Simple Knapsack algorithm

Brute force algorithm

- Maximize the value of N elements (wi,vi) while keeping the total weight
- less than a maximum value W.
- Maximize sum(xi*vi) i = 0,...,n and vi = 0 or vi = 1
- Subject to sum(xi*wi) <= W) i = 0,..,n and vi = 0 or vi = 1
- V0 + V1 +V2+ + Vi + + Vn
- 0/1 0/1 0/1 0/1
- This results in 2**n different sums (2**n binary numbers with n bits)

Brute force algorithm

- Requires the computation of 2**n sums
- 20 items \rightarrow 2**20 computations \sim = 10**6
- 40 items \rightarrow 2**40 computations \sim = 10**12
- Complexity O(2**n)
- Only possible for small sets of items

Knapsack algorithm

- Evaluate for all constraints less than maximum constraint W
- The current element is included in the subset when adding it does not exceed the constraint and improves the best value computed in prior iteration

Knapsack algorithm (Wikipedia)

```
// Input:
   // Values (stored in array v)
   // Weights (stored in array w)
   // Number of distinct items (n)
    // Knapsack capacity (W)
    // NOTE: The array "v" and array "w" are assumed to store all relevant values starting at index 1.
   array m[0..n, 0..W];
   for j from 0 to W do:
       m[0, j] := 0
10
   for i from 1 to n do:
11
       m[i, 0] := 0
12
13
    for i from 1 to n do:
14
       for j from 0 to W do:
15
           if w[i] > j then:
16
                m[i, j] := m[i-1, j]
17
18
            else:
                m[i, j] := max(m[i-1, j], m[i-1, j-w[i]] + v[i])
19
```

Knapsack algorithm

- Complexity time O(nw)
- Complexity space O(nw)

Knapsack algorithm: Dataset 1

• Total investment: 499.95

• Total profit: 198.53

• Previous Results

• Total investment: 498.76

• Total profit: 196.61

Knapsack algorithm: Dataset 2

• Total investment: 499.9

• Total profit: 197.95

• Previous Results

• Total investment: 489.24

• Total profit: 193.78

Sienna bought:

Share-GRUT

Share-KMTG	Value:23.21	Profit:9.277037
Share-GHIZ	Value:28.00	Profit:11.169200
Share-NHWA	Value:29.18	Profit:11.604886
Share-UEZB	Value:24.87	Profit:9.806241
Share-LPDM	Value:39.35	Profit:15.629820
Share-MTLR	Value:16.48	Profit:6.587056
Share-USSR	Value:25.62	Profit:10.135272
Share-GTQK	Value:15.40	Profit:6.152300
Share-FKJW	Value:21.08	Profit:8.385624
Share-MLGM	Value:0.01	Profit:0.001886
Share-QLMK	Value:17.38	Profit:6.863362
Share-WPLI	Value:34.64	Profit:13.821360
Share-LGWG	Value:31.41	Profit:12.406950
Share-ZSDE	Value:15.11	Profit:6.025868
Share-SKKC	Value:24.87	Profit:9.821163
Share-QQTU	Value:33.19	Profit:13.143240
Share-GIAJ	Value:10.75	Profit:4.289250
Share-XJMO	Value:9.39	Profit:3.753183
Share-LRBZ	Value:32.90	Profit:13.143550
Share-KZBL	Value:28.99	Profit:11.346686
Share-EMOV	Value:8.89	Profit:3.513328
Share-IFCP	Value:29.23	Profit:11.656924

Sienna bought:		
Share-ECAQ	3166	
Share-IXCI	2632	
Share-FWBE	1830	
Share-ZOFA	2532	
Share-PLLK	1994	
Share-YFVZ	2255	
Share-ANFX	3854	
Share-PATS	2770	
Share-NDKR	3306	
Share-ALIY	2908	
Share-JWGF	4869	
Share-JGTW	3529	
Share-FAPS	3257	
Share-VCAX	2742	
Share-LFXB	1483	
Share-DWSK	2949	
Share-XQII	1342	
Share-ROOM	1506	

Share-ECAQ	Value:31.66	Profit:12.502534
Share-IXCI	Value:26.32	Profit:10.370080
Share-FWBE	Value:18.30	Profit:7.287060
Share-ZOFA	Value:25.32	Profit:10.072296
Share-PLLK	Value:19.94	Profit:7.956060
Share-LXZU	Value:4.24	Profit:1.676496
Share-YFVZ	Value:22.55	Profit:8.817050
Share-ANFX	Value:38.54	Profit:15.308088
Share-PATS	Value:27.70	Profit:11.071690
Share-SCWM	Value:6.42	Profit: 2.446020
Share-NDKR	Value:33.06	Profit:13.190940
Share-ALIY	Value:29.08	Profit:11.611644
Share-JWGF	Value:48.69	Profit:19.441917
Share-JGTW	Value:35.29	Profit:13.914847
Share-FAPS	Value:32.57	Profit:12.878178
Share-VCAX	Value:27.42	Profit:10.691058
Share-LFXB	Value:14.83	Profit:5.900857
Share-DWSK	Value:29.49	Profit:11.604315
Share-XQII	Value:13.42	Profit:5.302242
Share-ROOM	Value:15.06	Profit:5.906532