

# Probability Density Function And Probability Mass Function

## Cumulative Distribution Function (cdf)

① PMF :

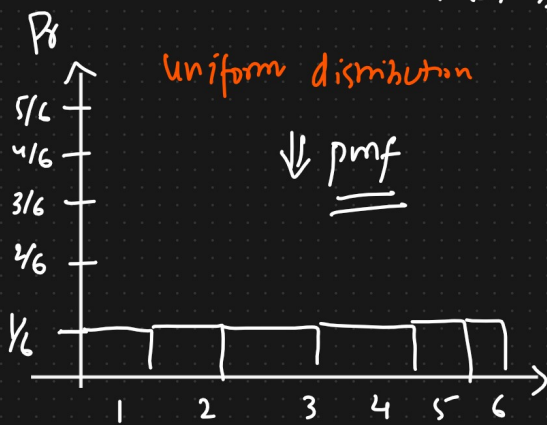
① Discrete Random Variable

PMF

Eg: Rolling a dice

$\{1, 2, 3, 4, 5, 6\}$   $\Pr(1) = 1/6$

$\Pr(2) = 1/6$



$$\Pr(X=1) = \frac{1}{6}$$

$$\Pr(X=2) = \frac{1}{6}$$

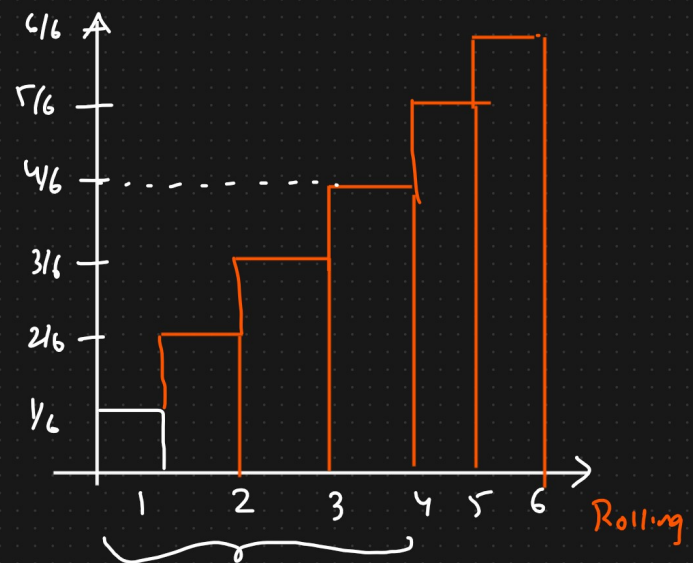
$$\Pr(X \leq 4) = \Pr(X=1) + \Pr(X=2)$$

$$+ \Pr(X=3) + \Pr(X=4)$$

$$= \frac{1}{6} + \frac{1}{6} + \frac{1}{6} + \frac{1}{6} = \frac{4}{6} = \frac{2}{3}$$

CDF

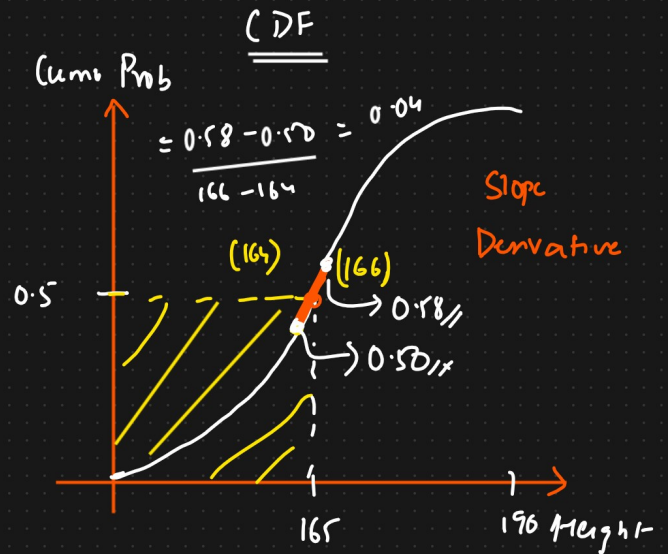
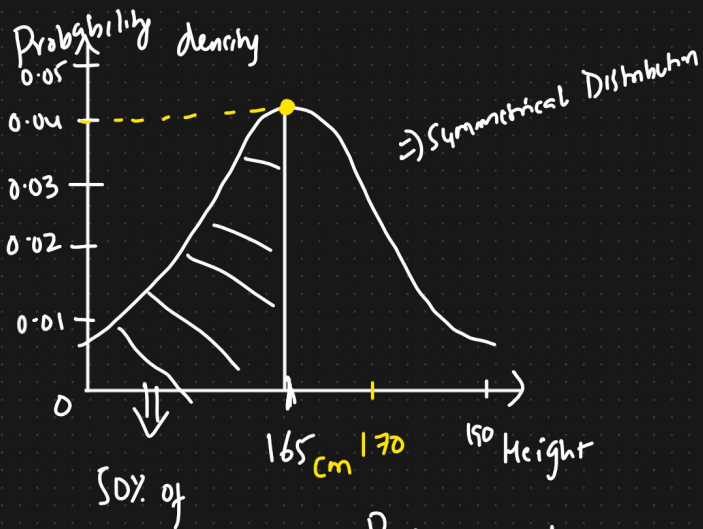
Cumulative Probability



$$\begin{aligned}
 \Pr(X \leq 6) &= \Pr(X=1) + \Pr(X=2) + \Pr(X=3) \\
 &\quad + \Pr(X=4) + \Pr(X=5) + \Pr(X=6) \\
 &= 1
 \end{aligned}$$

## ② Probability Density Function (PDF)

### ① Continuous Random Variable



Probability density  
 ↳ Gradient descent of  
 CDF