

AI1110

Assignment 5

Sai Pradeep
AI21BTECH11013

May 22, 2022

Outline

1 Question

2 Solution

EXAMPLE 4.25

Q:- We now assume that $p = 0.6$ and we wish to find n such that the probability that k is between $0.59n$ and $0.61n$ is at least 0.98

Solution

In this case. $p = 0.6$, $q = 0.4$

$$\Pr(0.59n \leq k \leq 0.61n) \approx G\left(\frac{0.61 \times n - 0.6 \times n}{\sqrt{0.4 \times 0.6 \times n}}\right) + G\left(\frac{0.59 \times n - 0.6 \times n}{\sqrt{0.4 \times 0.6 \times n}}\right)$$

$$G(x) = \int_{-\infty}^x \frac{e^{-\frac{y^2}{2}}}{\sqrt{2 \times \pi}} dy$$

$$\text{As } G(-x) = 1 - G(x)$$

$$\Pr(0.59n \leq k \leq 0.61n) \approx G\left(\frac{0.01 \times n}{\sqrt{0.24 \times n}}\right) + G\left(\frac{-0.01 \times n}{\sqrt{0.24 \times n}}\right)$$

Computation

$$\Pr(0.59n \leq k \leq 0.61n) \approx 2 \times G\left(\frac{0.01 \times n}{\sqrt{0.24 \times n}}\right) - 1 \quad (1)$$

Hence,

$$2 \times G\left(\frac{0.01 \times n}{\sqrt{0.24 \times n}}\right) - 1 \geq 0.98 \quad (2)$$

$$G\left(\frac{0.01 \times n}{\sqrt{0.24 \times n}}\right) \geq 0.99 \quad (3)$$

$$\frac{0.01 \times n}{\sqrt{0.24 \times n}} \geq 2.35 \quad (4)$$

$$0.24 \times n \geq \left(\frac{2.35}{0.01}\right)^2 \quad (5)$$

$$(6)$$

Hence, $n > 13254$

The value of n such that the probability that k is between $0.59n$ and $0.61n$ is at least 0.98 is at least 13254 .