

5. Consider a company that has two different divisions. The annual profits from the two divisions are independent and have distributions Profit1 ~ N(5, 32) and Profit2 ~ N(7, 42) respectively. Both the profits are in Million.
Answer the following questions about the total profit of the company in Rupees. Assume that \$1 = Rs. 45
- A. Specify a Rupee range (centered on the mean) such that it contains 95% probability for the annual profit of the company.
- B. Specify the 5th percentile of profit (in Rupees) for the company
- C. Which of the two divisions has a larger probability of making a loss in a given year?

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In [20]: ▶ import numpy as np
from scipy import stats
from scipy.stats import norm
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In [21]: ▶ # Mean profits from two different divisions of a company = Mean1 + Mean2
Mean = 5+7
print('Mean Profit is Rs', Mean*45,'Million')

Mean Profit is Rs 540 Million
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In [22]: ▶ # Variance of profits from two different divisions of a company = SD^2 = SD1^2 + SD2^2
SD = np.sqrt((9)+(16))
print('Standard Deviation is Rs', SD*45, 'Million')

Standard Deviation is Rs 225.0 Million
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A. Specify a Rupee range (centered on the mean) such that it contains 95% probability for the annual profit of the company.

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In [23]: ▶ print('Range is Rs',(stats.norm.interval(0.95,540,225)), 'in Millions')

Range is Rs (99.00810347848784, 980.9918965215122) in Millions
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B. Specify the 5th percentile of profit (in Rupees) for the company

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In [24]: ▶ # To compute 5th Percentile, we use the formula X=μ + Zσ; wherein from z table, 5 percentile = -1.645
X= 540+(-1.645)*(225)
print('5th percentile of profit (in Million Rupees) is',np.round(X,))

5th percentile of profit (in Million Rupees) is 170.0
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C. Which of the two divisions has a larger probability of making a loss in a given year?

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In [25]: ▶ # Probability of Division 1 making a Loss P(X<0)
stats.norm.cdf(0,5,3)
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Out[25]: 0.0477903522728147

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In [26]: ▶ # Probability of Division 2 making a Loss P(X<0)
stats.norm.cdf(0,7,4)
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Out[26]: 0.040059156863817086

Probability of Division 1 making a loss in a given year is more than Division 2.