

# Lecture 14: 24 May, 2021

Madhavan Mukund

<https://www.cmi.ac.in/~madhavan>

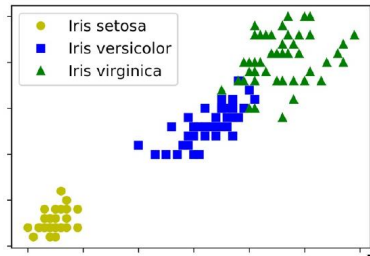
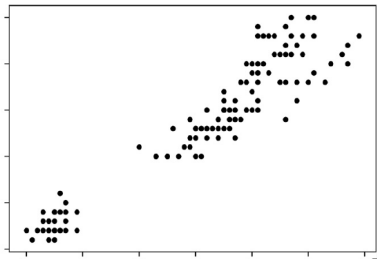
Data Mining and Machine Learning  
April–July 2021

# Unsupervised learning

- Supervised learning requires labelled data
- Vast majority of data is unlabelled
- What insights can you get into unlabelled data?

*"If intelligence was a cake, unsupervised learning would be the cake, supervised learning would be the icing on the cake ..."*

- Yann LeCun  
ACM Turing Award 2018



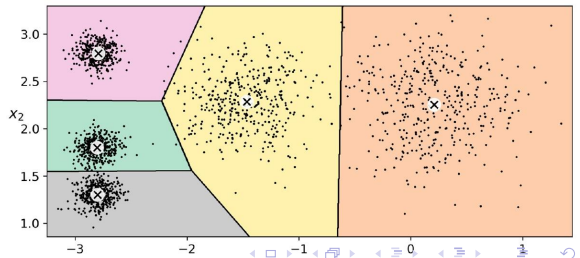
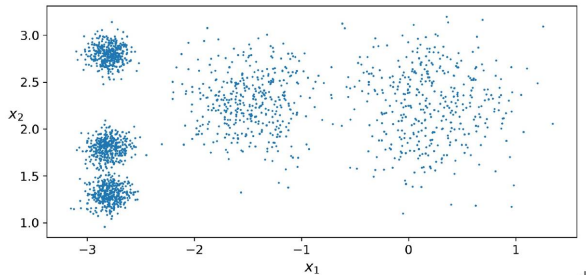
# Applications

- Customer segmentation
  - Marketing campaigns
- Anomaly detection
  - Outliers
- Semi-supervised learning
  - Propagate limited labels
- Image segmentation
  - Object detection



# Clustering

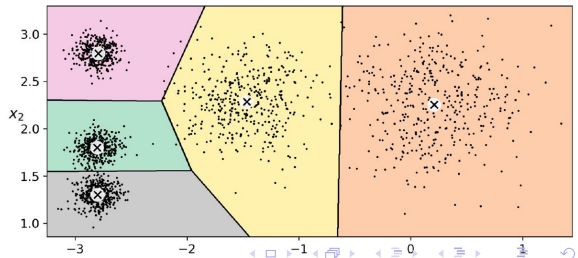
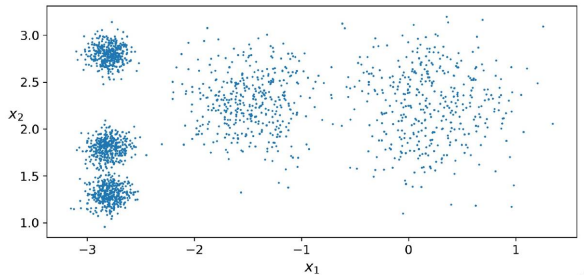
- Find natural groups of data
- Define a distance measure
- Group together data that is close together
- Top down
  - Partition data into clusters
- Bottom up
  - Group items into clusters



# Top down clustering

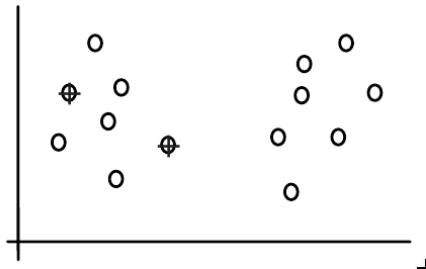
## K Means Clustering

- Data items are points in n dimensions
  - $(x_1, x_2, \dots, x_n)$
- Partition into K clusters
  - Fix K in advance
- Each cluster is represented by its geometric centre
  - *Centroid, or mean*
  - Hence “K means”



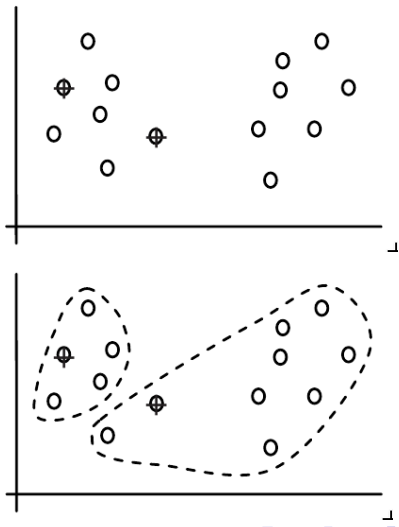
# K Means Algorithm

- Choose K points initially as random centroids
- In each iteration
  - Assign each point to nearest centroid
  - Recompute centroids
- Termination
  - Clusters stabilize
  - Sum square distance is below threshold



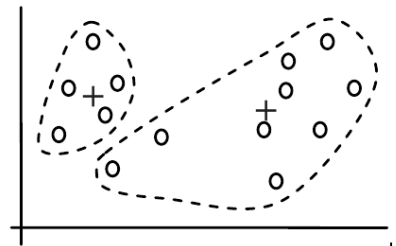
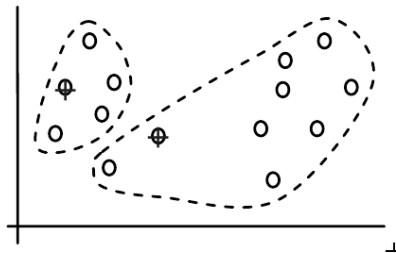
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# K Means Algorithm

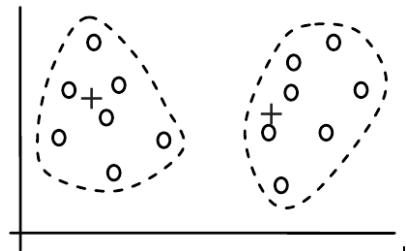
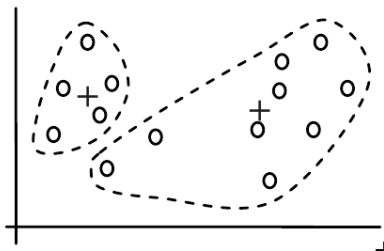
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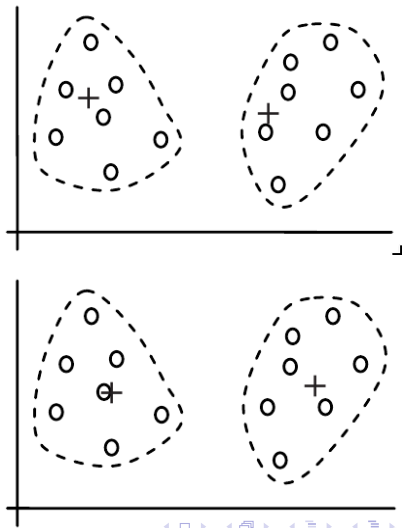
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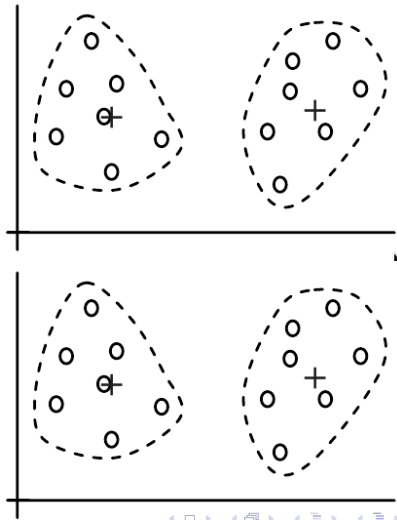
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# K Means Algorithm

- Choose K points initially as random centroids
- In each iteration
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- Termination
  - Clusters stabilize, or
  - Sum square distance is below threshold

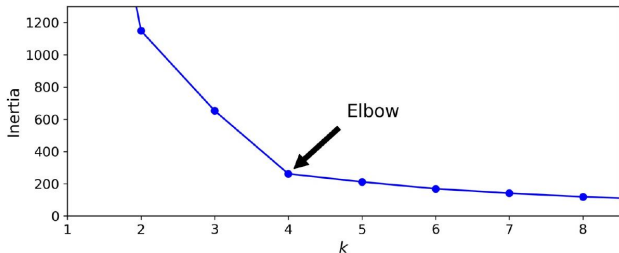


# Evaluating clustering

- How “tight” are the clusters?
- Mean squared distance from centroids – *inertia*

$$\frac{1}{n} \sum_{j=1}^K \sum_{x \in C_j} \text{dist}(x, \text{centroid}_j)^2$$

- Plot inertia for different values of K and look for optimum
- Can also use change in inertia threshold to stop iterations



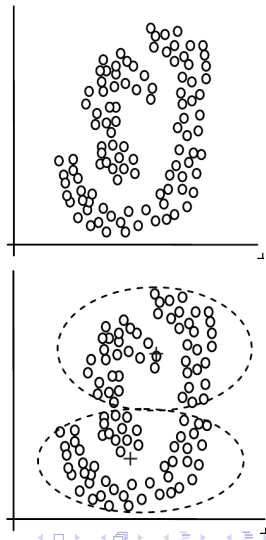
# K Means Algorithm

## Advantages

- Efficient – each iteration makes a single pass over data
  - Incrementally compute centroid

## Disadvantages

- Can only find clusters that look like ellipses



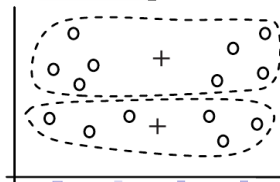
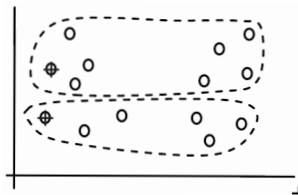
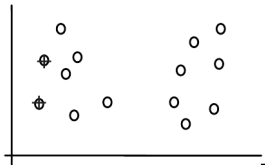
# K Means Algorithm

## Advantages

- Efficient – each iteration makes a single pass over data
  - Incrementally compute centroid

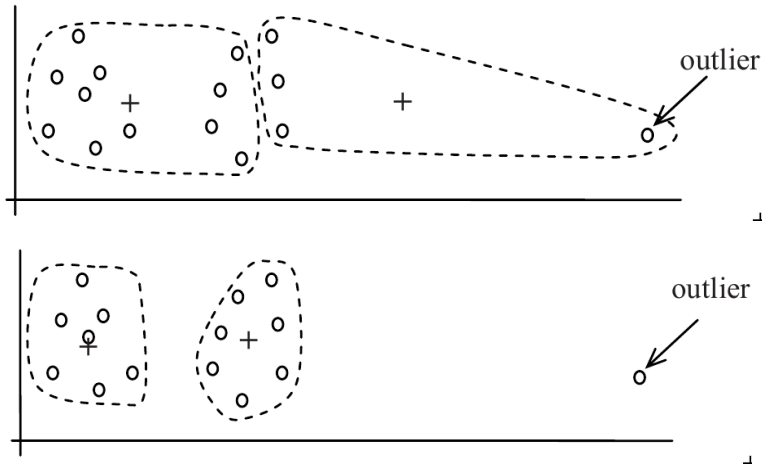
## Disadvantages

- Can only find clusters that look like ellipses
- Choice of initial random centroid matters
  - Repeat and check



# Outliers

- Anomalous values
  - Far away from all centroids
- But clustering with outliers distorts clusters
- How to identify outliers before clustering?

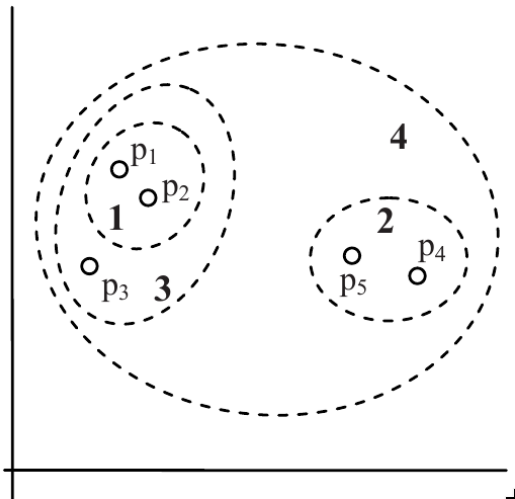


# Clustering

- K Means clustering can only find clusters that look like ellipses
- Instead, build clusters bottom up, by merging clusters

## Hierarchical clustering

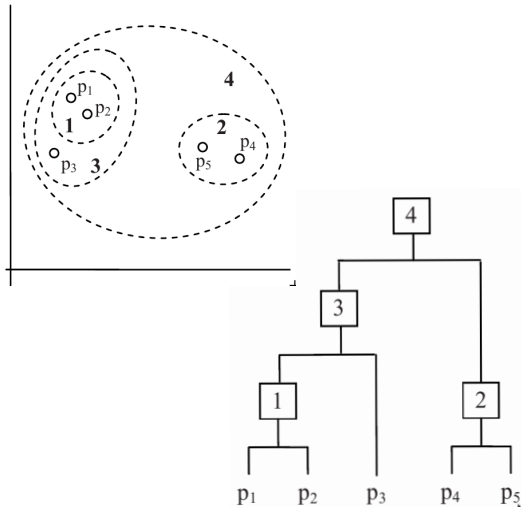
- Initially, each item is a singleton cluster
- At each step, merge nearest clusters





# Hierarchical Clustering

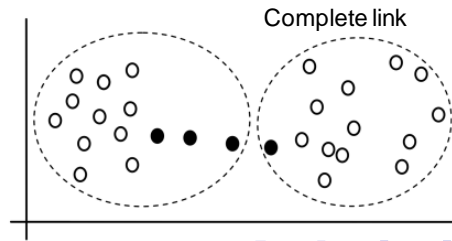
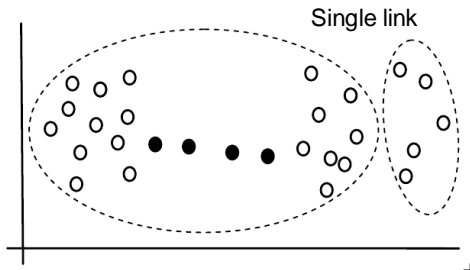
- Initially, each item is a singleton cluster
- At each step, merge nearest clusters
- Can represent process using a tree – dendrogram
- Choose appropriate level in dendrogram for final clustering



# Hierarchical Clustering

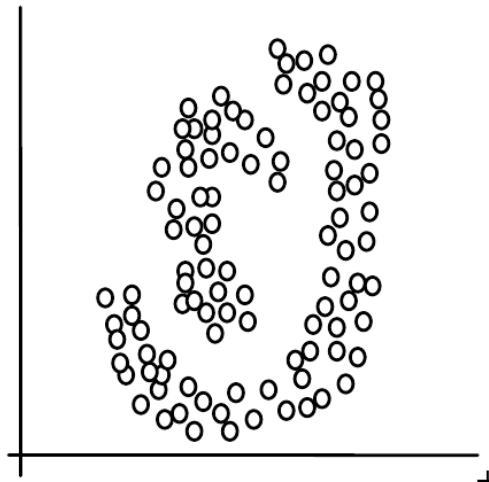
To merge clusters, define distance between clusters

- Single link: distance between closest points
  - Creates chain effect
- Complete link: maximum of pairwise distances
- Average link: mean of pairwise distances
- All require  $O(n^2)$  computation - expensive



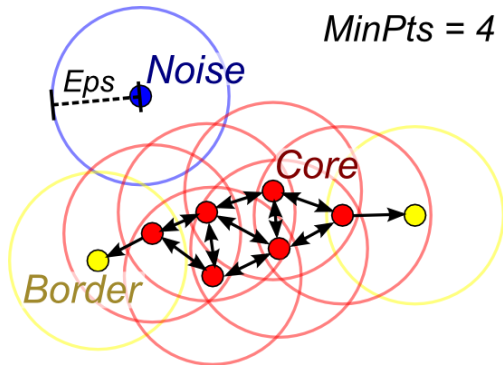
# Clustering

- How to identify odd shaped clusters?
- Cluster - group of points that are “close together”
- Identify “dense” neighbourhoods
- How do we formalize this?



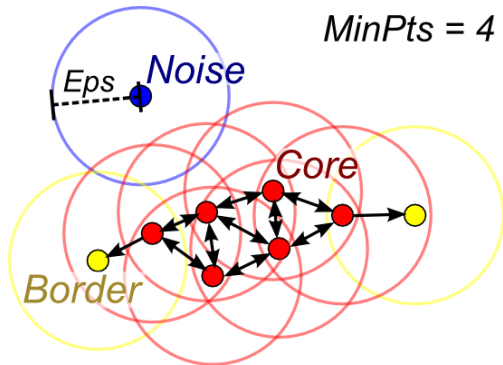
# Density based clustering

- Construct a small ball around each point, radius  $Eps$
- Identify a threshold for neighbours within ball,  $MinPts$
- **Core point** – has at least  $MinPts$  neighbours inside  $Eps$  ball
- Connect each core point to all its neighbours
- **Border points** – attached to core points but not core themselves
- **Noise** – disconnected points



# Density based clustering

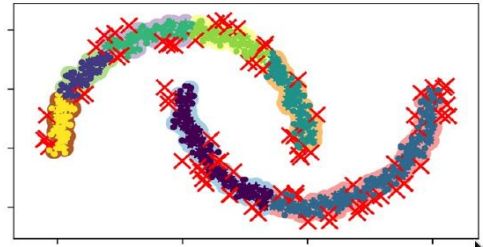
- Formally, edges from core points to neighbours define a directed graph
- Border points are part of this graph, but cannot add edges to extend the graph
- Discard the edge directions
- Connected components are clusters



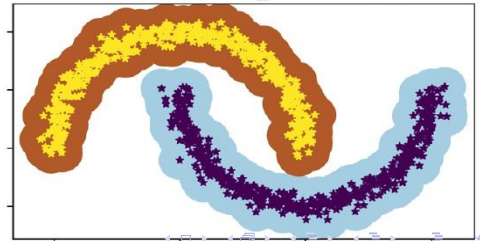
# Dbscan

- Implementation of density based clustering available in Python and R
- Smaller value of  $Eps$  subdivides into small clusters
- Larger  $Eps$  groups larger clusters

eps=0.05, min\_samples=5

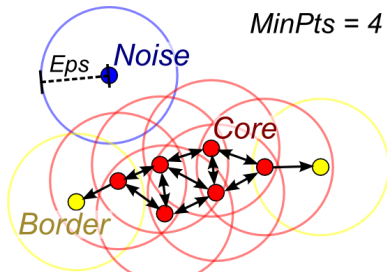
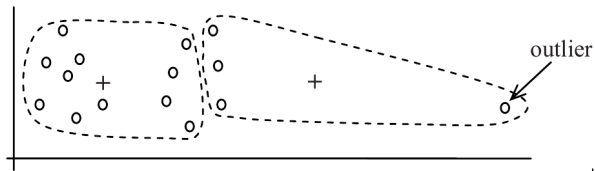


eps=0.20, min\_samples=5



# Outliers and clustering

- Outliers are points that lie outside natural clusters
- K Means – far away from all centroids
  - But outliers can distort the clustering process
- Density based clustering – not connected to any core point
  - But density is applied uniformly



# Outliers and density

- An outlier is less dense than its nearest neighbours
- But difference in density may be local
- A distance metric to eliminate  $o_2$  could make all of  $C_1$  outliers
- $C_1$  has 400 points,  $C_2$  has 100 points
- Larger distance would make all of  $C_2$  outliers with respect to  $C_1$

