

# LAB 2,3: Particle In 1D Box

Date: 22-12-23

## AIM:

1. Consider a quantum particle of mass  $m$  in a 1D infinite potential well of dimension  $L$ . Sketch the wavefunction and probability density using python. Label the X-axis in terms of ' $L$ '. Plot and compare the energy levels of the ground state and the first three excited states for potential well dimensions  $L/2$ ,  $L$ ,  $2L$ . Express energies in units of  $\hbar^2/8mL^2$ .
2. Consider a quantum particle of mass  $m$  in a 1D infinite potential well of dimension  $L$ . Sketch the wavefunction and probability density of first three eigenstates using python. Label the X-axis in terms of ' $L$ '. Investigate the change in amplitude and wavelength of wavefunction as ' $n$ ' increases.

## Particle in a Box

The wavefunctions of a particle in a box of length  $L$  is given as -

$$\psi = \sin \frac{n\pi x}{L}$$

The energy of a state  $n$  is given as -

$$\epsilon = \frac{n^2 \hbar^2}{8mL^2}$$

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In [1]: import numpy as np
import matplotlib.pyplot as plt
from scipy.constants import h
import ipywidgets as widgets
import matplotlib.colors as mcolors
import random
from fractions import Fraction
```

```
In [2]: def wavefunction(x,n = 1,L = 1):
    if(x>L or x<0):
        raise Exception("Particle Outside Box")
    return;
    return np.sin(n*np.pi*x/L)*(2/L)**0.5;
```

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In [3]: # UNIT - h^2/8mL^2
def energy(n,L):
    if(n<0):
        raise Exception("Negative Ground State Not Allowed")
    return;
    return ((n/L)**2)
```

```
In [4]: def plotWave(n = [1],L = 1):
    fig = plt.figure(figsize = (18,4))

    X = np.linspace(0,L,1000)
    for N in n:
        plt.subplot(1,2,1);
        plt.plot(X,[wavefunction(x,N,L) for x in X], label = "n = {0}".format(N))
        plt.title("Wavefunction of Particle in a Box",fontsize = 15)
        plt.subplot(1,2,2);
```

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plt.plot(X,[wavefunction(x,N,L)**2 for x in X], label = "n = {0}".format(N))
plt.title("Probability Density of Particle in a Box",fontsize = 15)

for i in [1,2]:
    plt.subplot(1,2,i)
    plt.xlim(left = 0, right = L);
    plt.grid()
    plt.xticks(ticks = np.linspace(0,L,5), labels = [f"{Fraction(i)}L" for i in np.linspace(0,1,5)])
    plt.legend(fontsize = 15,loc = 3)
#plt.savefig("Wavefunction")
plt.show()

```

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In [5]: def plotEnergy(L = [1],nmax = 5):
        L = list(L)
        L.sort(reverse=True)
        fig = plt.figure(figsize = (15,5))
        color_dict = dict(zip(L,random.choices(list(mcolors.BASE_COLORS.values()))[:2],k = len(L)))
        for l in L:
            plt.axhline(energy(1,l),color = color_dict[l],xmax = 1/L[0],label = f"{l}L",linewidth = 2)
            for n in range(2,nmax+1):
                plt.axhline(energy(n,l),xmax=1/L[0],color = color_dict[l],linewidth = 2*1)
        plt.xlim(right = max(L))
        plt.grid(axis = 'y',which = 'both')
        plt.ylabel('$h^2/8mL^2$',fontsize = 20)

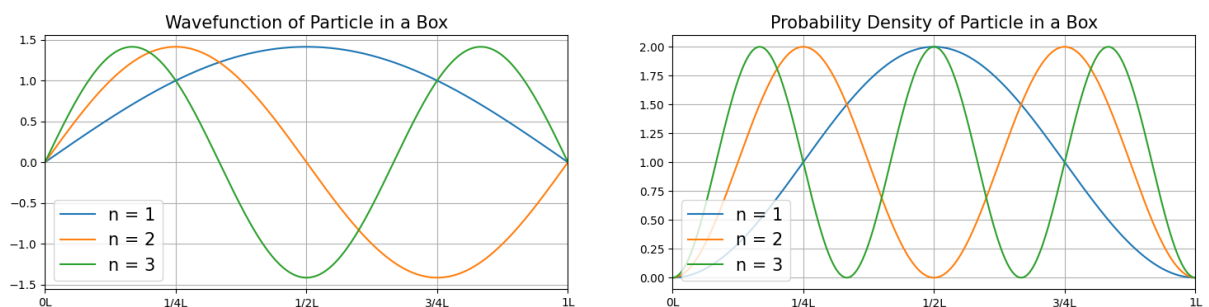
        xloc = plt.xticks()[0]
        plt.xticks(ticks = xloc, labels = [f"{Fraction(i)}L" for i in xloc])
        plt.legend(fontsize = 20)
        #plt.savefig("EnergyDiagram")
        plt.show()

```

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In [6]: plotWave(n = [1,2,3], L = 1)

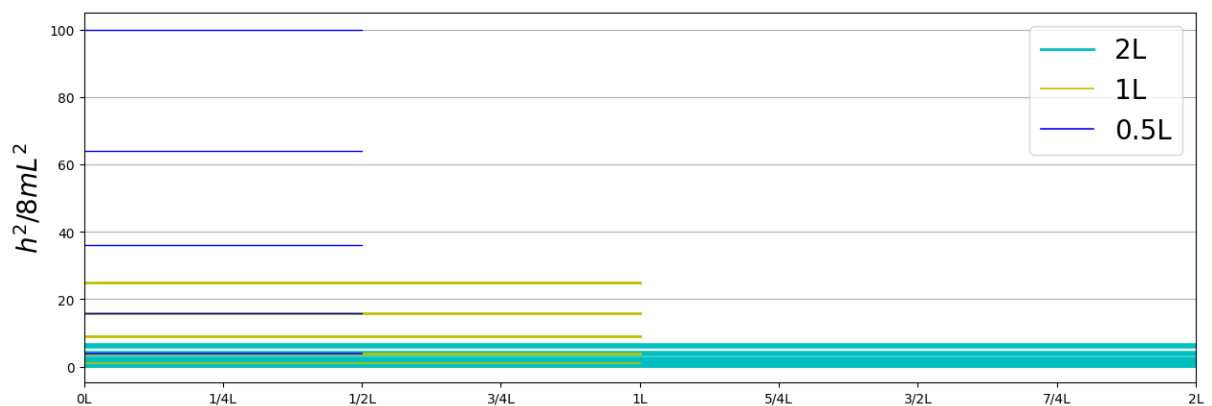
```



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In [7]: plotEnergy([0.5,1,2])

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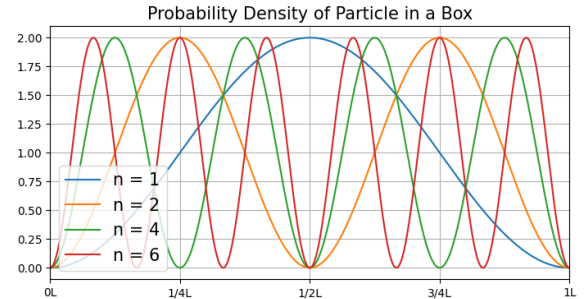
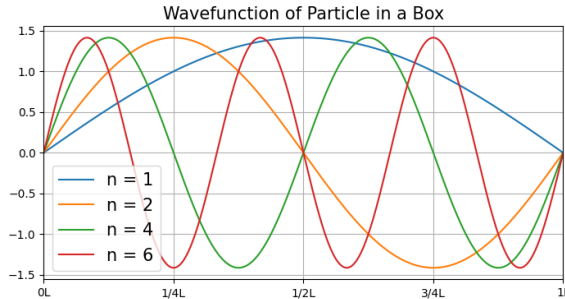
In [8]: widgets.interactive(plotWave,n = widgets.SelectMultiple(
        options=[1,2,3,4,5,6,7,8,9,10],
        value=[1],
        rows=10,
        description='N = ',
        disabled=False),L = widgets.fixed(1))

```

Out[8]:

N =

1
2
3
4
5
6
7
8
9
10



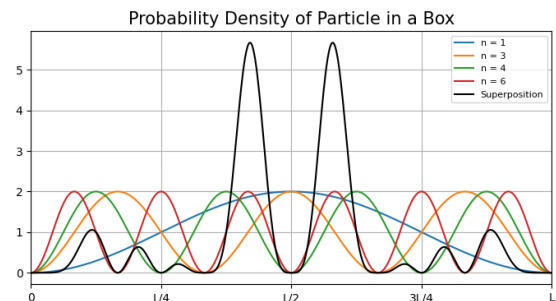
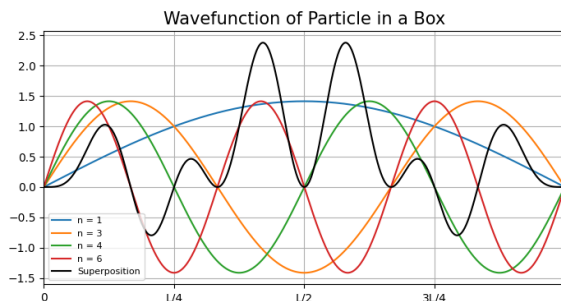
```
In [9]: def superpositionWave(n = [1], L = 1):
fig = plt.figure(figsize = (18,4))
X = np.linspace(0,L,1000)
psi = np.ones(len(X))
for N in n:
    plt.subplot(1,2,1);
    psi = np.vstack((psi,np.array([wavefunction(x,N,L) for x in X])))
    plt.plot(X, psi[-1], label = "n = {}".format(N))
    plt.title("Wavefunction of Particle in a Box",fontsize = 15)
    plt.subplot(1,2,2);
    plt.plot(X,psi[-1]**2, label = "n = {}".format(N))
    plt.title("Probability Density of Particle in a Box",fontsize = 15)
plt.subplot(1,2,1);
plt.plot(X, np.cumprod(psi,axis = 0)[-1], label = "Superposition",color = "black")
plt.subplot(1,2,2);
plt.plot(X,np.cumprod(psi,axis = 0)[-1]**2, label = "Superposition",color = "black")
for i in [1,2]:
    plt.subplot(1,2,i)
    plt.xlim(left = 0, right = L);
    #plt.ylim(bottom = -1, top = 1);
    plt.grid()
    plt.xticks([0,L/4,L/2,3*L/4,L],["0","L/4","L/2","3L/4","L"])
    plt.legend(fontsize = 8)
plt.show()

widgets.interactive(superpositionWave,n = widgets.SelectMultiple(
    options=[1,2,3,4,5,6,7,8,9,10],
    value=[1],
    rows=10,
    description='N = ',
    disabled=False),L = widgets.fixed(1))
```

Out[9]:

N =

1
2
3
4
5
6
7
8
9
10



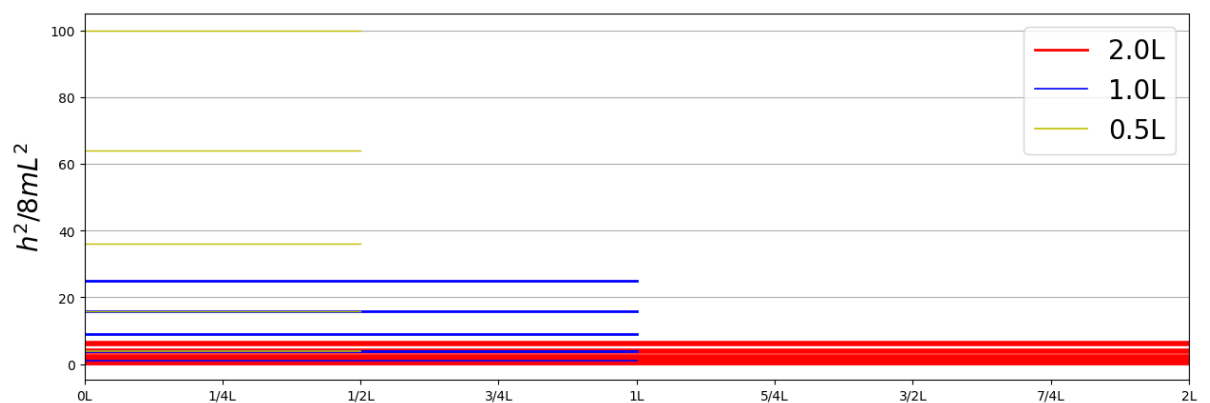
```
In [11]: widgets.interactive(plotEnergy,L = widgets.SelectMultiple(
    options=np.linspace(0.25,2,8),
    value=[1],
    rows=8,
    description='L = ',
    disabled=False
),nmax = widgets.IntSlider(value=5,max=10,min = 1,step=1))
```

Out[11]:

L =

0.25
0.5
0.75
1.0
1.25
1.5
1.75
2.0

nmax  5



In [ ]: