

Code

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import heapq
import numpy as np
q = []
goal = [[0,1,2], [3,4,5], [6,7,8]]
vis = set()
parent_map, move_map = {}, {}

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def manhattan(curr):

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    ans = 0

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    pos = {goal[i][j]: (i, j) for i in range(3) for j in range(3)}

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    for i in range(3):

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        for j in range(3):

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            x, y = pos[curr[i][j]]

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            ans += abs(i-x) + abs(j-y)

```

```

    return ans

```

```

def moves(curr):

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    x, y = [(i, j) for i in range(3) for j in range(3)
            if curr[i][j] == 0][0]

```

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    poss = [[0, -1, 'left'], [-1, 0, 'up'], [1, 0, 'down'],
            [0, 1, 'right']]

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    for dx, dy, direction in poss:

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        nx, ny = x+dx, y+dy

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        if 0 <= nx < 3 and 0 <= ny < 3:

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            curr1 = [row[:] for row in curr]

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            curr1[x][y], curr1[nx][ny] = curr1[nx][ny],
            curr1[x][y]

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            t_curr1 = tuple(map(tuple, curr1))

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            if t_curr1 not in vis:

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```

heapq.heappush(q, (manhattan(curr), curr))
vis.add(t - curr)
parent_map[tuple(map(tuple, curr))] = curr
move_map[tuple(map(tuple, curr))] = direction

```

```

def dfs(curr):
    vis.add(tuple(map(tuple, curr))
    if curr == goal:
        return True
    moves(curr)
    if q:
        curr = heapq.heappop(q)[1]
        if dfs(curr):
            return True
    return False

```

```

def display(board):
    print(" + - - + - - + - - + ")
    for row in board:
        print(" | " + " | ".join(str(x) if x != 0 else '2' for x in row) + " | ")
    print(" + - - + - - + - - + ")

```

```

c = [[] for i in range(3)]
for i in range(3):
    print(f"Enter elements of row {i+1}: ")
    c[i] = list(map(int, input().split()))
dfs(0)

```

```

result_path = []
directions = []
state = goal

```


while state:

result_path.append(state)

directions.append(move_map.get(tuple(map(tuple, state))))

state = parent_map.get(tuple(map(tuple, state)))

for ind, (state, direction) in enumerate(reversed(list(zip(result_path, directions))))

print(f"Step {ind}")

display(state)

if ind == 0:

print("Initial State")

if direction:

print(f"Move empty space {direction}")

print()

print(f"Steps taken: {len(result_path) - 1}")

Output :-

Enter elements of row 1: 3 7 6

Enter elements of row 2: 4 5 8

Enter elements of row 3: 2 0 1

Step 0 :

+ - - + - - + - - +

1 3 1 7 1 6 1

+ - - + - - + - - +

1 2 1 4 1 8 1

+ - - + - - + - - +

1 2 1 1 1 1 1

+ - - + - - + - - +

Initial state

Step 1 :

+	-	-	+	-	-	+	-	-	+
1	3	1	7	1	6	1			
+	-	-	+	-	-	+	-	-	+
1	4	1		1	8	1			
+	-	-	+	-	-	+	-	-	+
1	2	1	5	1	1	1			
+	-	-	+	-	-	+	-	-	+

Move empty space up

⋮

Step 59 :

+	-	-	+	-	-	+	-	-	+
1	0	1	1	1	2	1			
+	-	-	+	-	-	+	-	-	+
1	3	1	4	1	5	1			
+	-	-	+	-	-	+	-	-	+
1	6	1	7	1	8	1			
+	-	-	+	-	-	+	-	-	+

8 Move empty space up

Steps taken : 59