

Q1.

It is a specified observed numerical value used to estimate an unknown population parameter.

Point Estimate : - Single numerical value used to estimate an unknown population.

Interval Estimate : - Range of values used to estimate the unknown population parameter.

Q2.

```
In [1]: import math

def estimate_population_mean(sample_mean, sample_std, sample_size, confidence_level):
    margin_of_error = 1.96 * (sample_std / math.sqrt(sample_size))

    lower_bound = sample_mean - margin_of_error
    upper_bound = sample_mean + margin_of_error

    return lower_bound, upper_bound

sample_mean = 25.5
sample_std = 4.2
sample_size = 30
confidence_level = 0.95

lower_bound, upper_bound = estimate_population_mean(sample_mean, sample_std, sample_size, confidence_level)

print(f"Estimated population mean: {sample_mean:.2f}")
print(f"Confidence Interval: ({lower_bound:.2f}, {upper_bound:.2f})")
```

Estimated population mean: 25.50
Confidence Interval: (24.00, 27.00)

Q3.

- Hypothesis testing is a statistical method used to make inferences about population parameters based on a sample of data.

Importance :

- Statistical Inference
- Scientific Research
- Decision-Making in Business
- Quality control
- Medicine and Healthcare.

Q4.

Null Hypothesis :

- assumes no effect . stated as ,
population mean weight of male college students is less than
population mean weight of female college students.

Alternate Hypothesis :

- suggests that the average weight of male college students is
greater than the average weight of female college students.

Q5.

```
In [2]: import numpy as np
from scipy import stats

def two_sample_t_test(sample1, sample2, alpha=0.05):
    test_statistic, p_value = stats.ttest_ind(sample1, sample2, equal_var=False)

    return test_statistic, p_value

np.random.seed(42)
sample_size = 30
male_weights = np.random.normal(loc=175, scale=10, size=sample_size)
female_weights = np.random.normal(loc=160, scale=8, size=sample_size)
test_statistic, p_value = two_sample_t_test(male_weights, female_weights)

print("Test Statistic:", test_statistic)
print("P-value:", p_value)

if p_value < 0.05:
    print("Reject the null hypothesis. There is evidence of a significant difference")
else:
    print("Fail to reject the null hypothesis. There is no significant difference")
```

Test Statistic: 6.6048146907673155

P-value: 1.5484535940556787e-08

Reject the null hypothesis. There is evidence of a significant difference.

Q6.

Null Hypothesis :

- The assumption you are beginning with.

Alternative Hypothesis :

- opposite of null hypothesis.

Q7.

Steps :

- Formulate Hypothesis
- Collect Data
- Choose significance Level
- Conduct Test
- Make a Decision
- Draw Conclusions.

Q8.

- a number calculated from a statistical test , describes how likely you are to have found a particular set of observations if null hypothesis were true. Used in hypothesis testing to help decide whether to reject the null hypothesis.

Q9.

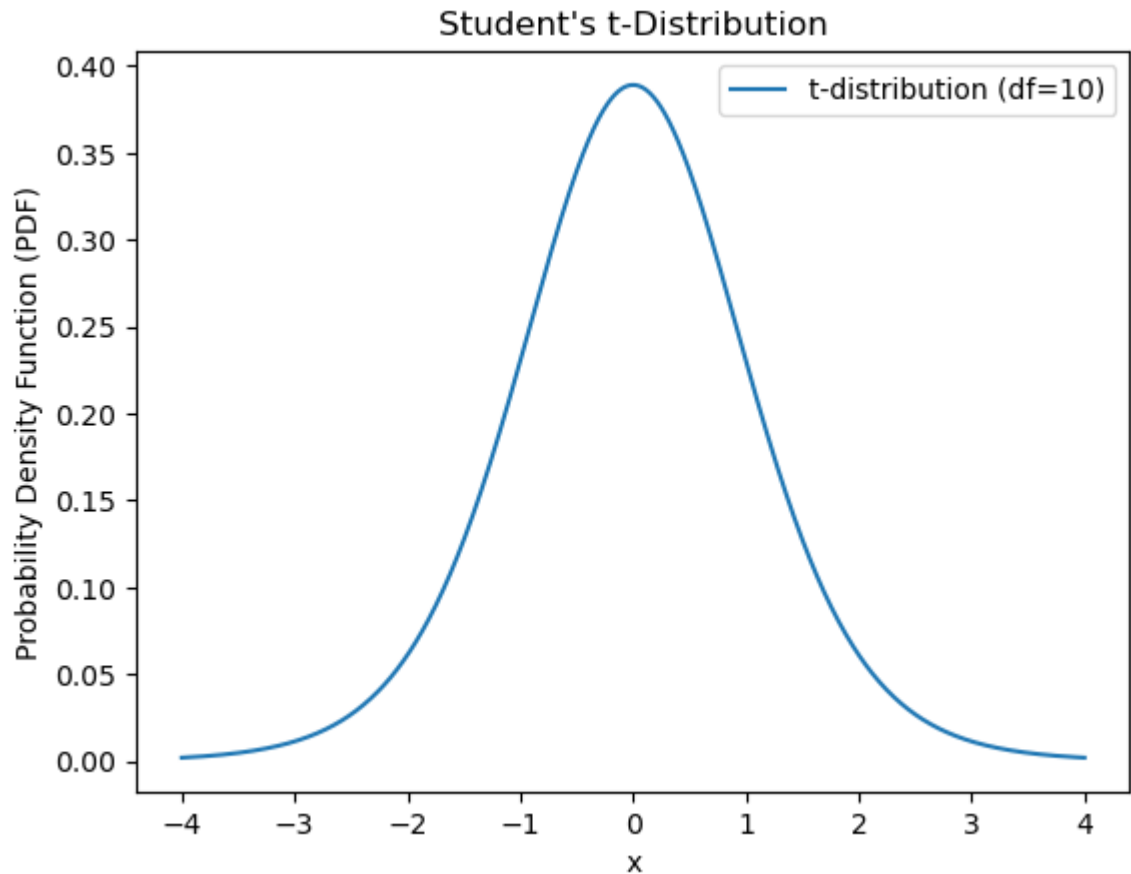
```
In [3]: import numpy as np
import matplotlib.pyplot as plt
from scipy.stats import t

degrees_of_freedom = 10

x_values = np.linspace(-4, 4, 1000)

pdf_values = t.pdf(x_values, df=degrees_of_freedom)

plt.plot(x_values, pdf_values, label=f"t-distribution (df={degrees_of_freedom})")
plt.title("Student's t-Distribution")
plt.xlabel("x")
plt.ylabel("Probability Density Function (PDF)")
plt.legend()
plt.show()
```



Q10.

```
In [4]: import numpy as np
from scipy.stats import ttest_ind

def two_sample_t_test(sample1, sample2, alpha=0.05):
    test_statistic, p_value = ttest_ind(sample1, sample2)

    return test_statistic, p_value

np.random.seed(42)
sample_size = 30
sample1 = np.random.normal(loc=10, scale=2, size=sample_size)
sample2 = np.random.normal(loc=12, scale=2, size=sample_size)

test_statistic, p_value = two_sample_t_test(sample1, sample2)

print("Test Statistic:", test_statistic)
print("P-value:", p_value)

if p_value < 0.05:
    print("Reject the null hypothesis. There is evidence of a significant difference")
else:
    print("Fail to reject the null hypothesis. There is no significant difference")
```

Test Statistic: -4.512913234547555

P-value: 3.176506547470154e-05

Reject the null hypothesis. There is evidence of a significant difference.

Q11.

- is a probability distribution that arises in the context of statistical inference.

Use :

- Unknown Population Standard Deviation
- Small Sample Size.

Q12.

- is a measure used in hypothesis testing to assess the evidence against the null hypothesis.

$$t = ((\text{sample mean}) - (\text{population mean})) / ((\text{sample standard deviation}) / (\text{math.sqrt}(n)))$$

Q13.

$$\text{degree_of_freedom} = n - 1 = 50 - 1 = 49.$$

```
In [5]: import math

sample_mean = 500
sample_std = 50
sample_size = 50
confidence_level = 0.95

df = sample_size - 1

t_critical = 2.009

margin_of_error = t_critical * (sample_std / math.sqrt(sample_size))

confidence_interval_lower = sample_mean - margin_of_error
confidence_interval_upper = sample_mean + margin_of_error

print(f"95% Confidence Interval: (${confidence_interval_lower:.2f}, ${confidence_interval_upper:.2f})")
95% Confidence Interval: ($485.79, $514.21)
```

Q14.

```
In [6]: import math

hypothesized_mean = 10
sample_mean = 8
sample_std = 3
sample_size = 100
```

```

significance_level = 0.05

df = sample_size - 1

t_statistic = (sample_mean - hypothesized_mean) / (sample_std / math.sqrt(sample_size))

critical_value_lower = -1.984
critical_value_upper = 1.984

if t_statistic < critical_value_lower or t_statistic > critical_value_upper:
    print("Reject the null hypothesis. There is evidence of a significant difference.")
else:
    print("Fail to reject the null hypothesis. There is no significant difference.")

```

Reject the null hypothesis. There is evidence of a significant difference.

Q15.

H_0 : true mean = 5 pounds H_1 : true mean < 5 pounds

$$t = 4.8 - 5 / ((0.5) / \text{math.sqrt}(25)) = -2$$

If $t < t(\text{critical})$, you reject the null hypothesis. If $t \geq t(\text{critical})$, you fail to reject the null hypothesis.

Q16.

t- stat for a two-sample t-test is given by : $t = 2.25$

If $t < t(\text{critical})$, you reject the null hypothesis. If $t \geq t(\text{critical})$, you fail to reject the null hypothesis.

Q17.

$$\text{Confidence Interval} = 4 \pm 2.576 * 0.212$$

$$\text{Margin of Error} = 2.576 * 0.212 = 0.546$$

$$\text{Confidence Interval} = (3.454, 4.546)$$

So, with 99% confidence, the population mean number of ads watched by viewers during a TV program is estimated to be between 3.454 and 4.546.