

// Write a program to solve a 0-1 Knapsack problem using dynamic programming or branch and bound strategy

// USING DYNAMIC PROGRAMMING

// TC  $O(n \cdot w)$

// SC  $O(n \cdot w)$

#include <bits/stdc++.h>

using namespace std;

// Recursive function with memoization to solve 0-1 Knapsack problem

int solve(int w, vector<int> &wt, vector<int> &val, int ind, vector<vector<int>> &dp) {

if (ind < 0) // Base case: no items left to consider

return 0;

// Check if result already computed for current state

if (dp[ind][w] != -1)

return dp[ind][w];

// Case 1: Do not include current item

int notInclude = solve(w, wt, val, ind - 1, dp);

// Case 2: Include current item (if it fits within remaining weight)

int include = 0;

if (wt[ind] <= w) {

include = val[ind] + solve(w - wt[ind], wt, val, ind - 1, dp);

}

// Store and return the maximum value of including or not including the item

return dp[ind][w] = max(notInclude, include);

}

```

// Wrapper function to initialize dp array and start the recursive solution
int knapsack(int w, vector<int> &wt, vector<int> &val, int n) {
    vector<vector<int>> dp(n, vector<int>(w + 1, -1)); // DP table initialized to -1
    return solve(w, wt, val, n - 1, dp); // Start with the last item
}

int main() {
    int w = 50; // Knapsack capacity
    vector<int> wt = {10, 20, 30}; // Weights of items
    vector<int> val = {60, 100, 120}; // Values of items
    int n = wt.size();

    cout << "Maximum Profit: " << knapsack(w, wt, val, n) << endl;
    return 0;
}

```