

## Binomial probability Distribution

$$f(x) = \binom{n}{x} p^x (1-p)^{n-x}$$

(21) Given success : 23%  $\therefore p = 0.23$   
 $x = 2$   $n = 6$   $(1-p) = 0.77$

(a)  $f(x) = \binom{n}{x} p^x (1-p)^{n-x}$

$$f(2) = \binom{6}{2} p^2 (1-p)^4 = \binom{6}{2} (0.23)^2 (0.77)^4$$

$$= (15) (0.0529) (0.3515)$$

$$f(2) = 0.2789$$

(b)  $P(x \geq 2) = f(2) + f(3) + f(4) + f(5) + f(6)$

$$\left. \begin{array}{l} f(2) = 0.2789 \\ f(3) = 0.1111 \\ f(4) = 0.0249 \\ f(5) = 0.0030 \\ f(6) = 0.0001 \end{array} \right\} = 0.4180 //$$

(c)  $n = 10$   $x = 0$

$$f(0) = \binom{10}{0} (0.23)^0 (0.77)^{10}$$

$$f(0) = 0.0733 //$$



(29) Given  $p = 30\% = 0.30$   $(1-p) = 0.70$

(a)  $n = 10$   $x = 3$

$$f(3) = \binom{10}{3} (0.30)^3 (0.70)^7$$

$$f(3) = 0.2668$$

(b)  $P(X \geq 3) = f(3) + f(4) + f(5) + \dots + f(10).$

$$f(3) = 0.2668$$

$$f(4) = 0.2001$$

$$f(5) = 0.1029$$

$$f(6) = 0.0368$$

$$f(7) = 0.0090$$

$$f(8) = 0.0014$$

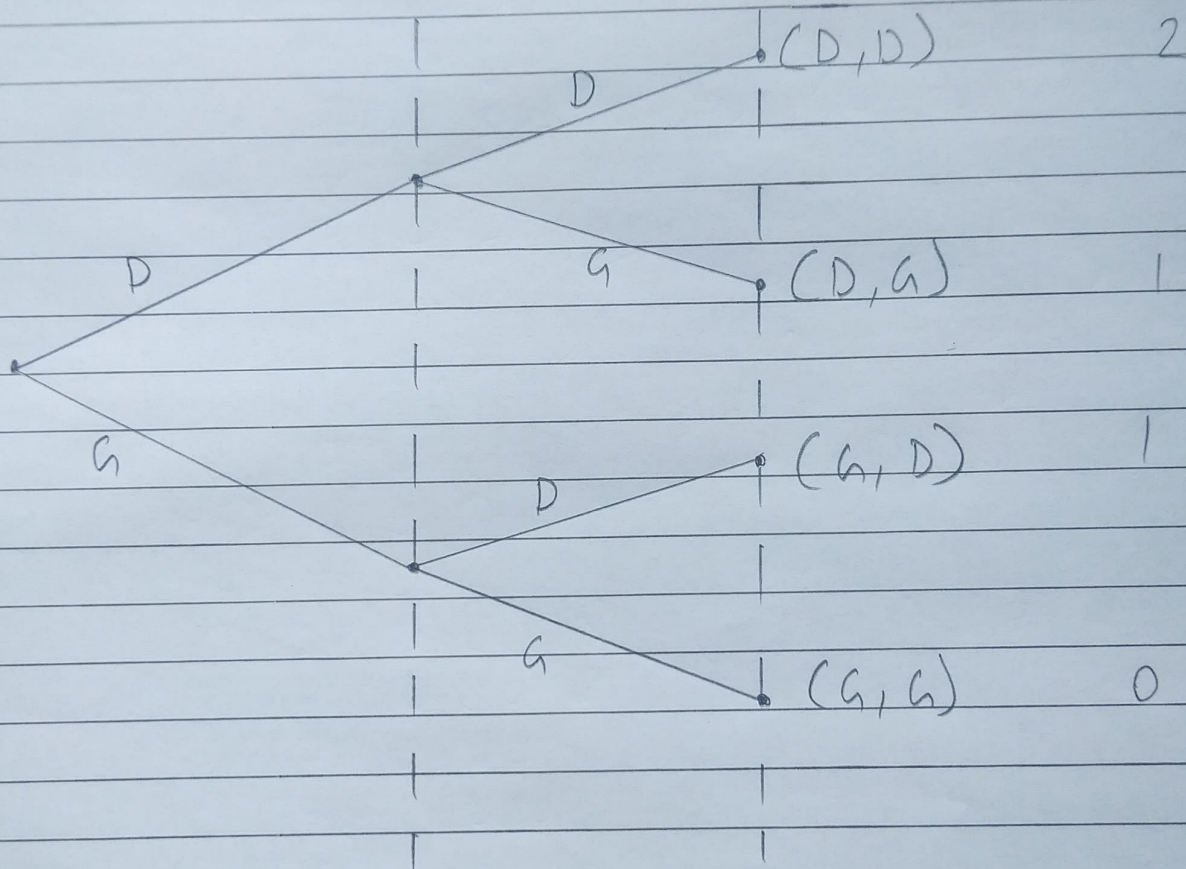
$$f(9) = 0.0001$$

$$f(10) = 0.0000$$

$$= 0.6171$$

(30) (a) Probability of a defective part being produced must be 0.03 for each part selected. parts must be selected independently.

(b) 1st part      2nd part outcome      no of defects



(c) Two outcomes with exactly one defective found.

$$(a) P(\text{no defects}) = \binom{2}{0} (0.03)^0 (0.97)^2 = 0.9409$$

$$P(1 \text{ defects}) = \binom{2}{1} (0.03)^1 (0.97)^1 = 0.0582$$

$$P(2 \text{ defects}) = \binom{2}{2} (0.03)^2 (0.97)^0 = 0.0009$$