Discrete Assignment EE1205 Signals and Systems

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Question 11.9.1.2: Write the first five terms of the sequence whose terms are represented by $x_n = \frac{n}{n+1}$

Solution: Given the terms of the sequence are $x_n = \frac{n}{n+1}$ where n = 1, 2, 3, 4...Now

$$x_1 = \frac{1}{2} \tag{1}$$

$$x_2 = \frac{2}{3} \tag{2}$$

$$x_3 = \frac{3}{4} \tag{3}$$

$$x_{1} = \frac{1}{2}$$

$$x_{2} = \frac{2}{3}$$

$$x_{3} = \frac{3}{4}$$

$$x_{4} = \frac{4}{5}$$
(1)
(2)
(3)

$$x_5 = \frac{5}{6} \tag{5}$$

Now,

$$u(n) = \begin{cases} 1 & n \ge 0 \\ 0 & n < 0 \end{cases} \tag{6}$$

In terms of u(n), x_n is

$$x_n = u(n) - \frac{u(n)}{n+1}$$
 (7)

Z-transform is defined as,

$$P(Z) = \sum_{i=-\infty}^{\infty} P(n).Z^{-n}$$
 (8)

Here, Z-transform

$$P(Z) = \sum_{i=1}^{\infty} x(n).Z^{-n}$$
(9)

$$=\sum_{i=1}^{\infty} \frac{n}{n+1} Z^{-n}$$
 (10)

On solving,

$$P(Z) = \frac{Z}{Z - 1} + Z \log (1 - Z^{-1})$$
(11)