

Latihan Konvolusi 2D



$x(n_1, n_2)$

$$\begin{array}{|c|} \hline 1 & 4 & 1 \\ \hline 2 & 5 & 3 \\ \hline 0 & & \end{array}$$

$h(n_1, n_2)$

$$\begin{array}{|c|} \hline 1 & 1 \\ \hline 1 & -1 \\ \hline 0 & \end{array}$$

Konvolusikan sinyal ~~tersebut~~ di atas tersebut.

$$y(n_1, n_2) = \sum_{k_1=-\infty}^{\infty} \sum_{k_2=-\infty}^{\infty} x(k_1, k_2) h(n_1 - k_1, n_2 - k_2)$$

Jawab

* Cerminkan $h(n_1, n_2)$

$$\begin{array}{|c|} \hline -1 & 1 \\ \hline 1 & 1 \\ \hline \end{array}$$

* Lalu, dikonvolusikan

(I)

$$\begin{array}{|c|} \hline 1 & 4 & 1 \\ \hline -1 & (1-2) & 5 & 3 \\ \hline 1 & 1 & \end{array} \leftrightarrow -1(0) + (2) = 2$$

$$\begin{array}{|c|} \hline 1 & 4 & 1 \\ \hline (-1-2) & (1-5) & 3 \\ \hline 1 & 1 & \end{array} \leftrightarrow -1(2) + (5) = 3$$

$$\begin{array}{|c|} \hline 1 & 4 & 1 \\ \hline 2 & ((-1-5) & (1-3) \\ \hline \end{array} \leftrightarrow (-5) + (3) = -2$$

$$\begin{array}{|c|} \hline 1 & 4 & 1 \\ \hline 2 & 5 & ((-1-3) & 1 \\ \hline 1 & 1 & \end{array} \leftrightarrow (-3) + (0) = -3$$

(II)

$$\begin{array}{|c|} \hline -1 & (1-1) & 4 & 1 \\ \hline 1 & (1-2) & 5 & 3 \\ \hline \end{array} \leftrightarrow 1(1) + (2) = 3$$

$$\begin{array}{|c|} \hline (-1-1) & (1-4) & 1 \\ \hline (1-2) & (1-5) & 3 \\ \hline \end{array} \leftrightarrow (-1) + 4 + 2 + 5 = 10$$

$$\begin{array}{|c|} \hline 1 & (-1-4) & (1-1) \\ \hline 2 & (1-5) & (1-3) \\ \hline \end{array} \leftrightarrow (-4) + 1 + 5 + 3 = 5$$

$$\begin{array}{|c|} \hline 1 & 4 & (-1-1) & 1 \\ \hline 5 & (1-3) & 1 \\ \hline \end{array} \leftrightarrow (-1) + (3) + 1(0) + 1(0) = 2$$

(III)

$$\begin{array}{|c|} \hline -1 & 1 \\ \hline 1 & (1-1) & 4 & 1 \\ \hline 2 & 5 & 3 \\ \hline \end{array} \leftrightarrow (-1) \cdot 0 + 1(0) + 1(0) + 1 = 1$$

$$\begin{array}{|c|} \hline -1 & 1 \\ \hline (1-1) & (1-4) & 1 \\ \hline 2 & 5 & 3 \\ \hline \end{array} \leftrightarrow (1-1) \cdot 0 + 1(0) + 1(1) + 1(4) = 5$$

$$\begin{array}{|c|} \hline -1 & 1 \\ \hline 1 & (1-4) & (1-1) \\ \hline 2 & 5 & 3 \\ \hline \end{array} \leftrightarrow (1-1) \cdot 0 + 1(0) + 1(4) + 1(1) = 5$$

$$\begin{array}{|c|} \hline -1 & 1 \\ \hline 1 & 4 & (1-1) & 1 \\ \hline 2 & 5 & 3 \\ \hline \end{array} \leftrightarrow (1-1) \cdot 0 + 1(0) + 1(1) + 1(0) = 1$$

* maka, hasil akhir konvolusi ini adalah

$$y(n_1, n_2) = \begin{array}{|c|} \hline 1 & 5 & 5 & 1 \\ \hline 3 & 10 & 5 & 2 \\ \hline 2 & 3 & -2 & -3 \\ \hline \end{array}$$