

Assignment No - 6.



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Title - Prims Algorithm

Problem- Statement- You have a business with several office; you want to lease phone lines to connect them up with each other; and the phone company charges different amounts of money to connect different pairs of cities. You want a set of lines that connect all your office with a minimum total cost. Solve the problem by suggesting appropriate data structures.

objectives -

Student will be able to understand concept of minimum Spanning tree with Prims algorithm.

Software requirement -

1. 64-bit open source linux or its derivative
2. open source c++ programming tool like G++/GCC
3. Turbo c++ compiler.

Theory -

Data structure to be used - Arrays: Two dimensional array (adjacency matrix) to store the adjacent vertices & the weights associated edges. one dimensional array to store an indicator for each vertex whether visited or not.

define max 20.



```
int adj-ver [max] [Max]; int edge-wt [max]  
[Max]; int ind [Max];
```

concepts to be used.

- Arrays
- Function to construct head List & adjacency matrix for a graph.
- Function to display adjacency matrix of a graph.
- Function to generate minimum Spanning Tree for a graph using Prim's algorithm

Spanning Tree - A Spanning Tree of a graph $G=(V,E)$ is sub graph of G having all vertices of G and no cycles is it.

Minimal Spanning Tree - The cost of a graph is the sum of the costs the edges in the weighted graph.

- when a graph G is connected, depth first or breadth first search starting at any vertex visits all the vertices in G .

- The edges of G in T form a tree which includes all the vertices of Graph G and this tree is called Spanning Tree.

Prim's Algorithm - Any Tree, which consists is an algorithm in graph Theory that finds a minimum Spanning Tree.



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This means it finds a subset of the edges that forms a tree that includes every vertex, where the total weight of all the edges in the tree is minimized.

Prims in 1957 and rediscovered by Edsger Dijkstra in 1969.

Algorithm / pseudo code:

Prim's Algorithm - All vertices of a connected graph are included in the minimum spanning tree. Prim's Algorithm starts from one vertex and grows the rest of tree by adding one vertex at a time by adding associated edge in T .

void prims(vertex i)

1. Start
2. initialize visited $[]$ to 0 for $(i=0; i < n; i++)$
visited $[i] = 0;$
3. Find minimum edge from i for $(j=0; j < n; j++)$
 {
 if ($\text{min} > a[i][j]$)
 {
 $\text{min} = a[i][j]$ $x = i;$
 $y = j;$
 }
 }
4. print the edge between i and j with weight.
5. Make visit $[i++] = x.$



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visit[j++] = y

6. Find next minimum edge starting from nodes of visit array.
7. Repeat step 6 until all the nodes are visited.
8. End.

Conclusion - Thus we have studied and implemented a minimum Spanning Tree Concept with the help of Prim's Algorithm.