

## Day 12:

### Task 1: Bit Manipulation Basics

Create a function that counts the number of set bits (1s) in the binary representation of an integer. Extend this to count the total number of set bits in all integers from 1 to n.

```
public class TotalSetBits {    public
static int totalSetBits(int n) {        int
totalBits = 0;        for (int i = 1; i <= n;
i++) {            totalBits +=
countSetBits(i);
        }
        return totalBits;
    }

    private static int countSetBits(int n) {
return Integer.bitCount(n);
    }

    public static void main(String[] args) {
        int n = 10;
        System.out.println(totalSetBits(n));
    }
}
```

### Explanation:

#### 1 **totalSetBits** method:

- **totalSetBits**(int n) iterates through numbers from 1 to n.
- For each number i, it calls the **countSetBits**(i) method to count the set bits in i and accumulates this count in **totalBits**.
- Finally, it returns **totalBits**, which is the total number of set bits in the binary representations of the integers from 1 to n.

#### **countSetBits** method:

- **countSetBits**(int n) simply calls **Integer.bitCount**(n), which counts the set bits in the integer n.

#### **main** method:

- In the main method, we set n = 10 and print the result of **totalSetBits**(n).
- The expected output for n = 10 is 17, which represents the total number of set bits in the binary representations of the integers from 1 to 10.

### Example Output

When we run the main method with n = 10, the output will be:

**17**

This output means that the total number of set bits in the binary representations of the integers from 1 to 10 is 17.

#### Binary representation and set bits for numbers from 1 to 10:

- 1 (binary **0001**) has 1 set bit.
- 2 (binary **0010**) has 1 set bit.
- 3 (binary **0011**) has 2 set bits.
- 4 (binary **0100**) has 1 set bit.
- 5 (binary **0101**) has 2 set bits.
- 6 (binary **0110**) has 2 set bits.
- 7 (binary **0111**) has 3 set bits.
- 8 (binary **1000**) has 1 set bit.

9 (binary **1001**) has 2 set bits.

10 (binary **1010**) has 2 set bits.

## Task 2: Unique Elements Identification

**Given an array of integers where every element appears twice except for two, write a function that efficiently finds these two non-repeating elements using bitwise XOR operations**

### Explanation

#### Understanding XOR properties:

- XOR of a number with itself is 0:  $a \oplus a = 0$ .
- XOR of a number with 0 is the number itself:  $a \oplus 0 = a$ .
- XOR is both commutative and associative:  $a \oplus b \oplus a = b \oplus (a \oplus a) = b$ .

```
public class TwoNonRepeatingElements {    public
static void findNonRepeating(int[] nums) {

    int xor = 0;

    // Step 1: Get the XOR of all elements
    for (int num : nums) {        xor ^= num;
    }

    // Step 2: Find any set bit in xor (any bit where x and y differ)
    int bitMask = 1;    while ((bitMask & xor) == 0) {
    bitMask <<= 1;
    }
```

```
int x = 0;  
int y = 0;    //
```

Step 3: Partition

the numbers

into two groups

and find the

non-repeating

elements

```
for (int num : nums) {  
    if ((num & bitMask) != 0) {  
        x ^= num;  
    } else {  
        y  
        ^= num;  
    }  
}
```

```
System.out.println("Non-repeating elements are: " + x + " and " + y);  
}
```

```
public static void main(String[] args) {  
    int[] nums = {1, 2, 3, 2, 1, 4};  
    findNonRepeating(nums); // Output: Non-repeating elements are: 3 and 4  
}
```

**Output:**

The output of the program will be

Non-repeating elements are: 3 and 4

Let's continue with the example array  $\text{nums} = \{1, 2, 3, 2, 1, 4\}$  and the xor value 7 (0111 in binary).

**Initialization:**

Start with  $\text{bitMask} = 1$  (0001 in binary).

Loop to find the set bit:

**First iteration:**

$(\text{bitMask} \& 0111) = (0001 \& 0111) = 0001$

Since this is not zero, continue.

**Second iteration:**  $\text{bitMask}$

is shifted left: 0010

$(0010 \& 0111) = 0010$

This is still not zero, continue.

**Third iteration:**  $\text{bitMask}$  is

shifted left: 0100

$(0100 \& 0111) = 0100$

This is still not zero, continue.

**Fourth iteration:**  $\text{bitMask}$  is

shifted left: 1000

$(1000 \& 0111) = 0000$

This is zero, exit the loop.