

Day 12:

Task 1: Bit Manipulation Basics

Create a function that counts the number of set bits (1s) in the binary representation of an integer. Extend this to count the total number of set bits in all integers from 1 to n.

```
public class TotalSetBits {  
    public static int totalSetBits(int n) {  
        int totalBits = 0;  
        for (int i = 1; i <= n; i++) {  
            totalBits += countSetBits(i);  
        }  
        return totalBits;  
    }  
  
    private static int countSetBits(int n) {  
        return Integer.bitCount(n);  
    }  
  
    public static void main(String[] args) {  
        int n = 10;  
        System.out.println(totalSetBits(n));  
    }  
}
```

Explanation:

1 **totalSetBits** method:

- **totalSetBits**(int n) iterates through numbers from 1 to n.
- For each number i, it calls the **countSetBits**(i) method to count the set bits in i and accumulates this count in **totalBits**.
- Finally, it returns **totalBits**, which is the total number of set bits in the binary representations of the integers from 1 to n.

countSetBits method:

- **countSetBits**(int n) simply calls **Integer.bitCount(n)**, which counts the set bits in the integer n.

main method:

- In the main method, we set n = 10 and print the result of **totalSetBits**(n).
- The expected output for n = 10 is 17, which represents the total number of set bits in the binary representations of the integers from 1 to 10.

Example Output

When we run the main method with n = 10, the output will be:

17

This output means that the total number of set bits in the binary representations of the integers from 1 to 10 is 17.

Binary representation and set bits for numbers from 1 to 10:

- 1 (binary **0001**) has 1 set bit.
- 2 (binary **0010**) has 1 set bit.
- 3 (binary **0011**) has 2 set bits.
- 4 (binary **0100**) has 1 set bit.
- 5 (binary **0101**) has 2 set bits.
- 6 (binary **0110**) has 2 set bits.
- 7 (binary **0111**) has 3 set bits.
- 8 (binary **1000**) has 1 set bit.
- 9 (binary **1001**) has 2 set bits.
- 10 (binary **1010**) has 2 set bits.

Task 2: Unique Elements Identification

Given an array of integers where every element appears twice except for two, write a function that efficiently finds these two non-repeating elements using bitwise XOR operations

Explanation

Understanding XOR properties:

- XOR of a number with itself is 0: $a \oplus a = 0$.
- XOR of a number with 0 is the number itself: $a \oplus 0 = a$.
- XOR is both commutative and associative: $a \oplus b \oplus a = b \oplus (a \oplus a) = b$.

```
public class TwoNonRepeatingElements {  
    public static void findNonRepeating(int[] nums) {  
        int xor = 0;  
  
        // Step 1: Get the XOR of all elements  
        for (int num : nums) {  
            xor ^= num;  
        }  
  
        // Step 2: Find any set bit in xor (any bit where x and y differ)  
        int bitMask = 1;  
        while ((bitMask & xor) == 0) {  
            bitMask <<= 1;  
        }  
  
        int x = 0;  
        int y = 0;
```

```

// Step 3: Partition the numbers into two groups and find the non-repeating elements
for (int num : nums) {
    if ((num & bitMask) != 0) {
        x ^= num;
    } else {
        y ^= num;
    }
}

System.out.println("Non-repeating elements are: " + x + " and " + y);
}

public static void main(String[] args) {
    int[] nums = {1, 2, 3, 2, 1, 4};
    findNonRepeating(nums); // Output: Non-repeating elements are: 3 and 4
}
}

```

Output:

The output of the program will be

Non-repeating elements are: 3 and 4

Let's continue with the example array `nums = {1, 2, 3, 2, 1, 4}` and the xor value 7 (0111 in binary).

Initialization:

Start with `bitMask = 1` (0001 in binary).

Loop to find the set bit:

First iteration:

$(\text{bitMask} \& 0111) = (0001 \& 0111) = 0001$

Since this is not zero, continue.

Second iteration:

bitMask is shifted left: 0010

$(0010 \& 0111) = 0010$

This is still not zero, continue.

Third iteration:

bitMask is shifted left: 0100

$(0100 \& 0111) = 0100$

This is still not zero, continue.

Fourth iteration:

bitMask is shifted left: 1000

$(1000 \& 0111) = 0000$

This is zero, exit the loop.