Discrete Assignment EE1205 Signals and Systems

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Question 11.9.1.2: Write the first five terms of the sequence whose n^{th} terms $x(n) = \frac{n}{n+1}$ **Solution:** Given the terms of the sequence are $x(n) = \frac{n}{n+1}$ where n = 0, 1, 2, 3, 4... In terms of u(n), x(n) is

$$x(n) = u(n) - \frac{u(n)}{n+1}$$
 (1)

$$x(n) = \begin{cases} 0 & \text{if } x = 0\\ u(n) - \frac{u(n)}{n+1} & \text{if } x > 0\\ \text{not defined} & \text{if } x < 0 \end{cases}$$

Z-transform is defined as,

$$x(n) \stackrel{Z}{\longleftrightarrow} X(Z)$$

$$X(Z) = \sum_{i=-\infty}^{\infty} x(n).Z^{-n}$$
 (2)

Here, Z-transform

$$X(Z) = \sum_{i=1}^{\infty} x(n).Z^{-n}$$
 (3)

$$= \sum_{i=1}^{\infty} \frac{n}{n+1} . Z^{-n}$$
 (4)

On solving,

$$X(Z) = \frac{Z}{Z - 1} + Z \log(1 - Z^{-1})$$
 (5)

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