

90%  $\equiv$  full credit

$\curvearrowright$  M/W/F

$\longrightarrow$  100% at end  
of semester.

100% = bonus credit

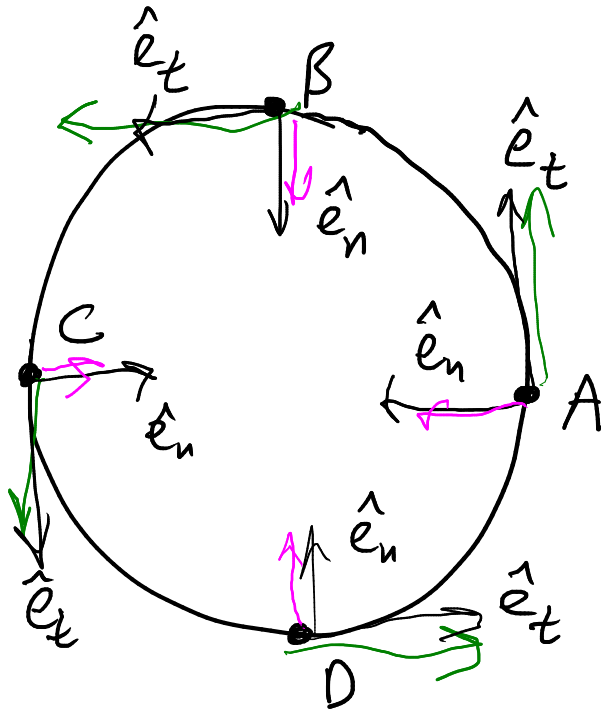
$\curvearrowright$  M/W

$\longrightarrow$  110% - - -

# Tangential / Normal basis vectors

ex 1 uniform circular motion

Constant speed  
 $\dot{s} = \text{const}$



$\|\vec{v}\|$  constant  
 $\vec{v}$  tangential

$$\hat{e}_t = \hat{v} = \frac{\vec{v}}{\|\vec{v}\|} = \frac{\vec{v}}{v}$$

$$\hat{e}_n = \frac{\dot{\hat{e}}_t}{\|\dot{\hat{e}}_t\|}$$

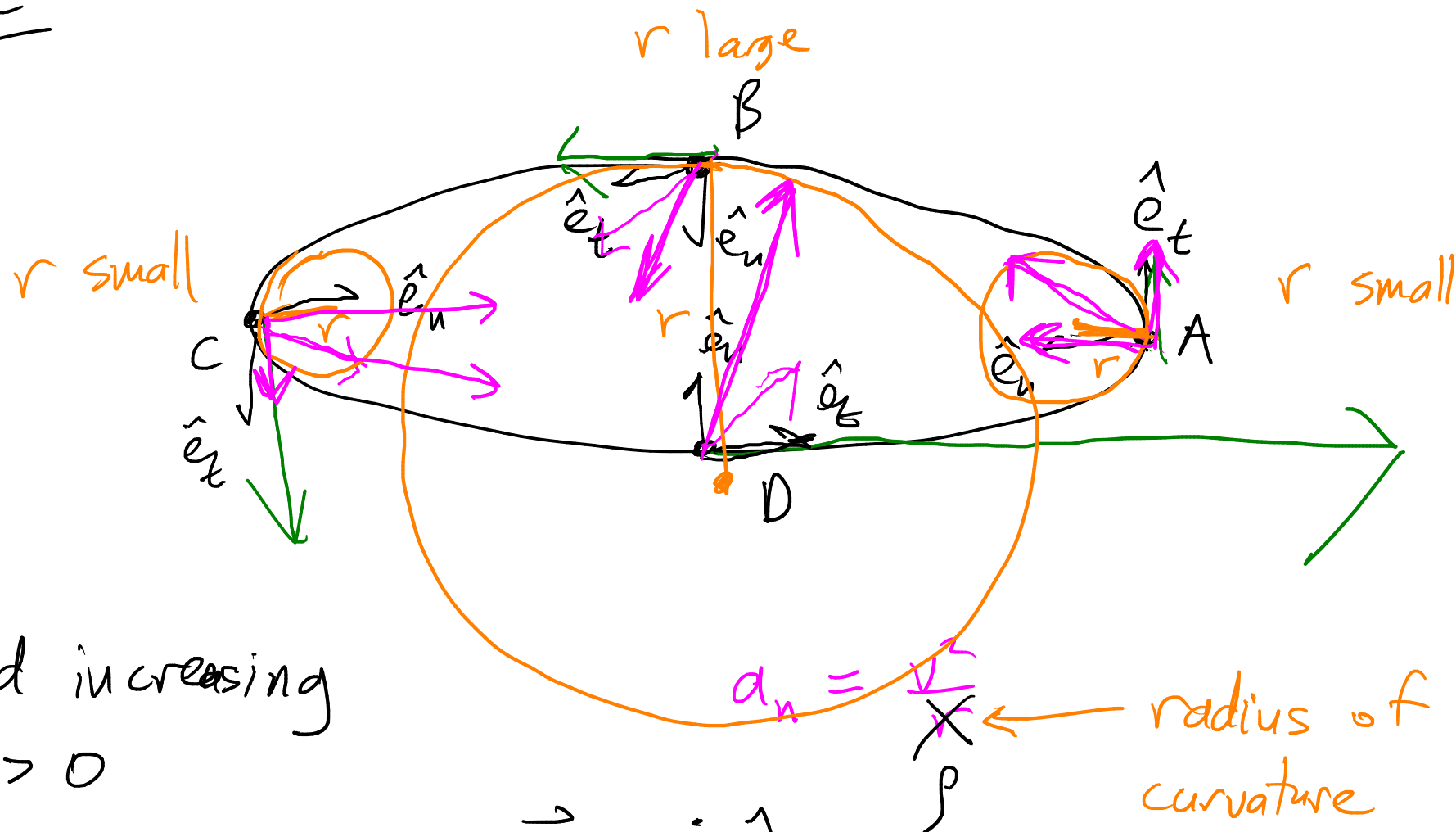
A: correct

B: wrong

$$\|\vec{a}\| = \frac{v^2}{r} = r\omega^2 = \text{constant}$$

$\vec{a}$  = normal

ex 2

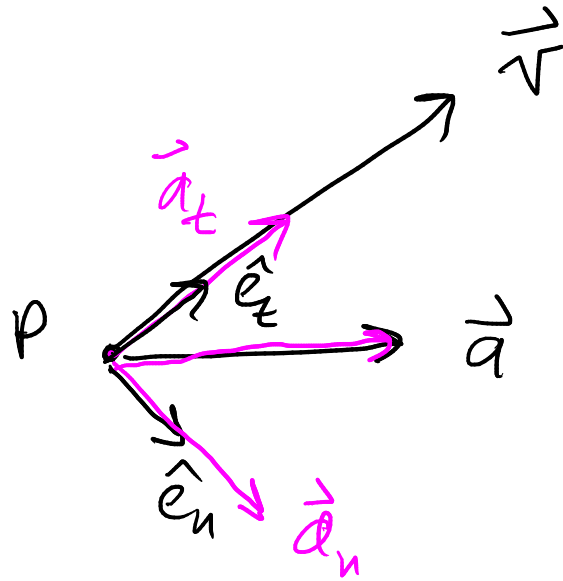


speed increasing  
 $\begin{cases} \dot{v} > 0 \\ \ddot{s} > 0 \end{cases}$   
 $\uparrow$  constant

$$\vec{v} = \dot{s} \hat{e}_t$$

$$\vec{a} = \underset{\substack{\uparrow \\ a_t}}{\ddot{s}} \hat{e}_t + \frac{\dot{s}^2}{\underset{\substack{\uparrow \\ a_n}}{\rho}} \hat{e}_n$$

$$\frac{1}{\rho} = \underset{\substack{\uparrow \\ \text{curvature}}}{\kappa}$$



speeding up

$$\vec{a}_t = \text{Proj}(\vec{a}, \vec{v})$$

$$\vec{a}_n = \text{Comp}(\vec{a}, \vec{v})$$

$$\begin{aligned}\vec{a} &= \hat{a}_t + \vec{a}_n \\ &= \ddot{s} \hat{e}_t + \frac{\dot{s}^2}{\rho} \hat{e}_n\end{aligned}$$

$$\hat{e}_n = \frac{\vec{a}_n}{\|\vec{a}_n\|}$$