

2023-April-10 Shift-1

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AI24BTECH11005 - Prajwal Naik

- 16) An arc PQ of a circle subtends a right angle at the centre O. The midpoint of the arcPq is R.If $\overrightarrow{OP} = \vec{u}$ and $\overrightarrow{OR} = \vec{v}$ and $\overrightarrow{OQ} = \alpha\vec{u} + \beta\vec{v}$, then α, β^2 are the roots of the equation :

a) $3x^2 - 2x - 1 = 0$

c) $x^2 - x - 2 = 0$

b) $3x^2 + 2x - 1 = 0$

d) $x^2 + x - 2 = 0$

- 17) A square piece of tin of side 30 cm is to be made into a box without top by cutting a square from each corner and folding up the flaps to form a box. If the volume of the box is maximum, then its surface area is equal to :

a) 800

b) 1025

c) 900

d) 675

- 18) Let O be the origin and the position vector of the point P be $-\hat{i} - 2\hat{j} + 3\hat{k}$. If the position vectors of the A, B and C are $-2\hat{i} + \hat{j} - 3\hat{k}, 2\hat{i} + 4\hat{j} - 2\hat{k}$ and $-4\hat{i} + 2\hat{j} - \hat{k}$ respectively, then the projection of the vector \overrightarrow{OP} on a vector perpendicular to the vectors $\overrightarrow{AB}, \overrightarrow{AC}$ is

a) $\frac{10}{3}$

b) $\frac{8}{3}$

c) $\frac{7}{3}$

d) 3

- 19) If A is a 3×3 matrix and $|A| = 2$, then $\left| 3adj\left(|3A|A^2\right) \right|$ is equal to :

a) 1

c) 3^{10}

b) 2

d) None of the above

20) a) 76

c) 70

b) 74

d) 72

- 21) The negation of the statement : $(p \vee q) \wedge (q \vee (\neg r))$ is

a) $((\neg p) \vee r) \wedge (\neg q)$

c) $((\neg p) \vee (\neg q) \vee (\neg r))$

b) $((\neg p) \vee (\neg q) \wedge (\neg r))$

d) $(p \vee r) \wedge (\neg q)$

- 22) The shortest distance between the lines $\frac{x+2}{1} = \frac{y}{-2} = \frac{z-5}{2}$ and $\frac{x-4}{1} = \frac{y-1}{2} = \frac{z+3}{0}$ is :

a) 8

c) 6

b) 7

d) 9

- 23) If the coefficient of x^7 in $\left(ax - \frac{1}{bx^2}\right)^{13}$ and the coefficient of x^{-5} in $\left(ax + \frac{1}{bx^2}\right)^{13}$ are equal, then a^3b^4 is equal to :

- a) 22
b) 44

- c) 11
d) 33

24) A line segment AB of length λ moves such that the points A and B remain on the periphery of a circle of radius λ . The locus of the point, that divides the line segment AB in the ratio 2:3, is a circle of radius :

- a) $\frac{2}{3}\lambda$
b) $\frac{\sqrt{19}}{7}\lambda$

- c) $\frac{3}{5}\lambda$
d) $\frac{\sqrt{19}}{5}\lambda$

25) For the system of linear equations

$$2x - y + 3z = 5$$

$$3x + 2y - z = 7$$

$$4x + 5y + \alpha z = \beta$$

Which of the following is not correct?

- a) The system is inconsistent for $\alpha = -5$, $\beta = 8$
b) The system has infinitely many solutions for $\alpha = -6$, $\beta = 9$
c) The system has a unique solution for $\alpha = -5$, $\beta = 8$
d) The system has infinitely many solutions for $\alpha = -5$, $\beta = 8$

26) Let the first term a and the common ratio r of a geometric progression be positive integers. If the sum of squares of its first three is 33033, then the sum of these terms is equal to :

- a) 210 b) 220 c) 231 d) 241

27) Let P be the point of intersection of the line $\frac{x+3}{3} = \frac{y+2}{1} = \frac{z-1}{-2}$ and the plane $x+y+z = 2$. If the distance of the point P from the plane $3x - 4y + 12z = 32$ is q, then q and 2q are the roots of the equation :

- a) $x^2 + 18x - 72 = 0$ b) $x^2 + 18x + 72 = 0$ c) $x^2 - 18x - 72 = 0$ d) $x^2 - 18x + 72 = 0$

28) Let f be a differentiable function such that $x^2 f(x) - x = 4 \int_0^x t f(t) dt$. $f(1) = \frac{2}{3}$. Then $18f(3)$ is equal to :

- a) 180 b) 150 c) 210 d) 160

29) Let N denote the sum of the numbers obtained when two dice are rolled. If the probability that $2^{N!} < N!$ is $\frac{m}{n}$. Where $(m, n) = 1$, then $4m - 3n$ equal to:

- a) 180 b) 150 c) 210 d) 160

30) If $I(x) = \int_e^{\sin x^2} (\cos x \sin 2x - \sin x) dx$ and $I(0) = 1$, then $I(\frac{\pi}{3})$ is equal to :

a) $e^{\frac{3}{4}}$

b) $-e^{\frac{3}{4}}$

c) $\frac{1}{2}e^{\frac{3}{4}}$

d) $-\frac{1}{2}e^{\frac{3}{4}}$