

$$x \leq y \quad y \geq z$$

$$\overline{x \quad y \quad z}$$

$$f = (x+y)(y+z) = xy + xz + y^2 + yz$$

$$A[p] \quad B[q] \quad C[r]$$

$$\text{Array}[i] \rightarrow 10^9$$

$$x_0 \quad x_1 \quad \dots \quad x_{p-1}$$

$$y_0 \quad y_1 \quad \dots \quad y_{q-1}$$

$$z_0 \quad z_1 \quad \dots \quad z_{r-1}$$

$$\begin{array}{ccc} 1 & 2 & 4 \\ 3 & 2 & \\ & 1 & 3 \end{array}$$

$$(x+y)(y+z) =$$

$$XY + XZ + Y^2 + YZ$$

0 1 2 3 4 5

A 1 2 3 4 5 6 (a)

B 4 3 1 1 (b)

C 2 4 5 6 (c)

X	Y	Z
1	<del>0</del> 4 <del>3</del> 1	<del>2</del> 4 <del>5</del> 2 2

cntx cnty  
0 0 10

          
x y z

a	b	c
0	<del>0</del> 1 2 3	<del>0</del> 1 2 <del>0</del> 1 0

Sum = vvv

Algo: 2

2 3 5  
4 3 2 1  
2 3 5 6

$X(p) \{ \square \square \}$

$Y(q) \{ \square \square \square \square \}$

$Z(r) \{ \square \}$

$$X \leq Y \geq Z \quad (X+Y)(Y+Z) = XY + XZ + Y^2 + YZ$$

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a=c=0  b=0
for (b = 0 to q-1)
    c=0
    y=Y(b)
    x=X(a)
    z=Z(c)
    if (x > y)
        if (b==0) break
        x++
        b=-1
    while (y >= z)
        s = s + ( ) % MOD
        z = Z(++c)

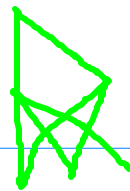
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↓  
 1 2 3  
 ↓  
 5 3  
 ↓ ↓  
~~5~~ 5 7

x	y	z
1	5	4
1	5	5
2	5	4
2	5	5
3	5	5
3	5	5

# Algo 3

$A(p)$   
 $B(q)$   
 $C(r)$



$\{$   
 $\}$

$$(x+y)(y+z) = \underline{xy} + \underline{y^2} + xz + yz$$

$$x+y = 2$$



x	y	z
1	5	3
1	5	5
2	5	5
2	5	5
3	5	3
3	5	5

	time
xy	2x
y <sup>2</sup>	3x2
xz	
yz	3y

$$\begin{aligned}
 y+x &= 11 \{ 3 \ 0 \} \\
 y+z &= 11 \{ 2 \ 0 \}
 \end{aligned}$$

$A$  1 2 3 6 p  
 $B$  5 3 q  
 $C$  3 5 7 r

Nonzero 11 9

x	y	z	xy	6x1=6
2	3	1	y <sup>2</sup>	9
2	3	1	xz	2
			yz	3
				<u>20</u>

$$\begin{aligned}
 &2 \\
 &3 \ 3 \\
 &1 \ 4 \\
 &\hline
 &40
 \end{aligned}$$

A 2 3 6

B 1 3 6

C 3 7 8

p  
q  
r

$y \rightarrow x = 0 \rightarrow 2$   
 $prev = 0 \rightarrow 2$

$y \rightarrow z = 0 \rightarrow 1$   
 $prev = 0 \rightarrow 1$

$sumX = 2 + 3$

$sumZ = 3$

A	<u>3</u>	<u>4</u>	<u>5</u>	<u>6</u>	<sup>↓</sup>	x	p
B	<u>1</u>	<u>2</u>	<u>3</u>	<u>5</u>	<u>8</u>	y	q
C	<u>4</u>	<u>5</u>	<u>6</u>	<u>7</u>		z	r

$$y \rightarrow x = 1$$

$$\text{Sum } x = 2$$

$$y \rightarrow z = 1, 2, 3$$

$$\text{Sum } z = 1 + 2 + 3$$

$$y = 2, 3$$

$$x = 2$$

$$z = 1, 2, 3$$

			↓	↓		
a	X		<u>2</u>	1		
b	Y		<u>2</u>	<u>3</u>		
c	Z		<u>1</u>	<u>2</u>	<u>3</u>	↓

	X	Y	Z
A	<u><math>a_0</math></u>	<u><math>a_1</math></u>	<u><math>a_2</math></u> ... <u><math>a_{p-1}</math></u>
B	<u><math>b_0</math></u>	<u><math>b_1</math></u>	<u><math>b_2</math></u> ... <u><math>b_{q-1}</math></u>
C	<u><math>c_0</math></u>	<u><math>c_1</math></u>	<u><math>c_2</math></u> ... <u><math>c_{r-1}</math></u>

$Y \rightarrow X$  ~~0~~ 1 2 3 4  
 $Y \rightarrow Z$  ~~0~~ 1 2 3 4

4 5 6 7 1  
1 3 5 8 9  
3 4 5 7 1

X    Y    Z  
 2    1    1

2    4 ↓  
 ↓ 2    3    4  
       ↓    ↓  
       1    4

$Y \rightarrow X = 1$   
 $Y \rightarrow Z =$

$\text{sum} X =$   
 $\text{sum} Z =$