

# Modified K-S Algorithm

## Algorithm

1. Let  $x_i \in B$ , where  $B = \{30.1, 17.6, 12.5, 9.7, 7.9, 6.7, 5.8, 5.1, 4.6\}$  is the expected proportion or Benford's proportion.
2. Let  $y_i \in O$ , where  $O$  is the observed proportion say

$$O = \{y_1, \dots, y_i, \dots, y_9\}.$$

3. Let  $T = \{(x_1, y_1), (x_2, y_2), \dots, (x_9, y_9)\}$ . Find the set of all  $9!$  permutations  $P$ .
4. Calculate

$$D_{p_k} = \max_{1 \leq i \leq j} \left| \sum_{i=1}^j (x_i^{(k)} - y_i^{(k)}) \right|, \quad j = 1, 2, \dots, 9$$

for the  $k$ -th permutation  $p_k$  in  $P$ .

5. Calculate  $\min\{D_{p_k} : p_k \in P \text{ and } k = 1, 2, \dots, 9!\}$ .