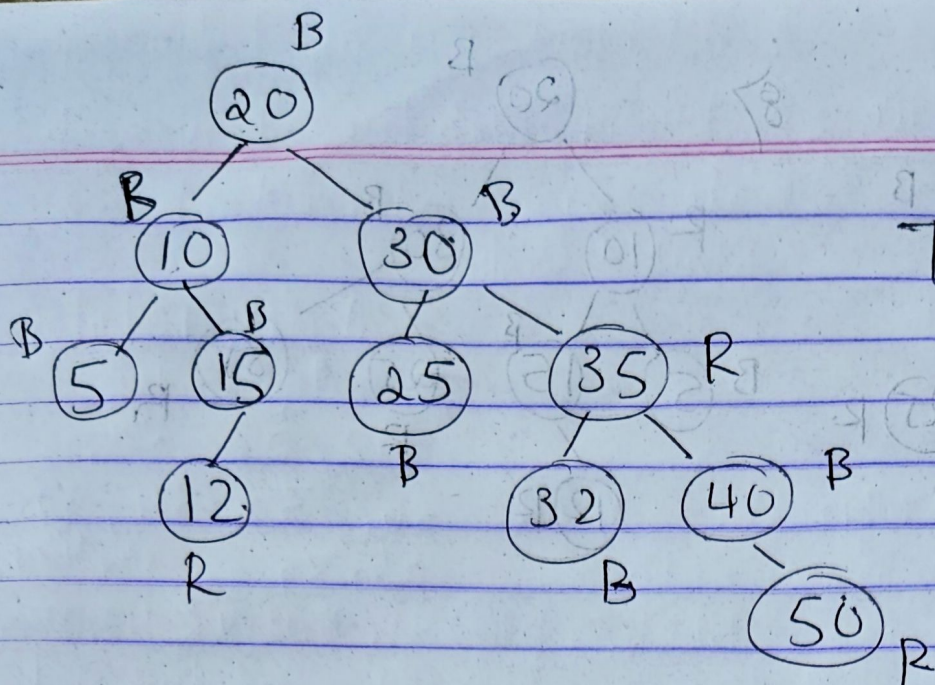


Red Red conflict. 25 is Red
uncolor parent, uncl, gra



Now Red-Red conflict. Change parent,
uncle, grandparent





Try 11

Eg 2

10, 20, 30, 15, 25

17 (10) R.

27.

(10) B

37 (10) B

⇒ (10) B

(20) R.

(20) R

(30) R

Red-Red conflict

uncle is red.

perform rotation

(20) B.

47.

(20) B.

(10) R

(30) R.

(10) R

(30) R

(15) R

Red-red conflict

Uncle is red

change color of parent, uncle & grand parent

⇒

(20) B

(10) B

(30) B

(15) R.

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(20) B

(10) B

(30) B

(15) R.

(25) R.

final Red-Black Tree.