

Digital Assignment-1 Solution (Set-1)

1. Convert 101010101 to decimal; the radix may not be always indicated.

$$\begin{aligned}
 N &= d \times r^8 + d \times r^7 + d \times r^6 + d \times r^5 + d \times r^4 + d \times r^3 + d \times r^2 + d \times r^1 + d \times r^0 \\
 &= 1 \times 2^8 + 0 \times 2^7 + 1 \times 2^6 + 0 \times 2^5 + 1 \times 2^4 + 0 \times 2^3 + 1 \times 2^2 + 0 \times 2^1 + 1 \times 2^0 \\
 &= 256 + 0 + 64 + 0 + 16 + 0 + 4 + 0 + 1 \\
 &= 341_{10}
 \end{aligned}$$

2. Convert 69₁₀ to binary.

ans:

1000101₂

3. Convert 69 to binary.

$$\begin{array}{r}
 2 \overline{) 69} \\
 2 \overline{) 34} \\
 \quad 1 \overline{) 17} \\
 \quad \quad 0 \overline{) 17} \\
 \quad \quad \quad 2 \overline{) 8} \\
 \quad \quad \quad \quad 1 \overline{) 1} \\
 \quad \quad \quad \quad \quad 2 \overline{) 4} \\
 \quad \quad \quad \quad \quad \quad 0 \overline{) 0} \\
 \quad \quad \quad \quad \quad \quad \quad 2 \overline{) 2} \\
 \quad \quad \quad \quad \quad \quad \quad \quad 0 \overline{) 0} \\
 \quad \quad \quad \quad \quad \quad \quad \quad \quad 1 \overline{) 1} \\
 \quad \quad \quad \quad \quad \quad \quad \quad \quad \quad 0 \overline{) 0}
 \end{array}$$

Read the remainders from bottom to top.

$$69_{10} = 1000101_2$$

4. Add 101111₂ and 10111₂.

Number 1 1 0 1 1 1 1

Number 2 1 0 1 1 1
1 0 0 0 1 1 0₂

During the addition, 1 + 1 = 10 and 1 + 1 + carry(1) = 11, and so on

5. Add 1111 and 1111.

$$\begin{array}{r}
 \text{Number 1:} \quad 1\ 1\ 1\ 1 \\
 \text{Number 2:} \quad 1\ 1\ 1\ 1 \\
 \text{Carry:} \quad \underline{1\ 1\ 1} \\
 \underline{1\ 1\ 1\ 1\ 0_2}
 \end{array}$$

Binary subtraction is performed in a manner similar to that in decimal subtraction. Because there are only two digits in binary, its subtraction often requires more borrowing operation than decimal numbers.

6. Subtract 1110 from 1000.

$$\begin{array}{r}
 10000 \\
 \underline{1110} \\
 00010_2
 \end{array}$$

We find that in the second column 1 cannot be subtracted from 0. So a 1 must be borrowed from the third column but it is a 0. In this example, 1 is available at the fifth column. So borrow this 1, leaving behind a 0. Then 1 is (1 + 1) in the fourth column. We borrow 1 leaving behind 1 in the fourth column. Finally, successive borrowing makes (1 + 1) in the second column from which we subtract 1, yielding 1 as answer in the second column. At this stage, we have the answers for zeroth and first column. The third, fourth and fifth columns are

$$\begin{array}{r}
 \text{Column} \quad 4 \quad 3 \\
 \begin{array}{c} 5 \\ 0 \end{array} \quad \begin{array}{cc} 1 & 1 \\ 1 & 1 \\ \underline{1} & \underline{1} \end{array} \\
 \underline{0 \quad 0 \quad 0}
 \end{array}$$

Thus, the complete answer is
 $00010_2 = 2_{10}$

7. Subtract 10101 from 101010.

$$\begin{array}{r}
 101010 \\
 \underline{10101} \\
 10101_2
 \end{array}$$

8. Convert 10101110111101012 to hexadecimal.

| | | | | |
|-----|------|------|------|--|
| 101 | 1110 | 1111 | 0101 | Group in four = from LSB Convert number |
| 0 | | | | |
| A | E | F | 5 | |
| | | | | |

9. Convert FA876₁₆.

| | | | | |
|-----|------|------|------|-----|
| F | A | 8 | 7 | 6 |
| 111 | 1010 | 1000 | 0111 | 011 |
| 1 | | | | 0 |

Thus, the solution is 1111, 1010, 1000, 0111, 0110₂.

10. Convert FA27D₁₆.

$$\begin{aligned}
 &F * 16^4 + A * 16^3 + 2 * 16^2 + 7 * 16^1 + D * 16^0 \\
 &= 15 * 65536 + 10 * 4096 + 2 * 356 + 7 * 16 + 13 \\
 &= 10,24,637
 \end{aligned}$$

11. Convert 57345.

| | |
|--|---|
| 16) 57345 16) 3584 - 1 16) 224 - 0 14 - 0 | ↑ |
|--|---|

14 00 1 → Convert decimal to hexadecimal notation.

↓

E 0 0 1₁₆

The result is E001₁₆.

12. Convert 1111101011012 to octal.

| | |
|--|---|
| Split the number into group of three 111 7 | 110 101 10 6 5 5 |
|--|---|

The result is 7655₈

13. Convert 67548 to binary.

| | | | |
|-----|-----|-----|-----|
| 6 | 7 | 5 | 4 |
| 110 | 111 | 101 | 100 |

The result is 110111101100₂.

14. Convert 86710 to octal number. It is simply a successive division by 8.

| | |
|---|---|
| 8) 867 8) 108 - 3 8) 13 - 4 1 - 5 | ↑ |
|---|---|

The result is (1543)₈

15. Given $m = 11010110$, $n = 01000101$

Determine (a) $(m - n)$ and (b) $(n - m)$

(a) 2's complement of n

01000101

1's complement 10111010

+1

2's complement 10111011

Add in 11010110

Delete carry $\rightarrow 1$ 10010001

$(m - n)$ 10010001

(b) 2's complement of m

11010110

1's complement 00101001

+1

2's complement 00101010

Add n 01000101

No carry 01101111

1's complement 10010000

+1 2's complement $(n -$

$m)$ 10010001

16. Convert the given decimal numbers to binary:

(i) $(258)_{10}$

(ii) $(137)_{10}$

(iii) $(11.6875)_{10}$

ans: i). 100000010

ii). 10001001

iii). 1011.1011

17. Convert the hexadecimal $(8F6)_{16}$ to a decimal number.

ans: 2294

18. How can you convert octal numbers to binary and vice versa

ans: Convert each octal number into its 3 bit binary representation.

Group 3 bits from lsb and convert it into equivalent octal notation.

19. How can you convert hexadecimal to binary and vice versa?

ans: Convert each hexadecimal number into its 4 bit binary representation.

Group 4 bits from lsb and convert it into equivalent hexadecimal notation.

20. Write the basic rules for addition and subtraction of binary numbers.

ans:

| <u>Addition :</u> | <u>Subtraction :</u> |
|-------------------|----------------------|
| $0 + 0 = 0$ | $0 - 0 = 0$ |
| $0 + 1 = 1$ | $1 - 0 = 1$ |
| $1 + 0 = 1$ | $1 - 1 = 0$ |
| $1 + 1 = 10$ | $10 - 1 = 1$ |
| $1 + 1 + 1 = 11$ | |

21. Take any two 8-bit binary numbers. Illustrate how to add and subtract the two.

| | |
|--|---|
| $ \begin{array}{r} \rightarrow 10110101 \\ (+) 01111011 \\ \hline 100110000 \\ \text{Carry} \nearrow \end{array} $ | $ \begin{array}{r} \rightarrow 10110101 \\ (-) 01111011 \\ \hline 00111010 \end{array} $ |
|--|---|

22. Find the decimal equivalents of the following binary numbers.

(a) 1111111

(b) 11001.0101

ans:

a). 127

b). 25.3125

23. Subtract in binary form:

$(47)_{10} - (23)_{10}$

ans: 11000

24. Decode the following into decimal form (H stands for Hexadecimal):

(a) FCH (b) 9AH

ans:

- a). 252
- b). 154

25. Perform the following conversions:

- (a) 279 from decimal to octal number.
- (b) 125 from decimal to octal number.
- (c) 11000111.1101 from binary to octal number.

ans:

- a). 427
- b). 175
- c). 307.64

26. Perform the indicated operations in binary:

- (a) $(32)_8 + (73)_8$
- (b) $(175)_8 - (114)_8$
- (c) $(7E)_{16} + (AD)_{16}$
- (d) $(BC)_{16} - (F4)_{11}$

ans:

- a). 1010101
- b). 0110001
- c). 100101011
- d). 11001000

27. Convert 1100 0111, 1101 to octal number.

ans:

307.64

28. Convert the decimal number 25.375 to its binary equivalent.

ans:

11001.011

29. Convert $(294.6875)_{10}$ into octal.

ans:

446.54

30. Convert the following numbers to their hexadecimal equivalents.

(a) $(49.5)_{10}$

(b) $(972.625)_{10}$

ans:

a). 31.8

b). 3CC.A

31. Convert 11000111.1101 to octal number.

ans:

307.64

