

```

format long

t = linspace(0, 1, 50);

% build the vandermonde A matrix with 10 columns
A = VanderMonde(cos(4*t), 10);

b = zeros(50, 1);
x = zeros(10, 1);

% build the vector b
for i = 1:50
    b(i) = cos(4 * t(i));
end

% (a) Formation and solution of the normal equations, using MATLAB s \
Ac = A' * A;
bc = A' * b;
L = chol(Ac, "lower");
y = L \ bc;
xa = L' \ y;

xa

% (b) QR factorization computed by mgs
[Q, R] = mgs(A);
xb = (lsp(b, Q, R))';

xb

% (c) QR factorization computed by house
[V, R] = house(A);
Q = formQ(V);
bh = Q' * b;
xc = R \ bh;

xc

% (d) x = A\b in MATLAB
xd = R \ (Q' * b);

xd

```

xa =

```

-0.0000000000000056
 0.9999999999998957
 0.0000000000001646
 0.00000000000013290
-0.0000000000007876
-0.0000000000046570
 0.0000000000012180
 0.0000000000060982
-0.000000000005922
-0.0000000000026745

```

xb =

Columns 1 through 3

-0.0000000000000001    0.999999999999492    0.0000000000000050

Columns 4 through 6

0.0000000000006089    -0.000000000000319    -0.0000000000020318

Columns 7 through 9

0.0000000000000535    0.0000000000025631    -0.0000000000000265

Column 10

-0.000000000010922

xc =

-0.0000000000000000  
0.9999999999999999  
0.0000000000000001  
0.0000000000000006  
-0.0000000000000004  
-0.0000000000000016  
0.0000000000000003  
0.0000000000000015  
0.0000000000000000  
-0.0000000000000004

xd =

-0.0000000000000000  
0.9999999999999999  
0.0000000000000001  
0.0000000000000006  
-0.0000000000000004  
-0.0000000000000016  
0.0000000000000003  
0.0000000000000015  
0.0000000000000000  
-0.0000000000000004