## TAM 212. Midterm 1 Practice. Feb 11, 2013. (V3)

- There are 50 questions worth points as shown in each question.
- You must not communicate with other students during this test.
- No electronic devices allowed.
- This is a 2 hour exam.
- Do not turn this page until instructed to do so.
- There are several different versions of this exam.

1.	$\mathbf{Fill}$	in	vour	inforn	nation
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Full Name:	
UIN (Student Number):	
NetID:	

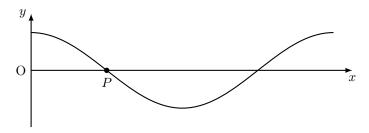
## 2. Circle your discussion section:

	Monday	Tuesday	Wednesday	Thursday
8–9		ADI (260) Karthik		
9–10		ADC (260) Venanzio		ADK (260) Aaron
10-11		ADD (256) Aaron	ADS (252) Ray	ADT (243) Aaron
		ADQ (344) Jan		ADU (344) Jan
11-12		ADE (252) Jan		ADL (256) Kumar
12-1	ADA (243) Ray	ADF (335) Seung	ADJ (256) Ray	ADN (260) Kumar
	ADP (135) Seung	ADG (336) Kumar	ADR (252) Lin	
1-2				
2-3				
3–4				
4-5	ADV (252) Karthik		ADO (260) Mazhar	
			ADW (252) Lin	
5–6	ADB (260) Mazhar	ADH (260) Karthik	ADM (243) Mazhar	

## 3. Fill in the following answers on the Scantron form:

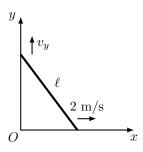
- 91. E
- 92. E
- 93. D
- 94. A
- 95. E
- 96. D

1. (1 point) A particle is moving to the right along a variable-height ground with ground height given by  $y(x) = \cos(x/10)$  m. The particle's horizontal velocity component is a constant  $v_x = 20$  m/s. What is the vertical component of velocity  $v_y$  when  $x = 5\pi$  m?



- (A)  $v_y = 0 \text{ m/s}$
- (B)  $v_y < -3 \text{ m/s}$
- (C)  $3 \text{ m/s} \le v_y$
- (D)  $0 \text{ m/s} \le v_y < 3 \text{ m/s}$
- (E)  $-3 \text{ m/s} \le v_y < 0 \text{ m/s}$

2. (1 point) A ladder leaning against the wall has a fixed length of  $\ell=5$  m. The bottom of the ladder is 3 m from the wall and is moving along the ground away from the wall at a speed of 2 m/s. What is the vertical component of the velocity  $v_y$  of the top of the ladder, assuming it remains in contact with the wall?



- (A)  $0 \text{ m/s} < v_y < 1 \text{ m/s}$
- (B)  $1 \text{ m/s} < v_y$
- (C)  $v_y < -1 \text{ m/s}$
- (D)  $-1 \text{ m/s} \le v_y < 0 \text{ m/s}$
- (E)  $v_y = 0 \text{ m/s}$

3. (1 point) Given a polar basis  $\hat{e}_r, \hat{e}_\theta$ , the time derivative of the angular basis vector satisfies

$$\dot{\hat{e}}_{\theta} = -\hat{e}_r.$$

- (A) True
- (B) False

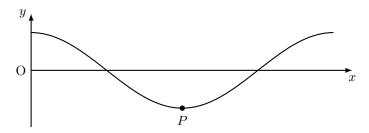
4. (1 point) The particle P has polar coordinates r=3 m,  $\theta=60^{\circ}$  and velocity  $\vec{v}=-\hat{\imath}$ . Which statement is true?

- (A)  $\dot{r} \geq 0$  and  $\dot{\theta} \geq 0$
- (B)  $\dot{r} < 0$  and  $\dot{\theta} \ge 0$
- (C)  $\dot{r} < 0$  and  $\dot{\theta} < 0$
- (D)  $\dot{r} \geq 0$  and  $\dot{\theta} < 0$

5. (1 point) A point currently has position vector  $\vec{r} = -2\hat{\imath} + 4\hat{\jmath}$  m and is rotating about the origin in the x-y plane with angular velocity  $\omega = -3$  rad/s. What is the  $\hat{\jmath}$  component of the velocity  $v_y$  of the point?

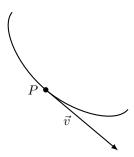
- (A)  $-5 \text{ m/s} \le v_y < 0 \text{ m/s}$
- (B)  $0 \text{ m/s} < v_y < 5 \text{ m/s}$
- (C) 5 m/s  $\leq v_y$
- (D)  $v_y = 0 \text{ m/s}$
- (E)  $v_y < -5 \text{ m/s}$

6. (1 point) A particle is moving to the right along a variable-height ground at a constant speed of v = 20 m/s. The ground height is given by  $y(x) = \cos(x/10)$  m. When the particle is at the lowest point on the ground, what is the vertical acceleration  $a_y$ ?



- (A)  $3 \text{ m/s}^2 \le a_y$
- (B)  $0 \text{ m/s}^2 < a_y < 3 \text{ m/s}^2$
- (C)  $a_y < -3 \text{ m/s}^2$
- (D)  $-2 \text{ m/s}^2 \le a_y < 0 \text{ m/s}^2$
- (E)  $a_y = 0 \text{ m/s}^2$

7. (1 point) A point P is moving around a curve and at a given instant has position and velocity  $\vec{v}$  as shown.



Which direction is the closest to the direction of the normal basis vector  $\hat{e}_n$  at the instant shown?

- (A) >
- (B) \
- (C) <sup><</sup>
- (D)  $\checkmark$

8. (1 point) A car driving down the road is at a distance  $s=t^2$  m from its starting point. At t=2 s the car is driving around a curve with radius of curvature  $\rho=8$  m. What is the magnitude of the acceleration a at this time?

- (A)  $a < 0 \text{ m/s}^2$
- (B)  $1 \text{ m/s}^2 \le a < 2 \text{ m/s}^2$
- (C)  $a = 0 \text{ m/s}^2$
- (D) 0 m/s<sup>2</sup>  $\leq a < 1$  m/s<sup>2</sup>
- (E)  $2 \text{ m/s}^2 \le a$

9. (1 point) If a particle has position vector  $\vec{r}(t) = 5e^t \hat{i} + \sin(2t) \hat{j} + (1 - 3t) \hat{k}$  m, what is its speed v(0) at time t = 0 s?

- (A)  $15 \text{ m/s} \le v(0)$
- (B) v(0) = 0 m/s
- (C)  $10 \text{ m/s} \le v(0) < 15 \text{ m/s}$
- (D) 5 m/s  $\leq v(0) < 10$  m/s
- (E) 0 m/s < v(0) < 5 m/s

10. (1 point) Given a polar basis  $\hat{e}_r, \hat{e}_\theta$ , the time derivative of the radial basis vector satisfies

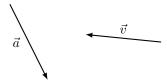
$$\dot{\hat{e}}_r \cdot \hat{e}_r = 0.$$

- (A) False
- (B) True

11. (1 point) A car is observed moving in the plane with velocity  $\vec{v} = 2\hat{\imath} - 4\hat{\jmath}$  and acceleration  $\vec{a} = 2\hat{\imath} + \hat{\jmath}$ . At this instant, is it:

- (A) slowing down
- (B) keeping its speed constant
- (C) speeding up

12. (1 point) The velocity  $\vec{v}$  and acceleration  $\vec{a}$  for a single particle P are shown below at a particular instant.



Which statement is true at this instant?

- (A) the particle's speed is not changing
- (B) the particle slowing down
- (C) the particle is speeding up

13. (1 point) At a certain instant, particles P and Q have position vectors and velocities given by:

$$\vec{r}_P = 3\hat{\imath} + 4\hat{\jmath} \text{ m}$$

$$\vec{r}_Q = -2\hat{\imath} + 6\hat{\jmath} \text{ m}$$

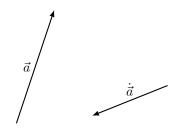
$$\vec{v}_P = -\hat{\imath} - 2\hat{\jmath} \text{ m/s}$$

$$\vec{v}_Q = 2\hat{\imath} + 5\hat{\jmath} \text{ m/s}$$

Which statement is true at this instant?

- (A) the two particles are moving further apart
- (B) the two particles are moving closer together
- (C) the two particles are staying at the same distance from each other

14. (1 point) The vector  $\vec{a}$  and its derivative  $\dot{\vec{a}}$  are shown below.



Which statement is true?

- (A) the length of  $\vec{a}$  is increasing
- (B) the length of  $\vec{a}$  is decreasing
- (C) the length of  $\vec{a}$  is staying the same

15. (1 point) A particle is moving in the plane with changing radius so that at a particular instant we have r=1 m and  $\dot{r}=-4$  m/s. The speed is v=5 m/s. What is the magnitude of  $\dot{\theta}$ ?

- (A)  $6 \text{ rad/s} \le |\dot{\theta}| < 8 \text{ rad/s}$
- (B)  $8 \text{ rad/s} \le |\dot{\theta}|$
- (C)  $2 \text{ rad/s} \le |\dot{\theta}| < 4 \text{ rad/s}$
- (D) 4 rad/s  $\leq |\dot{\theta}| < 6$  rad/s
- (E)  $0 \text{ rad/s} \le |\dot{\theta}| < 2 \text{ rad/s}$

16. (1 point) A particle starts at the origin at time t=0 s and its velocity is given by  $\vec{v}=t^3\,\hat{\imath}-t\,\hat{\jmath}$  m. At time t=2 s, what is the particle's distance r from the origin?

- (A)  $12 \text{ m} \le r < 16 \text{ m}$
- (B)  $0 \text{ m} \le r < 4 \text{ m}$
- (C)  $4 \text{ m} \leq r < 8 \text{ m}$
- (D)  $16 \text{ m} \le r$
- (E)  $8 \text{ m} \le r < 12 \text{ m}$

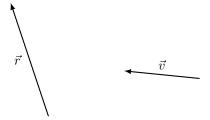
17. (1 point) A particle moves so that its position vector in the Cartesian basis is given by

$$\vec{r} = \cos t \,\hat{\imath} + \sin t \,\hat{\jmath} + t \,\hat{k} \, \,\mathrm{m}.$$

Using cylindrical coordinates, what is the angular component of velocity  $v_{\theta}$  at  $t = \pi/4$  s?

- (A)  $0 \text{ m/s} \le v_{\theta} < 1 \text{ m/s}$
- (B)  $-1 \text{ m/s} \le v_{\theta} < 0 \text{ m/s}$
- (C)  $v_{\theta} = 0 \text{ m/s}$
- (D)  $v_{\theta} < -1 \text{ m/s}$
- (E) 1 m/s  $\leq v_{\theta}$

18. (1 point) The position vector  $\vec{r}$  and velocity  $\vec{v}$  for a single particle P are shown below at a particular instant.



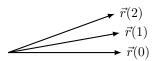
Which statement is true at this instant?

- (A) the distance of P from the origin is staying the same
- (B) the distance of P from the origin is decreasing
- (C) the distance of P from the origin is increasing

19. (1 point) A point is rotating about the origin in the x-y plane with angular velocity  $\omega = 2$  rad/s and velocity  $\vec{v} = 4\hat{\imath} - 2\hat{\jmath}$  m/s. What is the x coordinate of the point?

- (A)  $2 \text{ m} \leq x$
- (B)  $-2 \text{ m} \le x < 0 \text{ m}$
- (C) x < -2 m
- (D) 0 m < x < 2 m
- (E) x = 0 m

20. (1 point) The position vector  $\vec{r}(t)$  of a point is shown below at t=0 s, t=1 s, and t=2 s.



Which direction is the closest to the direction of the acceleration  $\vec{a}(0)$  at time t=0 s?

- $(A) \leftarrow$
- (B)  $\rightarrow$
- (C) ↑
- (D)  $\downarrow$

21. (1 point) If  $\vec{a} = 3\hat{\imath} + 4\hat{\jmath}$  and the derivative is  $\dot{\vec{a}} = 2\hat{\imath} - \hat{\jmath}$ , what can we say about the rate of change of the length of  $\vec{a}$  at this instant?

- (A) the length of  $\vec{a}$  is increasing
- (B) the length of  $\vec{a}$  is staying the same
- (C) the length of  $\vec{a}$  is decreasing

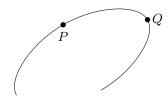
22. (1 point) A point is moving with position vector

$$\vec{r} = (t^2 - 2t)\,\hat{\imath} + t^2\,\hat{\jmath}.$$

What is the radius of curvature  $\rho$  at t = 1 s?

- (A)  $\rho$  is infinite
- (B)  $\rho = 0 \text{ m}$
- (C)  $0 \text{ m} < \rho < \frac{1}{2} \text{ m}$
- (D)  $\frac{1}{2}$  m  $\leq \rho < 1$  m
- (E)  $1 \text{ m} \le \rho < \infty$

23. (1 point) A car is driving on a curved race track at constant speed, with the top view shown below.



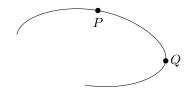
How does the magnitude of the car's acceleration  $a_P$  at point P compare to the value  $a_Q$  at point Q?

- (A)  $a_P > a_Q$
- (B)  $a_P = a_Q$
- (C)  $a_P < a_Q$

24. (1 point) A particle is moving with position vector given by  $\vec{r} = t \hat{\imath} + t^2 \hat{\jmath}$  m. At time t = 1 s, what is the vertical component of the normal vector  $e_{n,y}$ ?

- $(A) \ \frac{1}{2} \le e_{n,y}$
- (B)  $-\frac{1}{2} \le e_{n,y} < 0$
- (C)  $e_{n,y} = 0$
- (D)  $e_{n,y} < -\frac{1}{2}$
- (E)  $0 \le e_{n,y} < \frac{1}{2}$

25. (1 point) A point is moving around the curve shown below with varying speed.



The radius of curvature and speed at P and Q are given by:

$$\rho_P = 4 \text{ m}$$
 $v_P = 4 \text{ m/s}$ 

$$\rho_Q=2~\mathrm{m}$$

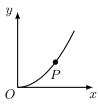
$$v_P = 4 \text{ m/s}$$

$$v_Q = 2 \text{ m/s}.$$

Which of the following is true about the normal accelerations  $a_{P,n}$  at P and  $a_{Q,n}$  at Q?

- (A)  $a_{P,n} > a_{Q,n}$
- (B)  $a_{P,n} = a_{Q,n}$
- (C)  $a_{P,n} < a_{Q,n}$

26. (1 point) A particle is moving to the right along the curve  $y = \frac{1}{3}x^2$  m at a constant speed of  $v = \frac{5}{3}$  m/s. What is the horizontal component of velocity  $v_x$  when x = 2 m?



- (A)  $0 \text{ m/s} \le v_x < 2 \text{ m/s}$
- (B)  $2 \text{ m/s} \leq v_x$
- (C)  $-2 \text{ m/s} \le v_x < 0 \text{ m/s}$
- (D)  $v_x = 0 \text{ m/s}$
- (E)  $v_x < -2 \text{ m/s}$

27. (1 point) For a certain position P the distance from the origin is r = 4 m and the polar basis vectors are:

$$\hat{e}_r = -\frac{1}{2}\hat{\imath} - \frac{\sqrt{3}}{2}\hat{\jmath}$$

$$\hat{e}_{\theta} = \frac{\sqrt{3}}{2}\hat{\imath} - \frac{1}{2}\hat{\jmath}$$

What is the horizontal coordinate x?

- (A)  $-2 \text{ m} \le x < 0 \text{ m}$
- (B) 2 m < x
- (C) x < -2 m
- (D) 0 m < x < 2 m
- (E) x = 0 m

28. (1 point) The position vector  $\vec{r}$  and velocity  $\vec{v}$  for a single particle P are shown below at a particular instant.



Which statement about the polar angle derivative  $\dot{\theta}$  is true at this instant?

- (A)  $\dot{\theta} < 0$
- (B)  $\dot{\theta} = 0$
- (C)  $\dot{\theta} > 0$

- 29. (1 point) The vector  $\vec{a} = 3\hat{\imath} 4\hat{\jmath}$  has derivative  $\dot{\vec{a}} = -2\hat{\imath} \hat{\jmath}$ . What is the rate of change  $\dot{a}$  of the length?
- (A)  $\dot{a} < -1$
- (B)  $0 < \dot{a} < 1$
- (C)  $-1 \le \dot{a} < 0$
- (D)  $1 \le \dot{a}$
- (E)  $\dot{a} = 0$

30. (1 point) A particle moves so that its position in polar coordinates is given by

$$r = \frac{1}{2}t^2$$
 m

$$\theta = 2t \text{ rad.}$$

What is the radial component of acceleration  $a_r$  at t=2 s?

- (A)  $0 \text{ m/s}^2 \le a_r < 7 \text{ m/s}^2$
- (B)  $7 \text{ m/s}^2 \le a_r$
- (C)  $a_r < -7 \text{ m/s}^2$
- (D)  $a_r = 0 \text{ m/s}^2$
- (E)  $-7 \text{ m/s}^2 \le a_r < 0 \text{ m/s}^2$

31. (1 point) A position P has an associated polar basis with

$$\hat{e}_{\theta} = \frac{1}{\sqrt{2}}\hat{\imath} - \frac{1}{\sqrt{2}}\hat{\jmath}.$$

What is  $\theta$ ?

- (A)  $\frac{3}{2}\pi \le \theta < 2\pi$
- (B)  $\pi \le \theta < \frac{3}{2}\pi$
- (C)  $0 \le \theta < \frac{1}{2}\pi$
- (D)  $\frac{1}{2}\pi \le \theta < \pi$

- 32. (1 point) The particle P has polar coordinates r=2 m,  $\theta=-\frac{3}{4}\pi$  rad and rates of change  $\dot{r}>0$  and  $\dot{\theta}<0$ . Which statement about the velocity  $\vec{v}$  of P must be true?
- (A)  $v_y < 0$
- (B)  $v_y \ge 0$
- (C)  $v_x \ge 0$
- (D)  $v_x < 0$

33. (1 point) A position P has an associated polar basis with

$$\hat{e}_r = \frac{1}{2}\hat{\imath} + \frac{\sqrt{3}}{2}\hat{\jmath}.$$

- What is  $\hat{e}_{\theta}$ ?
- (A)  $\hat{e}_{\theta} = \frac{\sqrt{3}}{2}\hat{i} \frac{1}{2}\hat{j}$
- (B)  $\hat{e}_{\theta} = -\frac{\sqrt{3}}{2}\hat{i} + \frac{1}{2}\hat{j}$
- (C)  $\hat{e}_{\theta} = \frac{\sqrt{3}}{2}\hat{i} + \frac{1}{2}\hat{j}$
- (D)  $\hat{e}_{\theta} = -\frac{\sqrt{3}}{2}\hat{i} \frac{1}{2}\hat{j}$

34. (1 point) A particle P has position vector and velocity:

$$\vec{r} = 5\hat{\imath} + 2\hat{\jmath} \text{ m}$$
 
$$\vec{v} = 2\hat{\imath} - 4\hat{\jmath} \text{ m/s}.$$

Is the distance from P to the origin:

- (A) increasing
- (B) staying the same
- (C) decreasing

35. (1 point) A particle P has position vector, velocity, and acceleration given by:

$$\begin{aligned} \vec{r} &= 4\hat{\imath} + 2\hat{\jmath} \text{ m} \\ \vec{v} &= 2\hat{\imath} - 7\hat{\jmath} \text{ m/s} \\ \vec{a} &= -3\hat{\imath} - 2\hat{\jmath} \text{ m/s}^2 \end{aligned}$$

Consider the following statements:

- (i) The particle is moving closer to the origin.
- (ii) The particle is moving further from the origin.
- (iii) The particle is speeding up.
- (iv) The particle is slowing down.

Which statements are true?

- $(\mathbf{A})$  (i) and (iii)
- (B) (ii) and (iii)
- (C) (i) and (iv)
- (D) (ii) and (iv)
- (E) none of the other options

36. (1 point) The velocity  $\vec{v}(t)$  of a point is shown below at t=0 s and t=1 s.



Which direction is the closest to the direction of the acceleration  $\vec{a}(0)$  at time t = 0 s?

- (A) ↑
- (B) ↓
- (C) ←
- $(D) \rightarrow$

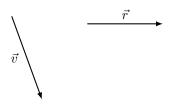
37. (1 point) A vector  $\vec{a}$  and its derivative  $\dot{\vec{a}}$  have  $||\vec{a}|| = 3$ ,  $||\dot{\vec{a}}|| = 4$ , and  $\vec{a} \cdot \dot{\vec{a}} = -6$ . What can we say about the rate of change of the length of  $\vec{a}$  at this instant?

- (A) the length of  $\vec{a}$  is increasing
- (B) the length of  $\vec{a}$  is decreasing
- (C) the length of  $\vec{a}$  is staying the same

38. (1 point) A point has Cartesian coordinates x = -3 m, y = -2 m. What is its polar coordinate angle  $\theta$ ?

- (A)  $\pi \operatorname{rad} \leq \theta < \frac{3}{2}\pi \operatorname{rad}$
- (B)  $\frac{1}{2}\pi$  rad  $\leq \theta < \pi$  rad
- (C) 0 rad  $\leq \theta < \frac{1}{2}\pi$  rad
- (D)  $\frac{3}{2}\pi \operatorname{rad} \leq \theta < 2\pi \operatorname{rad}$

39. (1 point) The position vector  $\vec{r}$  and velocity  $\vec{v}$  for a single particle P are shown below at a particular instant.



Which statement about  $\dot{r}$  is true at this instant?

- (A)  $\dot{r} = 0$
- (B)  $\dot{r} > 0$
- (C)  $\dot{r} < 0$

40. (1 point) A point is moving around the curve shown and is currently at position P. Consider a polar basis  $\hat{e}_r$ ,  $\hat{e}_\theta$  at P from the origin O and a tangential/normal basis  $\hat{e}_t$ ,  $\hat{e}_n$  at P.



Which of the following is true?

- (A)  $\hat{e}_n = -\hat{e}_r$
- (B)  $\hat{e}_n = -\hat{e}_\theta$
- (C)  $\hat{e}_n = \hat{e}_r$
- (D)  $\hat{e}_n = \hat{e}_\theta$

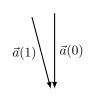
41. (1 point) A position P has an associated polar basis so that

$$\hat{\imath} = \frac{1}{\sqrt{2}}\hat{e}_r - \frac{1}{\sqrt{2}}\hat{e}_\theta.$$

What is  $\theta$ ?

- (A)  $\pi \le \theta < \frac{3}{2}\pi$
- (B)  $\frac{3}{2}\pi \le \theta < 2\pi$
- (C)  $\frac{1}{2}\pi \le \theta < \pi$
- (D)  $0 \le \theta < \frac{1}{2}\pi$

42. (1 point) The vector  $\vec{a}(t)$  is pictured below at t = 0 s and t = 1 s.



Which direction is the closest to the direction of  $\dot{\vec{a}}(0)$ ?

- $(A) \leftarrow$
- (B) ↓
- (C) ↑
- $(D) \rightarrow$

- 43. (1 point) A point is currently at position x=3 m, y=2 m, z=0 m and is rotating in the x-y plane about the origin with angular velocity  $\vec{\omega}=2\hat{k}$ . The velocity  $\vec{v}$  of the point is:
- (A)  $\vec{v} = -4\hat{\imath} + 6\hat{\jmath} \text{ m/s}$
- (B)  $\vec{v} = -4\hat{\imath} 6\hat{\jmath} \text{ m/s}$
- (C)  $\vec{v} = 4\hat{\imath} 6\hat{\jmath} \text{ m/s}$
- (D)  $\vec{v} = 4\hat{\imath} + 6\hat{\jmath} \text{ m/s}$

44. (1 point) A particle moves so that its position in polar coordinates is given by

$$r=2t~\mathrm{m}$$

$$\theta = -\frac{\pi}{8}t^2$$
 rad.

What is the  $\hat{\imath}$  component of velocity  $v_x$  at t=2 s?

- (A)  $v_x < -6 \text{ m/s}$
- (B)  $-6 \text{ m/s} \le v_x < 0 \text{ m/s}$
- (C)  $v_x = 0 \text{ m/s}$
- (D) 6 m/s  $\leq v_x$
- (E)  $0 \text{ m/s} \le v_x < 6 \text{ m/s}$

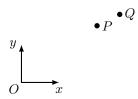
45. (1 point) The position vector of a particle is given by

$$\vec{r} = (4t^2 - 2)\hat{\imath} + (4t^2 - t^3)\hat{\jmath}$$
 m.

Which statement is true at time t = 0?

- (A) the  $\hat{\jmath}$  component of the particle's velocity is decreasing
- (B) the  $\hat{j}$  component of the particle's velocity is staying the same
- (C) the  $\hat{j}$  component of the particle's velocity is increasing

46. (1 point) Points P and Q are moving in circular paths around the origin O with angular velocities  $\omega_P$  and  $\omega_Q$ .



The two particles are moving with the same speed. Which statement is true?

- (A)  $\frac{1}{2}|\omega_Q| < |\omega_P| \le |\omega_Q|$
- (B)  $|\omega_P| \leq \frac{1}{2} |\omega_Q|$
- (C)  $|\omega_Q| < |\omega_P| \le 2|\omega_Q|$
- (D)  $2|\omega_Q| < |\omega_P|$

47. (1 point) A spaceship is moving with velocity and acceleration given in a polar basis by

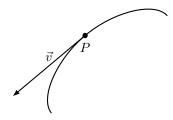
$$\vec{v} = 3\,\hat{e}_r + 4\,\hat{e}_\theta \text{ m/s}$$

$$\vec{a} = -7 \,\hat{e}_r - \hat{e}_\theta \,\,\mathrm{m/s^2}.$$

What is the radius of curvature of the spaceship's path?

- (A) 0 m  $\leq \rho < 2$  m
- (B)  $\rho = 0 \text{ m}$
- (C) 6 m  $\leq \rho$
- (D)  $2 \text{ m} \le \rho < 4 \text{ m}$
- (E)  $4 \text{ m} \le \rho < 6 \text{ m}$

48. (1 point) A car is driving on a curved track with the top view shown below. At a given instant the car is at point P with velocity  $\vec{v}$  and its speed is increasing, such that the tangential and normal components of its acceleration are equal in magnitude.



Which direction is the closest to the direction of the acceleration  $\vec{a}$  at the instant shown?

- $(A) \rightarrow$
- (B)  $\leftarrow$
- (C) ↑
- $(D) \downarrow$

49. (1 point) A point has polar coordinates r = 4 m,  $\theta = -120^{\circ}$ . What is its horizontal coordinate x?

- (A) x < -2 m
- (B) 2 m < x
- (C) 0 m < x < 2 m
- (D) x = 0 m
- (E)  $-2 \text{ m} \le x < 0 \text{ m}$

- 50. (1 point) A car is observed moving in the plane with velocity  $\vec{v} = 3\hat{\imath} + 2\hat{\jmath}$  and acceleration  $\vec{a} = -2\hat{\imath} + 4\hat{\jmath}$ . At this instant, is it:
- (A) stationary
- (B) driving around a curve counterclockwise
- (C) driving around a curve clockwise
- (D) driving in a straight line