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ROLL NO : 10

CLASS : MCA-II

SUBJECT : CONM

Q(1): Evaluate Integral of $(e^x x^2) \sin x$ dx from 0 to 1 using Trapezoidal rule correct to 3 decimal places

```
#include<stdio.h>
```

```
#include<conio.h>
```

```
#include<math.h>
```

```
#define epsilon 0.0005
```

```
void trapezoidal(double,double,int);
```

```
double f(double x)
```

```
{
```

```
    return (exp(x*x)*sin(x));
```

```
}
```

```
void main()
```

```
{
```

```
    int N=2;
```

```
    double a,b;
```

```
    a=0;
```

```
    b=1;
```

```
    trapezoidal(a,b,N);
```

```
    getch();
```

```
}
```

```

void trapezoidal(double a,double b,int N)
{
    int i,limit=20,k=1;

    double sum=0,old_sum=0,h;

    printf("=====Trapezoidal
Rule=====\\n\\n");

    printf("\\nSr No\\t\\t|\\tN\\t\\t|\\th\\t\\t|\\tIntegral\\n");

    printf("_____");
    while(k<=limit)
    {
        sum=0;
        h=(b-a)/N;
        for(i=1;i<N;i++)
        {
            sum+=2*f(a+i*h);
        }
        sum+=(f(a)+f(b));
        sum *=h/2;
        printf("\\n%d\\t\\t|\\t%d\\t\\t|\\t%lf\\t\\t|\\t%lf",k,N,h,sum);
        if(fabs(sum-old_sum)<epsilon)
        {
            printf("\\n\\n-->The Estimate of the Integral is %lf",sum);
            break;
        }
        N*=2;
        k++;
        old_sum=sum;
    }
}

```

output:

=====Trapezoidal

Rule=====

| Sr No | | N | | h | | Integral |
|-------|--|---|--|---|--|----------|
|-------|--|---|--|---|--|----------|

| | | | | | | |
|---|--|----|--|----------|--|----------|
| 1 | | 2 | | 0.500000 | | 0.879636 |
| 2 | | 4 | | 0.250000 | | 0.804736 |
| 3 | | 8 | | 0.125000 | | 0.785295 |
| 4 | | 16 | | 0.062500 | | 0.780386 |
| 5 | | 32 | | 0.031250 | | 0.779156 |
| 6 | | 64 | | 0.015625 | | 0.778848 |

-->The Estimate of the Integral is 0.778848

Q(2): Evaluate the integral:

integral of $dx/(1+x)$ from 0 to 1

Using

(i) Simpson's 1/3 Rule correct to six decimal places

(ii) Simpson's 3/8 rule correct to six decimal places

```
#include<stdio.h>
```

```
#include<conio.h>
```

```
#include<math.h>
```

```
#define epsilon 0.0000005
```

```
void simpsons1_3(double,double,int);
```

```
void simpsons3_8(double,double,int);
```

```
double f(double x)
```

```
{
```

```
    return (1/(1+x));
```

```
}
```

```
void main()
```

```
{
```

```
    int N=2;
```

```
    double a,b;
```

```
    a=0;
```

```
    b=2;
```

```
    simpsons1_3(a,b,N);
```

```
    simpsons3_8(a,b,N);
```

```
    getch();
```

```
}
```

```

void simpsons1_3(double a,double b,int N)
{
    printf("=====Simpsons 1/3
Rule=====\\n\\n");

    int i,limit=20,k=1;

    double sum=0,old_sum=0,h;

    printf("\\nSr No\\t\\t|\\tN\\t\\t|\\th\\t\\t|\\tIntegral\\n");

    printf("_____
_____");

    while(k<=limit)
    {
        sum=0;

        h=(b-a)/N;

        for(i=1;i<N;i++)
        {
            if(i%2==0)

                sum+=2*f(a+i*h);

            else

                sum+=4*f(a+i*h);

        }

        sum+=(f(a)+f(b));

        sum *=h/3;

        printf("\\n%d\\t\\t|\\t%d\\t\\t|\\t%lf\\t\\t|\\t%lf",k,N,h,sum);

        if(fabs(sum-old_sum)<epsilon)
        {

            printf("\\n\\n-->The Estimate of the Integral Using simpsons1/3 Rule is
%lf",sum);

            break;

        }

        N*=2;

        k++;
    }
}

```

```

        old_sum=sum;
    }
    printf("\n\n");
}

void simpsons3_8(double a,double b,int N)
{
    printf("=====Simpsons 3/8
Rule=====\\n\\n");
    int i,limit=20,k=1;
    double sum=0,old_sum=0,h;
    printf("\\nSr No\\t\\t|\\tN\\t\\t|\\th\\t\\t|\\tIntegral\\n");
    printf("_____");
    while(k<=limit)
    {
        sum=0;
        h=(b-a)/N;
        for(i=1;i<N;i++)
        {
            if(i%3==0)
                sum+=2*f(a+i*h);
            else
                sum+=3*f(a+i*h);
        }
        sum+=(f(a)+f(b));
        sum *=3*h/8;
        printf("\\n%d\\t\\t|\\t%d\\t\\t|\\t%lf\\t\\t|\\t%lf",k,N,h,sum);
        if(fabs(sum-old_sum)<epsilon)
        {
            printf("\\n\\n-->The Estimate of the Integral Using simpsons3/8 Rule is
%lf",sum);

```

```

        break;
    }
    N*=2;
    k++;
    old_sum=sum;
}
}

```

output:

=====Simpsons 1/3
Rule=====

| Sr No | N | h | Integral |
|-------|----|----------|----------|
| 1 | 2 | 1.000000 | 1.111111 |
| 2 | 4 | 0.500000 | 1.100000 |
| 3 | 8 | 0.250000 | 1.098725 |
| 4 | 16 | 0.125000 | 1.098620 |
| 5 | 32 | 0.062500 | 1.098613 |
| 6 | 64 | 0.031250 | 1.098612 |

-->The Estimate of the Integral Using simpsons1/3 Rule is 1.098612

=====Simpsons 3/8
Rule=====

| Sr No | N | h | Integral |
|-------|---|---|----------|
|-------|---|---|----------|

| | | | | | | |
|----|--|------|--|----------|--|----------|
| 1 | | 2 | | 1.000000 | | 1.062500 |
| 2 | | 4 | | 0.500000 | | 1.056250 |
| 3 | | 8 | | 0.250000 | | 1.087541 |
| 4 | | 16 | | 0.125000 | | 1.087999 |
| 5 | | 32 | | 0.062500 | | 1.095955 |
| 6 | | 64 | | 0.031250 | | 1.095995 |
| 7 | | 128 | | 0.015625 | | 1.097958 |
| 8 | | 256 | | 0.007813 | | 1.097960 |
| 9 | | 512 | | 0.003906 | | 1.098449 |
| 10 | | 1024 | | 0.001953 | | 1.098449 |

-->The Estimate of the Integral Using simpsons3/8 Rule is 1.098449

Q(3): A car laps a race track in 84 seconds. The speed of the car at each 6-second interval is determined by using a radar gun and is given from the beginning of the lap, in feet/second by the entries in the following table.

Time 0 6 12 18 24 30 36 42 48 54 60 66 72 78 84

Speed 124 134 148 156 147 133 121 109 99 85 78 89 104 116 123

How long is the track?

Use (i) Trapezoidal Rule (ii) Simpson's $1/3$ rule (iii) Simpson's $3/8$ rule

```
#include<stdio.h>
```

```
#include<conio.h>
```

```
#include<math.h>
```

```
void simpsons1_3(double,double,int);
```

```
void simpsons3_8(double,double,int);
```

```
void trapezoidal(double,double,int);
```

```
double f(int x)
```

```
{
```

```
    switch(x)
```

```
    {
```

```
        case 0:return 124;
```

```
        case 6:return 134;
```

```
        case 12:return 148;
```

```
        case 18:return 156;
```

```
        case 24:return 147;
```

```
        case 30:return 133;
```

```
        case 36:return 121;
```

```
        case 42:return 109;
```

```
        case 48:return 99;
```

```

        case 54: return 85;

        case 60: return 78;

        case 66: return 89;

        case 72: return 104;

        case 78: return 116;

        case 84: return 123;

    }

}

void main()
{
    int N=14;

    double a,b;

    a=0;

    b=84;

    trapezoidal(a,b,N);

    simpsons1_3(a,b,N);

    simpsons3_8(a,b,N);

    getch();

}

void trapezoidal(double a,double b,int N)
{
    int i;

    double sum=0,h;

    sum=0;

    h=(b-a)/N;

    for(i=1;i<N;i++)
    {
        sum+=2*f(a+i*h);
    }

    sum+=(f(a)+f(b));
}

```

```

        sum *=h/2;

        printf("\n-->Length of track using Trapezoidal Rule=%0.2lf Feet",sum);
    }

void simpsons1_3(double a,double b,int N)
{
    int i;
    double sum=0,h;
    sum=0;
    h=(b-a)/N;
    for(i=1;i<N;i++)
    {
        if(i%2==0)
            sum+=2*f(a+i*h);
        else
            sum+=4*f(a+i*h);
    }
    sum+=(f(a)+f(b));
    sum *=h/3;
    printf("\n-->Length of track using Simpsons 1/3 Rule=%0.2lf Feet",sum);
}

void simpsons3_8(double a,double b,int N)
{
    int i;
    double sum=0,h;
    sum=0;
    h=(b-a)/N;
    for(i=1;i<N;i++)
    {
        if(i%3==0)

```

```

        sum+=2*f(a+i*h);
    else
        sum+=3*f(a+i*h);
    }
    sum+=(f(a)+f(b));
    sum *=3*h/8;
    printf("\n-->Length of track using Simpsons 3/8 Rule=%0.2lf Feet",sum);
}

```

output:

-->Length of track using Trapezoidal Rule=9855.00 Feet

-->Length of track using Simpsons 1/3 Rule=9858.00 Feet

-->Length of track using Simpsons 3/8 Rule=9760.50 Feet

Q(4): Write a program to solve the differential equation $dy/dx=(y-x)/(y+x)$, where $y(0) = 1$, using

(i) Euler's method

(ii) Runge - Kutta second order method

in the interval 0 to 1 using step-size 0.1 Tabulate your results

```
#include<stdio.h>
```

```
#include<conio.h>
```

```
#include<math.h>
```

```
void euler(double,double,double,int);
```

```
void runge_kutta_2(double,double,double,int);
```

```
double f(double x,double y)
```

```
{
```

```
    return ((y-x)/(y+x));
```

```
}
```

```
void main()
```

```
{
```

```
    int limit;
```

```
    double xi,yi,h;
```

```
    xi=0;
```

```
    yi=1;
```

```
    h=0.1;
```

```
    limit=1;
```

```
    euler(xi,yi,h,limit);
```

```
    runge_kutta_2(xi,yi,h,limit);
```

```
    getch();
```

```
}
```

```
void euler(double xi,double yi,double h,int limit)
```

```

{

    double yi_1;

    yi_1=yi;

    printf("=====EULER METHOD=====\\n\\n");

    printf("\\nx\\t\\t|\\tSolution\\n");

    printf("_____\\n");

    while(xi<=limit)

    {

        yi=yi_1;

        printf("\\n%0.2lf\\t\\t|\\t%lf",xi,yi);

        yi_1=yi + h* f(xi,yi);

        xi+=h;

    }

    printf("\\n\\n-->Solution With Eulers method= %lf\\n\\n",yi);

}

```

```

void runge_kutta_2(double xi,double yi,double h,int limit)

{

    double yi_1,k0,k1;

    yi_1=yi;

    printf("=====RUNGE-KUTTA SECOND ORDER METHOD=====\\n\\n");

    printf("\\nx\\t\\t|\\tSolution\\n");

    printf("_____");

    while(xi<=limit)

    {

        yi=yi_1;

        printf("\\n%0.2lf\\t\\t|\\t%lf",xi,yi);

        k0=h*f(xi,yi);

        k1=h*f(xi+h,yi+k0);

        yi_1=yi + (0.5)*(k0+k1);

        xi+=h;

    }

}

```

```

    }

    printf("\n\n-->Solution With RUNGE-KUTTA SECOND ORDER METHOD= %lf",yi);

}

```

output:

=====EULER METHOD=====

| x | | Solution |
|---|--|----------|
|---|--|----------|

| | | |
|------|--|----------|
| 0.00 | | 1.000000 |
| 0.10 | | 1.100000 |
| 0.20 | | 1.183333 |
| 0.30 | | 1.254418 |
| 0.40 | | 1.315818 |
| 0.50 | | 1.369193 |
| 0.60 | | 1.415694 |
| 0.70 | | 1.456161 |
| 0.80 | | 1.491231 |
| 0.90 | | 1.521399 |
| 1.00 | | 1.547062 |

-->Solution With Eulers method= 1.547062

=====RUNGE-KUTTA SECOND ORDER METHOD=====

| x | | Solution |
|---|--|----------|
|---|--|----------|

| | | |
|------|--|----------|
| 0.00 | | 1.000000 |
| 0.10 | | 1.091667 |
| 0.20 | | 1.168728 |
| 0.30 | | 1.234629 |
| 0.40 | | 1.291489 |
| 0.50 | | 1.340729 |
| 0.60 | | 1.383361 |
| 0.70 | | 1.420135 |
| 0.80 | | 1.451627 |
| 0.90 | | 1.478291 |
| 1.00 | | 1.500491 |

-->Solution With RUNGE-KUTTA SECOND ORDER METHOD= 1.500491

Q(5): Find the solution of differential equation, for the range $0 \leq t \leq 1$ $dy/dt = t + (y)^{(1/2)}$
with $y(0) = 1$, taking step size $h = 0.2$ using Runge-Kutta method of order 4

```
#include<stdio.h>
```

```
#include<conio.h>
```

```
#include<math.h>
```

```
void runge_kutta_4(double,double,double,int);
```

```
double f(double t,double y)
```

```
{
```

```
    return (t+sqrt(y));
```

```
}
```

```
void main()
```

```
{
```

```
    int limit;
```

```
    double ti,yi,h;
```

```
    ti=0;
```

```
    yi=1;
```

```
    h=0.2;
```

```
    limit=1;
```

```
    runge_kutta_4(ti,yi,h,limit);
```

```
    getch();
```

```
}
```

```
void runge_kutta_4(double ti,double yi,double h,int limit)
```

```
{
```

```
    double yi_1,k0,k1,k2,k3;
```

```
    yi_1=yi;
```

```
    printf("=====RUNGE-KUTTA FORTH ORDER METHOD=====\n\n");
```

```

printf("\nt\t\t\t\t\tSolution\n");
printf("_____");
while(ti<=limit)
{
    yi=yi_1;
    printf("\n%0.2lf\t\t\t\t\t",ti,yi);
    k0=h*f(ti,yi);
    k1=h*f(ti+(h/2),yi+(k0/2));
    k2=h*f(ti+(h/2),yi+(k1/2));
    k3=h*f(ti+h,yi+k2);
    yi_1=yi + (k0+2*k1+2*k2+k3)/6;
    ti+=h;
}
printf("\n\n-->Solution With RUNGE-KUTTA FORTH ORDER METHOD= %lf",yi);
}

```

output:

=====RUNGE-KUTTA FORTH ORDER METHOD=====

| t | | Solution |
|------|--|----------|
| 0.00 | | 1.000000 |
| 0.20 | | 1.230632 |
| 0.40 | | 1.524809 |
| 0.60 | | 1.885413 |
| 0.80 | | 2.314716 |
| 1.00 | | 2.814506 |

-->Solution With RUNGE-KUTTA FORTH ORDER METHOD= 2.814506

Q(6): Find the solution of differential equation $dy/dt = 1/2 (t+y)$, for $y(2.0)$ given

$$y(0) = 2$$

$$y(0.5) = 2.636$$

$$y(1.0) = 3.595$$

$$\text{and } y(1.5) = 4.968, \text{ use } h = 0.5$$

using (i) Milne-Simpson's predictor corrector method

(ii) Adam-Bashforth-Moulton's predictor-corrector method

```
#include<stdio.h>
```

```
#include<conio.h>
```

```
#include<math.h>
```

```
#define epsilon 0.00005
```

```
void milne_simpsons_predictor_corrector(double[],double[],double);
```

```
void adam_bashforth_moultons_predictor_corrector(double[],double[],double);
```

```
double f(double t,double y)
```

```
{
```

```
    return ((t+y)/2);
```

```
}
```

```
void main()
```

```
{
```

```
    double h,y[10],t[10];
```

```
    h=0.5;
```

```
    y[0]=2;
```

```
    y[1]=2.636;
```

```
    y[2]=3.595;
```

```
    y[3]=4.968;
```

```
    t[0]=0;
```

```
    t[1]=0.5;
```

```

t[2]=1.0;
t[3]=1.5;
t[4]=2.0;
milne_simpsons_predictor_corrector(y,t,h);
adam_bashforth_moultons_predictor_corrector(y,t,h);
getch();
}

void milne_simpsons_predictor_corrector(double y[],double t[],double h)
{
    double yi_old=0;
    int i;
    i=3;
    printf("====milne_simpsons_predictor_corrector METHOD====\n\n");
    //predictor Method
    y[i+1]=y[i-3]+(4*h)*(2*f(t[i],y[i])-f(t[i-1],y[i-1])+2*f(t[i-2],y[i-2]))/3;
    printf("Using Predictor Formula y4=%lf",y[i+1]);

    //Corrector formula
    while(fabs(yi_old-y[i+1])>epsilon)
    {
        yi_old=y[i+1];
        y[i+1]=y[i-1] + (h/3) *(f(t[i+1],y[i+1])+ 4* f(t[i],y[i])+f(t[i-1],y[i-1]));
        printf("\n-->Using Corrector Formula y4=%lf",y[i+1]);
    }

    printf("\n\n---->Solution With milne_simpsons_predictor_corrector METHOD=
%lf\n\n",y[i+1]);
}

void adam_bashforth_moultons_predictor_corrector(double y[],double t[],double h)
{

```

```

double yi_old=0;

int i;

i=3;

printf("=====adam_bashforth_moultons_predictor_corrector METHOD=====\n\n");

//predictor Method

y[i+1]=y[i]+(h/24)*(55*f(t[i],y[i])-59*f(t[i-1],y[i-1])+37*f(t[i-2],y[i-2])-9*f(t[i-3],y[i-3]));

printf("Using Predictor Formula y4 =%lf",y[i+1]);


//Corrector formula

while(fabs(yi_old-y[i+1])>epsilon)

{

    yi_old=y[i+1];

    y[i+1]=y[i] + (h/24) *(9*f(t[i+1],y[i+1])+ 19 * f(t[i],y[i])-5*f(t[i-1],y[i-1])+f(t[i-2],y[i-2]));

    printf("\n-->Using Corrector Formula y4=%lf",y[i+1]);

}

printf("\n\n---->Solution With adam_bashforth_moultons_predictor_corrector METHOD=

%lf",y[i+1]);

}

```

output:

=====milne_simpsons_predictor_corrector METHOD=====

Using Predictor Formula y4 =6.871000

-->Using Corrector Formula y4=6.873167

-->Using Corrector Formula y4=6.873347

-->Using Corrector Formula y4=6.873362

---->Solution With milne_simpsons_predictor_corrector METHOD= 6.873362

=====adam_bashforth_moultons_predictor_corrector METHOD=====

Using Predictor Formula $y_4 = 6.870781$

-->Using Corrector Formula $y_4 = 6.873104$

-->Using Corrector Formula $y_4 = 6.873322$

-->Using Corrector Formula $y_4 = 6.873343$

---->Solution With adam_bashforth_moultons_predictor_corrector METHOD= 6.873343

Q(7): Use Adam-Bashforth-Moulton's predictor-corrector method to obtain the solution of the equation $dy/dx = 1 - xy/x^2$ at $x = 1.4$, where $y(1) = 1$.

Compute $y(1.1)$, $y(1.2)$ and $y(1.3)$ using Runge-Kutta second order method.

Tabulate the results obtained thus.

```
#include<stdio.h>
```

```
#include<conio.h>
```

```
#include<math.h>
```

```
#define epsilon 0.00005
```

```
void adam_bashforth_moultons_predictor_corrector(double[],double[],double);
```

```
double runge_kutta_2(double,double,double,double);
```

```
double f(double x,double y)
```

```
{
```

```
    return ((1-x*y)/(x*x));
```

```
}
```

```
void main()
```

```
{
```

```
    double h,y[10],x[10];
```

```
    h=0.1;
```

```
    x[0]=1;
```

```
    x[1]=1.1;
```

```
    x[2]=1.2;
```

```
    x[3]=1.3;
```

```
    x[4]=1.4;
```

```
    y[0]=1;
```

```
    y[1]=runge_kutta_2(x[0],y[0],h,1.2);
```

```
    y[2]=runge_kutta_2(x[0],y[0],h,1.3);
```

```

y[3]=runge_kutta_2(x[0],y[0],h,1.4);

printf("\n=====By Runge-Kutta second order method\n");
printf("y(1.1)=%lf\n y(1.2)=%lf\n y(1.3)=%lf\n",y[1],y[2],y[3]);
adam_bashforth_moultons_predictor_corrector(y,x,h);
getch();
}

void adam_bashforth_moultons_predictor_corrector(double y[],double x[],double h)
{
    double yi_old=0;
    int i;
    i=3;
    printf("=====adam_bashforth_moultons_predictor_corrector METHOD=====\n\n");
    //predictor Method
    y[i+1]=y[i]+(h/24)*(55*f(x[i],y[i])-59*f(x[i-1],y[i-1])+37*f(x[i-2],y[i-2])-9*f(x[i-3],y[i-3]));
    printf("Using Predictor Formula y(1.4) =%lf",y[i+1]);

    //Corrector formula
    while(fabs(yi_old-y[i+1])>epsilon)
    {
        yi_old=y[i+1];
        y[i+1]=y[i] + (h/24) *(9*f(x[i+1],y[i+1])+ 19 * f(x[i],y[i])-5*f(x[i-1],y[i-1])+f(x[i-2],y[i-
2])));
        printf("\n-->Using Corrector Formula y(1.4)=%lf",y[i+1]);
    }

    printf("\n\n---->Solution With adam_bashforth_moultons_predictor_corrector METHOD=
%lf",y[i+1]);
}

double runge_kutta_2(double xi,double yi,double h,double limit)

```



```

{
    double yi_1,k0,k1;
    yi_1=yi;
    while(xi<limit)
    {
        yi=yi_1;
        k0=h*f(xi,yi);
        k1=h*f(xi+h,yi+k0);
        yi_1=yi + (0.5)*(k0+k1);
        xi+=h;
    }
    return yi;
}

```

output:

=====By Runge-Kutta second order method

$y(1.1)=0.995868$

$y(1.2)=0.985480$

$y(1.3)=0.971311$

=====adam_bashforth_moultons_predictor_corrector METHOD=====

Using Predictor Formula $y(1.4)=0.954695$

-->Using Corrector Formula $y(1.4)=0.954878$

-->Using Corrector Formula $y(1.4)=0.954873$

---->Solution With adam_bashforth_moultons_predictor_corrector METHOD= 0.954873

Q(8): Use Milne Simpson predictor corrector method to obtain the solution of the equation $dy/dx = 1 - xy/x^2$ at $x = 1.4$, where $y(1) = 1$.
Compute $y(1.1)$, $y(1.2)$ and $y(1.3)$ using Runge-Kutta fourth order method.
Tabulate the results obtained thus.

```
#include<stdio.h>
#include<conio.h>
#include<math.h>
#define epsilon 0.00005

void milne_simpsons_predictor_corrector(double[],double[],double);
double runge_kutta_4(double,double,double,double);
double f(double x,double y)
{
    return ((1-x*y)/(x*x));
}
void main()
{
    double h,y[10],x[10];
    h=0.1;
    x[0]=1;
    x[1]=1.1;
    x[2]=1.2;
    x[3]=1.3;
    x[4]=1.4;

    y[0]=1;
    y[1]=runge_kutta_4(x[0],y[0],h,1.2);
    y[2]=runge_kutta_4(x[0],y[0],h,1.3);
```

```

y[3]=runge_kutta_4(x[0],y[0],h,1.4);

printf("\n=====By Runge-Kutta Forth order method\n");
printf("y(1.1)=%lf\n y(1.2)=%lf\n y(1.3)=%lf\n",y[1],y[2],y[3]);
milne_simpsons_predictor_corrector(y,x,h);
getch();
}

void milne_simpsons_predictor_corrector(double y[],double x[],double h)
{
    double yi_old=0;
    int i;
    i=3;
    printf("=====milne_simpsons_predictor_corrector METHOD=====\n\n");
    //predictor Method
    y[i+1]=y[i-3]+(4*h)*(2*f(x[i],y[i])-f(x[i-1],y[i-1])+2*f(x[i-2],y[i-2]))/3;
    printf("Using Predictor Formula y(1.4)=%lf",y[i+1]);

    //Corrector formula
    while(fabs(yi_old-y[i+1])>epsilon)
    {
        yi_old=y[i+1];
        y[i+1]=y[i-1] + (h/3) *(f(x[i+1],y[i+1])+ 4* f(x[i],y[i])+f(x[i-1],y[i-1]));
        printf("\n-->Using Corrector Formula y(1.4)=%lf",y[i+1]);
    }

    printf("\n\n---->Solution With milne_simpsons_predictor_corrector METHOD=
    %lf\n\n",y[i+1]);
}

double runge_kutta_4(double xi,double yi,double h,double limit)
{
    double yi_1,k0,k1,k2,k3;

```

```

    yi_1=yi;
    while(xi<limit)
    {
        yi=yi_1;
        k0=h*f(xi,yi);
        k1=h*f(xi+(h/2),yi+(k0/2));
        k2=h*f(xi+(h/2),yi+(k1/2));
        k3=h*f(xi+h,yi+k2);
        yi_1=yi + (k0+2*k1+2*k2+k3)/6;
        xi+=h;
    }
    return yi;
}

```

output:

=====By Runge-Kutta Forth order method

y(1.1)=0.995737

y(1.2)=0.985268

y(1.3)=0.971050

=====milne_simpsons_predictor_corrector METHOD=====

Using Predictor Formula $y(1.4)=0.954478$

-->Using Corrector Formula $y(1.4)=0.954629$

-->Using Corrector Formula $y(1.4)=0.954626$

---->Solution With milne_simpsons_predictor_corrector METHOD= 0.954626

Q(9): From the following table estimate $y'(1.1)$ and $y'(1.2)$ using 3 point formulas and 5 point formulas

x 1.0 1.05 1.10 1.15 1.20 1.25 1.30

y 1.0 1.0247 1.0488 1.0724 1.0954 1.1180 1.1402

```
#include<stdio.h>
```

```
#include<conio.h>
```

```
#include<math.h>
```

```
void _3point_formulas(double[],double[],double);
```

```
void _5point_formulas(double[],double[],double);
```

```
void main()
```

```
{
```

```
    double x[10],y[10],h=0.5;
```

```
    x[0]=1.0;
```

```
    x[1]=1.05;
```

```
    x[2]=1.10;
```

```
    x[3]=1.15;
```

```
    x[4]=1.20;
```

```
    x[5]=1.25;
```

```
    x[6]=1.30;
```

```
    y[0]=1.0;
```

```
    y[1]=1.0247;
```

```
    y[2]=1.0488;
```

```
    y[3]=1.0724;
```

```
    y[4]=1.0954;
```

```
    y[5]=1.1180;
```

```
    y[6]=1.1402;
```

```

    _3point_formulas(x,y,h);
    _5point_formulas(x,y,h);
    getch();
}

```

```

void _3point_formulas(double x[],double y[],double h)

```

```

{

    double x0=x[2],ans;
    int i=2;
    //Endpoint formula
    printf("\n=====3 Pont End Point Formula=====\\n");
    ans=(1/(2*h)) * (-3 * y[i] + 4*y[i+1]-y[i+2]);
    printf("\n--->y(1.1)'=%lf",ans);
    i=4;
    ans=(1/(2*h)) * (-3 * y[i] + 4*y[i+1]-y[i+2]);
    printf("\n--->y(1.2)'=%lf",ans);
    //Midpoint Formula
    i=2;
    printf("\n=====3 Pont Mid Point Formula=====\\n");
    ans=(1/(2*h)) * (-y[i-1] + y[i+1]);
    printf("\n--->y(1.1)'=%lf",ans);
    i=4;
    ans=(1/(2*h)) * (-y[i-1] + y[i+1]);
    printf("\n--->y(1.2)'=%lf",ans);
    //Endpoint formula
    printf("\n=====3 Pont End Point Formula=====\\n");
    i=2;
    ans=(1/(2*h)) * (y[i-2] - 4*y[i-1]+3*y[i]);
    printf("\n--->y(1.1)'=%lf",ans);

```

```

        i=4;

        ans=(1/(2*h)) * (y[i-2] - 4*y[i-1]+3*y[i]);

        printf("\n--->y(1.2)'=%lf",ans);

    }

```

```

void _5point_formulas(double x[],double y[],double h)

```

```

{

    double x0=x[2],ans;

    int i=2;

    //Endpoint formula

    printf("\n\n\n=====5 Pont End Point Formula=====\\n");

    ans=(1/(12*h)) * ( -25*y[i] +48*y[i+1]-36* y[i+2]+16*y[i+3]-3*y[i+4]);

    printf("\n--->y(1.1)'=%lf",ans);


    //Midpoint Formula

    i=2;

    printf("\n=====5 Pont Mid Point Formula=====\\n");

    ans=(1/(12*h)) * ( y[i-2] - 8*y[i-1]+8* y[i+1]-y[i+2]);

    printf("\n--->y(1.1)'=%lf",ans);

    i=4;

    ans=(1/(12*h)) * ( y[i-2] - 8*y[i-1]+8* y[i+1]-y[i+2]);

    printf("\n--->y(1.2)'=%lf",ans);

}

```

```

*****

```

output:

```

=====3 Pont End Point Formula=====

```

$$\text{---}>y(1.1)'=0.047800$$

$$\text{---}>y(1.2)'=0.045600$$

=====3 Pont Mid Point Formula=====

$$\text{---}>y(1.1)'=0.047700$$

$$\text{---}>y(1.2)'=0.045600$$

=====3 Pont End Point Formula=====

$$\text{---}>y(1.1)'=0.047600$$

$$\text{---}>y(1.2)'=0.045400$$

=====5 Pont End Point Formula=====

$$\text{---}>y(1.1)'=0.048033$$

=====5 Pont Mid Point Formula=====

$$\text{---}>y(1.1)'=0.047700$$

$$\text{---}>y(1.2)'=0.045567$$
